

# An Opportunistic DRR (O-DRR) Uplink Scheduling Scheme for IEEE 802.16-based Broadband Wireless Networks

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**Abstract**— We present a novel scheme for uplink scheduling in WiMax networks that attempts to balance worst-case fairness in bandwidth allocation with the delay requirements of traffic, while taking the varying nature of the wireless channel into account. We assume a polling-based mode of operation at the base station (*BS*), and provide a method of obtaining an optimal polling interval  $k$  at which the *BS* should poll the subscriber stations (*SSs*) to ensure that the delay requirements of traffic are met, while the relative unfairness in bandwidth allocation remains bounded. We devise an *opportunistic deficit round robin (O-DRR)* scheme that schedules sessions by taking into account the variations in the wireless channel, and demonstrate that there exists a range of values  $k$  of the polling interval over which our proposed scheduler is fair (as measured by Jain’s fairness index), thus giving a service provider a choice of balancing fairness with delay, and pricing its services accordingly.

## I. INTRODUCTION

Among various broadband access systems, fixed broadband wireless access (FBWA) systems are expected to be the most flexible systems in the future. Although a fiber optic links and digital subscriber line link (DSL) are existing broadband wired technologies in the last mile, broadband wireless access (BWA) [1] based services, have the advantages of fast deployment, dynamic sharing of radio resources, and low cost. Due to the upcoming different air interface technologies, BWA systems promise high data rates in the last mile. BWA systems are expected to support QoS for real time applications, such as video conferencing, video streaming and voice-over-IP . IEEE 802.16 [1], [2], [3] is a BWA standard, sponsored by the IEEE LAN/MAN society, operating in the 2-11 GHz range and provides non line of sight (NLOS) access. The IEEE 802.16 (or the so-called WiMax) standard defines the physical (PHY) and medium-access control (MAC) layers for fixed (and, eventually, mobile) broadband wireless access networks.

The WiMax standard, in its simplest form, uses time-division duplex (TDD), and provides access to each subscriber station (*SS*)/user using demand assignment multiple-access time-division multiple access (DAMA-TDMA). DAMA is a capacity assignment technique that adapts to the demands of multiple users by dynamically assigning time slots to users depending on their bandwidth and QoS requirements.

In WiMax, time is divided into frames, each of which, in turn, is composed of a fixed number of slots [4], [5], [6]. Each frame consists of an *uplink subframe* and a *downlink subframe* (cf. Fig. 1). Requests by *SSs* are made during control slots in the uplink subframe, while grants from the *BS* are communicated to *SSs* during control slots in the downlink subframe.

The grants thus communicated are used to schedule data either in the uplink subframe corresponding to the ongoing frame or the next one. While the WiMax standard specifies the grant mechanisms, it leaves open the scheduling mechanism to be used allowing for different providers, vendors to innovate in this area. To fill the gap, we suggest a polling-based opportunistic deficit round robin (O-DRR) scheduling scheme for the uplink flows in WiMax. This is a unique scheme and attempts to balance worst-case fairness in bandwidth allocation with the delay requirements of traffic, while taking the varying nature of the wireless channel into account.

The rest of the paper is organized as follows. In Section II, we discuss the various QoS classes defined in WiMax standard and the need of a scheduling mechanism for WiMax. We give an operational overview of our O-DRR scheme in Section III. Further, in Section IV, we explain the optimization technique to find the polling interval for uplink scheduling. A closed-form expression is obtained to find the polling interval for different classes of traffic. In Section V we explain the bandwidth assignment technique to *SSs*/users using our O-DRR scheme, which exploit the channel condition between *BS* and *SSs* during the scheduling process. Finally, in Section VI, we discuss our simulation model and experiments.

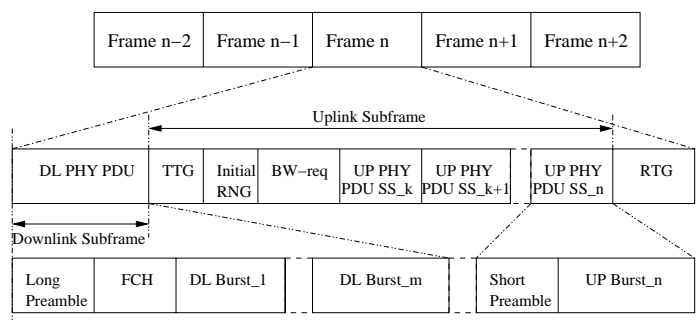


Fig. 1. Frame Structure in IEEE 802.16

## II. IEEE 802.16 QOS CLASSES AND SCHEDULING

The IEEE 802.16 standard [2] can support multiple communication services (data, voice and video) with different QoS requirements. The MAC layer defines QoS signaling mechanisms and functions that can control *BS* and *SS* data transmissions.

On the downlink, the transmission is relatively simple, because the *BS* is the only one that transmits during a

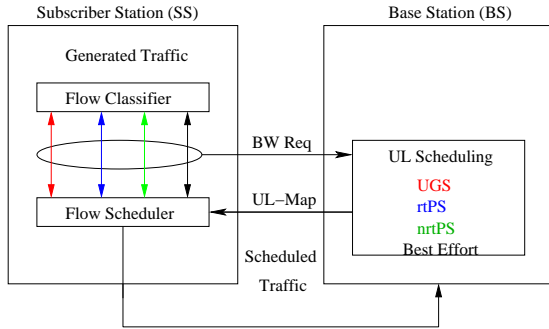


Fig. 2. QoS Architecture of IEEE 802.16

downlink sub-frame. Data packets are broadcast to all *SSs* and an *SS* only listens in on the packets destined for it. On the uplink, the *BS* determines the number of time slots for which each *SS* will be allowed to transmit in an uplink sub-frame. This information is broadcast by the *BS* through the uplink map message (UL-MAP) at the beginning of each frame. The UL-MAP contains an information element (IE) per *SS*, which includes the transmission opportunities for each *SS*, i.e., the time slots in which a *SS* can transmit during the uplink sub-frame. The *BS* uplink-scheduling module determines the IEs by using the bandwidth request message sent from the *SSs* to the *BS*.

In the IEEE 802.16 standard, bandwidth-requests are normally transmitted in two modes: a *contention mode* and a *contention-free mode* (polling). In the contention mode, the *SSs* send bandwidth-requests during a contention period, and contention is resolved by the *BS* using an exponential back-off strategy. In the contention-free mode, the *BS* polls each *SS*, and an *SS* in reply sends its BW-request. There are four types of basic services described in the standard. Namely, Unsolicited Grant Service (UGS); Real-Time Polling Service (rtPS); Non-Real-Time Polling Service (nrtPS); Best Effort (BE) service [2]. Variable bandwidth assignment is possible in rtPS, nrtPS and BE services, whereas UGS service needs fixed and dedicated bandwidth assignment. Figure 2 shows the QoS architecture of IEEE 802.16 based services.

#### A. Scheduling in IEEE 802.16-based Network

IEEE 802.16 standard defines the QoS signaling mechanisms, whereas it is silent on the scheduling policy for the services and users. Scheduling in both uplink and downlink are left open in the standard. However, the standard defines grant per SS basis (GPSS) [2] and grant per connection basis (GPC) schemes for scheduling. Scheduling in the downlink direction is simpler than in the uplink direction. This is because, the *BS* has the knowledge of all queues assigned to *SSs* in the downlink, whereas it does not have in the uplink. *BS* can use a scheduler similar to that used in traditional wire-line network in downlink scheduling, whereas in the uplink, it can't. This is because the *BS* does not have the complete information of all *SSs* and the links are wireless in nature with random channel characteristics. Also, IEEE 802.16 is a frame based system, not like usual packet based or TDMA system. The usual scheduling algorithms of wire-line networks like WFQ [7], SCFQ [8], W<sup>2</sup>FQ [9] and wireless network like TBFQ [10] can't be used here. This is because WiMax is not a work conserving scheme and definition of time, virtual

time, service time for the incoming packets of connected *SSs* are not possible at the *BS*. Hence there is a need of a new uplink scheduling algorithm for IEEE 802.16 based networks. Our aim in this paper is to find a new scheduling mechanism in the uplink for IEEE 802.16 based network. In the following sections we discuss our proposed scheduling algorithm for IEEE 802.16 based networks. This is a unique scheme and is completely different from usual wire-line and wireless scheduling algorithms.

### III. OPERATIONAL OVERVIEW

Our scheme works by obtaining a list of *schedulable users*, based on the traffic requirements of the users and the signal-to-interference-plus-noise ratio (SINR) of the wireless channel. In our scheme, polling is performed by the *BS*, only once every  $k$  frames, which we term a *scheduling epoch*. That is, once every  $k$  frames the *BS* determines the set of *SSs* that are *eligible* to transmit, and their bandwidth requirements. We label these *SSs* the *eligible set*. An *SS* is eligible if, at the polling instant, it has a non-empty queue and the SINR of its wireless link to the *BS* is above a minimum threshold (say,  $SINR_{th}$ ). We observe here that the SINR of a wireless link between a *SS* and a *BS* is obtainable in the IEEE 802.16-standard, during each frame, from measurements that are automatically made at the physical layer.

Once determined, the membership of the eligible set is frozen for the entire scheduling epoch. We also define a *schedulable SS* to be one that is eligible during a given frame of a scheduling epoch and that was eligible at the start of that epoch. During a scheduling epoch, therefore, the *BS* only schedules traffic from the schedulable set. (That is, the *BS* does not discover the status of the queue and wireless link of the remaining *SSs* in the network until its next polling opportunity.)

For each subsequent frame in the scheduling epoch (that is, for every frame for the next  $k$  frames), the *BS* schedules, using Opportunistic Deficit Round Robin (to be described shortly), the transmissions of the *schedulable SSs*. Note that the membership of the schedulable set *changes dynamically* from frame to frame during a scheduling epoch, depending on the state of the wireless channel between the *SS* and the *BS*. At the end of  $k$  frames, the *BS* recomputes the states of all of the *SSs* (by polling), and begins the above process over again.

The best choice of the polling interval  $k$  is determined by considering the maximum delay that a set of *SSs* can tolerate and the worst-case relative fairness in their bandwidth allocations. That is, our goal is to ensure that we choose a  $k$  such that every session is polled within a time  $kT_f$  (where  $T_f$  is the duration of a frame) that is less than its delay tolerance  $T_D$ , while still being fair to the different sessions.

### IV. DETERMINING THE OPTIMAL POLLING INTERVAL $k$

As explained earlier, the *BS* needs to poll the *SSs* to discover the bandwidth and QoS requirements of the *SSs*. Intuitively, there is a trade off here. If the *BS* polls very frequently, it would have the most current information and may successfully satisfy the QoS requirements of the *SSs*, but the polling overhead, and, therefore, the efficiency, would be low. By contrast, if the *BS* polls the *SSs* very infrequently, it may have a very low overhead but would likely run the

Scheduling epoch Frame = 1			
SS	SINR	DRR Flag	Lag/Lead
1	20	0	+Q
2	35	1	-Q
3	30	1	-Q
4	25	0	+Q

Scheduling epoch Frame = 2			
SS	SINR	DRR Flag	Lag/Lead
1	32	1	+2Q
2	35	1	0
3	30	1	0
4	33	1	+2Q

Fig. 3. Operation of O-Deficit Round Robin Scheduling

risk of being quite unfair to the traffic at the  $SS$ s and of not meeting their QoS requirements (e.g. delay constraints). So, it is crucial to find appropriate value for  $k$ , such that both efficiency and fairness are balanced. Our proposal is to minimize a combination of the worst-case relative fairness in bandwidth plus the normalized delay, such that the provider can choose the relative weightage of fairness and delay.

We denote the duration in slots of the downlink subframe by  $T_{dl}$  and the duration in slots of the uplink subframe by  $T_{ul}$ . So that the frame duration  $T_f = T_{ul} + T_{dl}$  slots.

In our scheme, the  $BS$  maintains a list  $L$  of the addresses of all  $SS$ s. If we denote by  $\phi_i$  the ideal share of bandwidth to be obtained by  $SS_i$ , the slots in the uplink subframe  $T_{ul}$  can be divided proportionately among the  $SS$ s in the ratio of their  $\phi_i$ 's. The  $BS$  polls the  $SS$ s to discover their bandwidth requirements and updates an active list  $L_{active}$  of  $SS$ s, with the polling repeated at the start of every scheduling epoch.

Although the  $BS$  polls the  $SS$ 's only once at the start of each scheduling epoch the, scheduling itself is performed in each frame, based on the opportunity condition  $SINR_i \geq SINR_{th}$ , where  $SINR_i$  is the SINR of the channel between the  $BS$  and  $SS_i$ . Hence, polling is done over  $kT_f$  slots, whereas the scheduling is done over  $T_f$  slots. Therefore, if a packet/data at an  $SS$  misses one round of polling, it will require at least  $(k+1)T_f$  time slots to be transmitted.

Let  $i$  and  $j$  be a pair of  $SS$ s that are maximally backlogged during an interval  $(t_1, t_2)$ . The *fairness measure*  $FM(t_1, t_2)$  over all pairs of flows/ $SS$ s  $i$  and  $j$  that are backlogged in interval  $(t_1, t_2)$  is defined as:

$$FM(t_1, t_2) = \left( \frac{sent_i(t_1, t_2)}{\phi_i} - \frac{sent_j(t_1, t_2)}{\phi_j} \right), \quad (1)$$

where  $sent_i(t_1, t_2)$  and  $sent_j(t_1, t_2)$  represent the amount of traffic sent by the backlogged flows  $i$  and  $j$ , respectively, and  $\phi_i$  and  $\phi_j$  represent the bandwidth share of flows  $i$  and  $j$ , respectively.

If the share of all  $SS$ s is equal (when all are backlogged),  $\phi_i = \phi_j = 1$ , and  $\sum_i \phi_i = N$ , where  $N$  is the total number of  $SS$ s in the system. As discussed in [11], if  $Q_i$  is the quantum of slots for  $SS_i$  in each round of a DRR scheme, then we define:

$$\phi_i = \frac{Q_i}{Q}, \text{ where } Q = \min_i \{Q_i\} = \frac{T_f}{N}. \quad (2)$$

The worst-case occurs when only one  $SS$  (say  $SS_i$ ) is backlogged at the instant of polling by the  $BS$ , but each of

the  $N-1$  remaining  $SS$ 's becomes backlogged *immediately* thereafter. Hence,  $Q_i = T_f$  and  $\phi_i = N$ . In this case, the worst-case fairness measure  $FM_w(t_1, t_2)$  can be expressed as:

$$FM_w(t_1, t_2) = \left( \frac{R(t_2 - t_1)}{N} \right). \quad (3)$$

The worst case time interval for our system occurs when  $(t_2 - t_1) = kT_f$ . Note that each frame actually consists of both uplink as well as downlink slots, while it is only the uplink slots that are used for  $SS$  to  $BS$  transmission. Assuming that the uplink and downlink subframes occupy an equal number of slots, and that there is no wastage of slots (i.e., the administrative slots are negligible, so that all the slots in the uplink can be assigned to the traffic), the usable slots in  $(t_2 - t_1)$  are  $\alpha kT_f$ , where  $\alpha$  is a system parameter that lies between 0 and 1. We assume  $\alpha = \frac{1}{2}$ , henceforth. So, the worst case fairness measure  $FM(t_1, t_2)$  is:

$$FM_w(t_1, t_2) = FM_w(kT_f) = \left( \frac{\alpha RkT_f}{N} \right), \quad (4)$$

where  $R$  is the maximum data rate that is achievable at this moment (as per the IEEE 802.16 standard it is 120Mbps for 64-QAM modulation scheme). Our aim is to find a  $k$  such that the  $BS$  can poll the  $SS$ s to achieve the smallest worst-case fairness measure  $FM_w$  and minimum delay. For this, we define a normalized delay ( $ND$ ) as:  $ND = \frac{T_D}{kT_f}$ , where  $T_D$  is the delay bound of traffic at a  $SS$  (the maximum delay that a flow for a particular application can tolerate, e.g., 10msec, 50msec, 200msec and 500msec for UGS, rtPS, nrtPS and BE services, respectively). We would like the optimal  $k$  in our solution to be such that the worst case fairness measure and normalized delay are minimum. This can be achieved by the following optimization framework.

$$\min_k f(k) = c_1 |FM_w(k)| + c_2 ND(k), \quad (5)$$

where  $c_1$  is the cost for unit of  $FM$  per bit and  $c_2$  is the cost per normalized delay. The worst case value of  $k$  can be found at the equilibrium point, where,  $c_1 |FM'_w(k)| = -c_2 ND'(k)$ , which simplifies to,

$$k = \sqrt{\left( \frac{c_2 NT_D}{c_1 R \alpha T_f^2} \right)} = \sqrt{\left( c \frac{NT_D}{R \alpha T_f^2} \right)}, \quad (6)$$

where  $c$  is the ratio of the cost per unit delay to the cost per unit  $FM$ . The value of  $c$  depends upon the type of traffic, as the value of  $T_D$  is different for different traffic types.

Having obtained the optimum value of  $k$ , we perform uplink bandwidth assignments using our modified DRR algorithm.

#### V. BANDWIDTH ASSIGNMENT USING OPPORTUNISTIC DRR (O-DRR)

We suggest a deficit round robin (DRR) based scheduling technique that runs at the  $BS$  to allocate bandwidth to the contending uplink flows. Our scheme assumes that: (i) The channel between the  $SS$  and the  $BS$  is a Rayleigh fading channel, (ii) the coherence time of the channel is greater than the frame length (the IEEE 802.16 standard for point-to-multipoint network supports the frame lengths of is 0.5msec, 1msec, and 2msec), i.e., the channel does not change during a frame duration and that the (iii) SINR of each channel is known to the  $BS$  (which, as pointed out earlier, is obtainable from measurements at the physical layer).

We utilize DRR's idea of maintaining a quantum size  $Q_i$  and a deficit counter for  $SS_i$ , which we term the lead/lag counter  $L_i$ . The  $BS$  also maintains an indicator variable  $DRRFlag_i$  for each  $SS$ .  $DRRFlag_i = 1$ , if  $SS_i$  is assigned bandwidth in this frame, else  $DRRFlag_i = 0$ . If, at a polling interval  $n$  during a scheduling epoch,  $SINR_i$  is less than  $SINR_{th}$ ,  $SS_i$  is not scheduled, and its quantum  $Q_i$  is distributed among the remaining  $SS$ s in proportion to their weights, while  $SS_i$ 's lead/lag counter is *incremented* by  $Q_i$ , the amount of service it missed. Likewise, the lead/lag counter of an  $SS_j$  that received more than its minimum share  $Q_i$  of the uplink slots is decremented by the amount of slots that  $SS_j$  received over and above its quantum  $Q_j$ . The idea being to enforce fairness between different  $SS$ 's in the long term.

Figure 3 illustrates our O-DRR scheme. We assume that the minimum SINR requirement for each  $SS$  is 30dB, the share for each user  $i$  is  $Q$  and all users have data to send. We also assume the lag/lead counter is 0 for each user at the beginning of the  $k^{th}$  scheduling epoch. At the  $k^{th}$  epoch,  $SS$ 's 1 and 4 do not satisfy the SINR requirements, so their DRR flag is set to zero while the DRR flags of  $SS$ s 1 and 3 are set to 1. Since,  $SS$ s 1 and 4 are lagging, their lag/lead counter is set to  $+Q$  after the first scheduling frame. Similarly, the lag/lead counters of  $SS$ s 2 and 3 are set to  $-Q$  after the first scheduling frame, since  $SS$ s 2 and 3 are assigned their normal share  $Q$  and also receive the unused share  $Q$  of  $SS$ s 1 and 4. In the next frame, the SINR of each link exceeds the threshold. Hence, the DRR flag for each  $SS$  is 1.  $SS$ s 1 and 4 now receive bandwidth  $2Q$  where as  $SS$ s 2 and 3 receive bandwidth 0. This is because  $SS$ s 2 and 3 have already used  $2Q$  slots each in the previous polling interval, so their share in the current polling interval is reduced by the extra share previously received. This dynamic bandwidth assignment process continues and the  $BS$  schedules the  $SS$ s at a polling frequency obtained from Eq. 6. Our scheduling algorithm for the uplink flows, based on DRR is explained in Algorithm 1.

#### VI. SIMULATION MODEL AND EXPERIMENT

We simulated an IEEE 802.16 environment with one  $BS$  and different sets of  $SS$ s ( $N = 50, 100$ ). The optimization-based method to determine the polling interval, described in Section IV was used to find the range of values of  $k$  and the worst case  $k$ . Using simulations with different sets of  $N$ ,  $T_D$ ,  $T_f$  and  $R$ , we obtained a set of  $c$ s and  $k$ s, summarized in Table I. A WiMax service provider can thus select a  $c$  that is

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#### Algorithm 1 : O-DRR Algorithm for UL Scheduling (at $BS$ )

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- 1: Set initial  $k = k_{initial}$ , the polling interval,
  - 2: Set the *polling timer* =  $kT_f$
  - 3: **if** *polling timer* has not expired **then**
  - 4:  $BS$  polls and updates the  $SINR$ , Queue state for each  $SS$
  - 5:  $BS$  updates the active list ( $L_{active}$ ) of  $SS$ . ( $i \in L_{active}$ , if  $(I(SINR_i > SINR_{th_i}) \wedge Queue\ state_i)! = 0$ )
  - 6: **for**  $\forall i \in L_{active}$  of  $BS$ , check  $SINR_i$  **do**
  - 7:     **if**  $SINR_i \leq SINR_{th_i}$  **then**
  - 8:         Withdraw the BW assigned to  $SS_i$  and mark  $SS_i$  as "lagging" other  $SS$ s as "leading"
  - 9:         Re-assign the withdrawn BW to "leading"  $SS$ s proportionate to their weights  $\phi_i$ .
  - 10:     **end if**
  - 11:     **end for**
  - 12: **else**
  - 13:     Update  $k$  (either with off-line values of  $k$  or by using the Eqn. 6)
  - 14: **end if**
  - 15: Continue with step 2
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most suitable for the business, provided the delay and fairness constraints of the users are met. We then simulated the O-DRR algorithm described in Algorithm 1. For different  $N, k$ , we observed the the lag/lead counter of each  $SS$ , the instantaneous queue status of each  $SS$ , the delay characteristics of the scheduler, the queue size of each  $SS$  over a long time interval (1000 frames). The queue sizes were found to be bounded over the period. The lag/lead counter and the slot allocation varied with SINR and  $k$ . Assuming 100 slots per  $T_{ul}$ , we show how the slots assignment for 100 users varied with different  $k$  in Figs. 4, 5, 6. Each point in each of the curves was obtained by averaging the  $SS$  slot assignments over several simulation runs. We observe that as  $k$  increases, the difference in the number of slot assignment to different  $SS$ s also increases (as expected). We see from Figure 5 that Jain's Fairness Index [12], however, remains above 90% for a fairly large range of  $k$ , suggesting that it is possible for the provider to trade of fairness for delay by choosing an appropriate value of  $k$  at which the fairness and the bandwidth requirements of different users are satisfied.

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$N/T_D$	N=10	50	100	$k$	Comments
50msec	$c = 1200 - 243 * 10^3$	$c = 1200 - 9.72 * 10^3$	$c = 1200 - 24.3 * 10^3$	1-45	rtPS Traffic
200msec	$c = 300 - 972 * 10^3$	$c = 300 - 194.4 * 10^3$	$c = 300 - 97.2 * 10^3$	1-180	nrtPS Traffic
500msec	$c = 120 - 2430 * 10^3$	$c = 120 - 486 * 10^3$	$c = 120 - 243 * 10^3$	1-450	BE Traffic

TABLE I

PARAMETERS OF OPTIMIZATION BASED POLLING IN IEEE 802.16 ( $R = 120Mbps, T_f = 1msec, \alpha = 0.5$ )

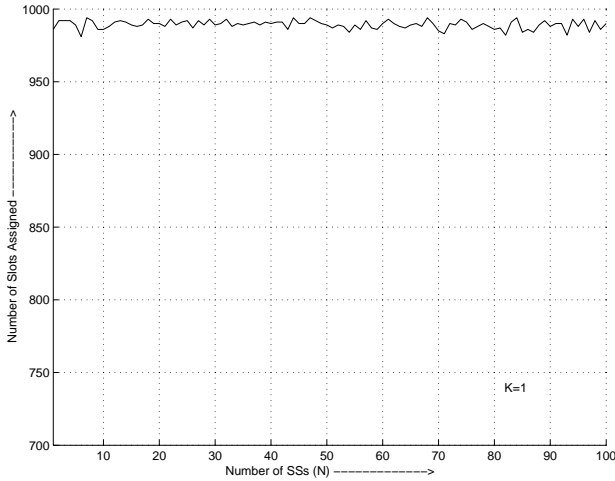


Fig. 4. Slots Assigned with  $k=1$

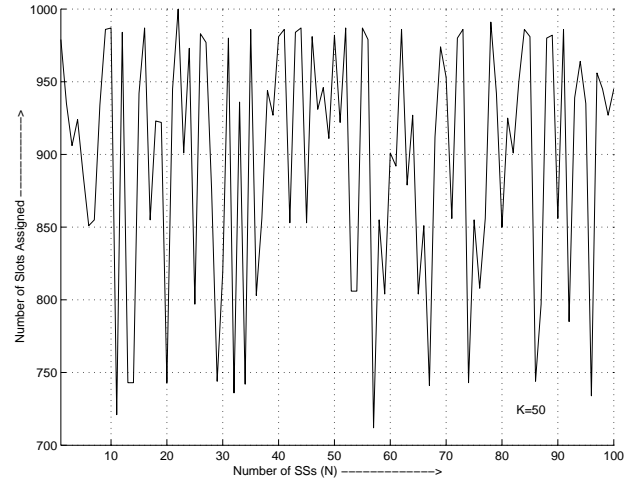


Fig. 6. Slots Assigned with  $k=50$

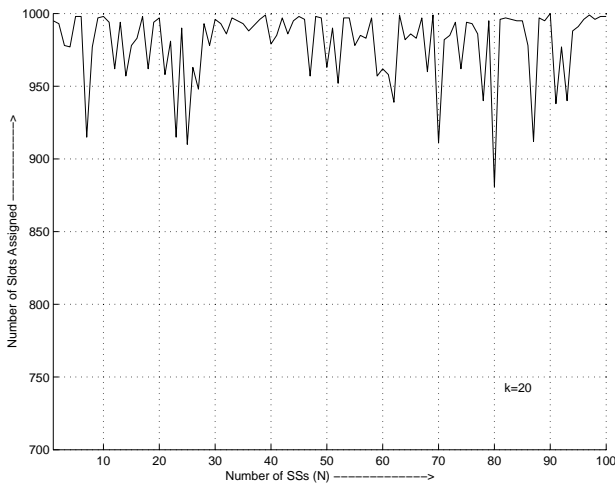


Fig. 5. Slots Assigned with  $k=20$

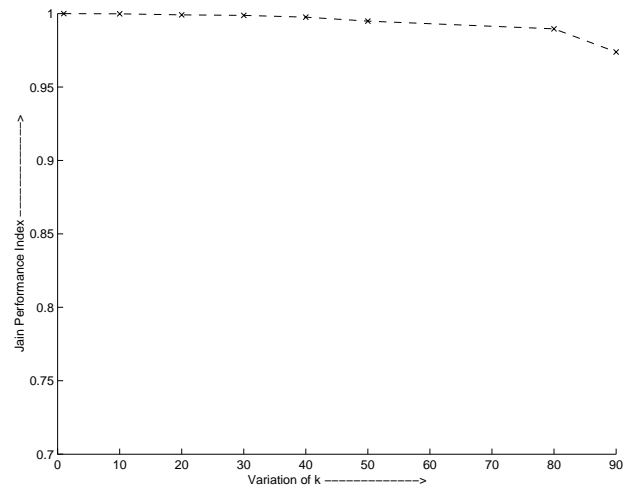


Fig. 7. Fairness in BW using Jain's Fairness Index

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