

EE101: Op Amp circuits (Part 5)



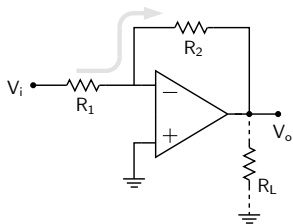
M. B. Patil

mbpatil@ee.iitb.ac.in

www.ee.iitb.ac.in/~sequel

Department of Electrical Engineering
Indian Institute of Technology Bombay

Feedback: inverting amplifier

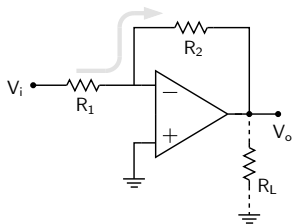


$$V_o = A_V(V_+ - V_-) \quad (1)$$

Since the Op Amp has a high input resistance,
 $i_{R1} = i_{R2}$, and we get,

$$V_- = V_i \frac{R_2}{R_1 + R_2} + V_o \frac{R_1}{R_1 + R_2} \quad (2)$$

Feedback: inverting amplifier



$$V_o = A_V(V_+ - V_-) \quad (1)$$

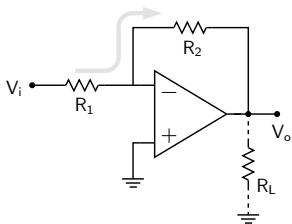
Since the Op Amp has a high input resistance,
 $i_{R1} = i_{R2}$, and we get,

$$V_- = V_i \frac{R_2}{R_1 + R_2} + V_o \frac{R_1}{R_1 + R_2} \quad (2)$$

$$V_i \uparrow \rightarrow V_- \uparrow \rightarrow V_o \downarrow \rightarrow V_- \downarrow$$

Eq. 2 Eq. 1 Eq. 2

Feedback: inverting amplifier



$$V_o = A_V(V_+ - V_-) \quad (1)$$

Since the Op Amp has a high input resistance,
 $i_{R1} = i_{R2}$, and we get,

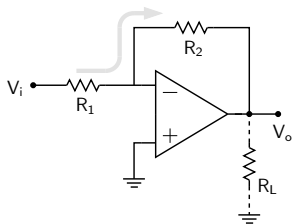
$$V_- = V_i \frac{R_2}{R_1 + R_2} + V_o \frac{R_1}{R_1 + R_2} \quad (2)$$

$$V_i \uparrow \rightarrow \boxed{V_- \uparrow} \rightarrow V_o \downarrow \rightarrow \boxed{V_- \downarrow}$$

Eq. 2 Eq. 1 Eq. 2

The circuit reaches a stable equilibrium.

Feedback: inverting amplifier



$$V_o = A_V(V_+ - V_-) \quad (1)$$

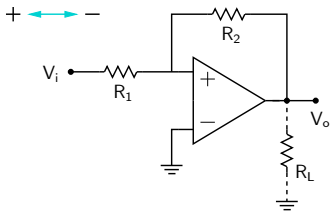
Since the Op Amp has a high input resistance, $i_{R1} = i_{R2}$, and we get,

$$V_- = V_i \frac{R_2}{R_1 + R_2} + V_o \frac{R_1}{R_1 + R_2} \quad (2)$$

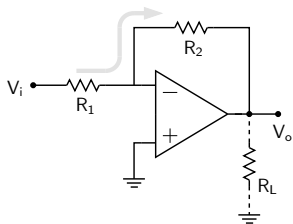
$$V_i \uparrow \rightarrow \boxed{V_- \uparrow} \rightarrow V_o \downarrow \rightarrow \boxed{V_- \downarrow}$$

Eq. 2 Eq. 1 Eq. 2

The circuit reaches a stable equilibrium.



Feedback: inverting amplifier



$$V_o = A_V(V_+ - V_-) \quad (1)$$

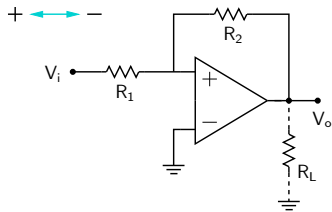
Since the Op Amp has a high input resistance, $i_{R1} = i_{R2}$, and we get,

$$V_- = V_i \frac{R_2}{R_1 + R_2} + V_o \frac{R_1}{R_1 + R_2} \quad (2)$$

$$V_i \uparrow \rightarrow \boxed{V_- \uparrow} \rightarrow V_o \downarrow \rightarrow \boxed{V_- \downarrow}$$

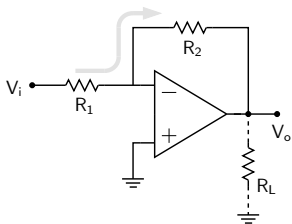
Eq. 2 Eq. 1 Eq. 2

The circuit reaches a stable equilibrium.



$$V_+ = V_i \frac{R_2}{R_1 + R_2} + V_o \frac{R_1}{R_1 + R_2} \quad (3)$$

Feedback: inverting amplifier



$$V_o = A_V(V_+ - V_-) \quad (1)$$

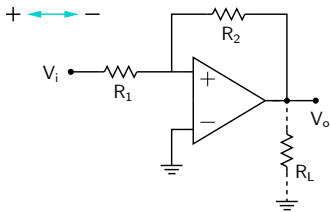
Since the Op Amp has a high input resistance, $i_{R1} = i_{R2}$, and we get,

$$V_- = V_i \frac{R_2}{R_1 + R_2} + V_o \frac{R_1}{R_1 + R_2} \quad (2)$$

$$V_i \uparrow \rightarrow \boxed{V_- \uparrow} \rightarrow V_o \downarrow \rightarrow \boxed{V_- \downarrow}$$

Eq. 2 Eq. 1 Eq. 2

The circuit reaches a stable equilibrium.

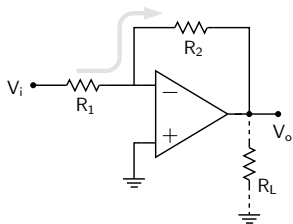


$$V_+ = V_i \frac{R_2}{R_1 + R_2} + V_o \frac{R_1}{R_1 + R_2} \quad (3)$$

$$V_i \uparrow \rightarrow V_+ \uparrow \rightarrow V_o \uparrow \rightarrow V_+ \uparrow$$

Eq. 3 Eq. 1 Eq. 3

Feedback: inverting amplifier



$$V_o = A_V(V_+ - V_-) \quad (1)$$

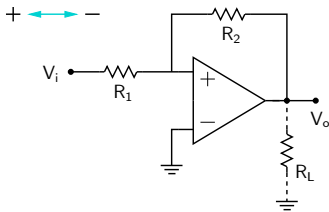
Since the Op Amp has a high input resistance, $i_{R1} = i_{R2}$, and we get,

$$V_- = V_i \frac{R_2}{R_1 + R_2} + V_o \frac{R_1}{R_1 + R_2} \quad (2)$$

$$V_i \uparrow \rightarrow V_- \uparrow \rightarrow V_o \downarrow \rightarrow V_- \downarrow$$

Eq. 2 Eq. 1 Eq. 2

The circuit reaches a stable equilibrium.



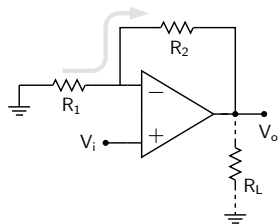
$$V_+ = V_i \frac{R_2}{R_1 + R_2} + V_o \frac{R_1}{R_1 + R_2} \quad (3)$$

$$V_i \uparrow \rightarrow V_+ \uparrow \rightarrow V_o \uparrow \rightarrow V_+ \uparrow$$

Eq. 3 Eq. 1 Eq. 3

We now have a positive feedback situation. As a result, V_o rises (or falls) indefinitely, limited finally by saturation.

Feedback: noninverting amplifier

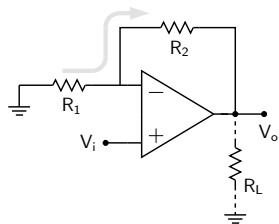


$$V_o = A_V(V_+ - V_-) \quad (1)$$

Since the Op Amp has a high input resistance,
 $i_{R1} = i_{R2}$, and we get,

$$V_- = V_o \frac{R_1}{R_1 + R_2} \quad (2)$$

Feedback: noninverting amplifier



$$V_o = A_V(V_+ - V_-) \quad (1)$$

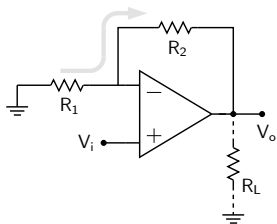
Since the Op Amp has a high input resistance,
 $i_{R1} = i_{R2}$, and we get,

$$V_- = V_o \frac{R_1}{R_1 + R_2} \quad (2)$$

$$V_i \uparrow \rightarrow V_o \uparrow \rightarrow V_- \uparrow \rightarrow V_o \downarrow$$

Eq. 1 Eq. 2 Eq. 1

Feedback: noninverting amplifier



$$V_o = A_V(V_+ - V_-) \quad (1)$$

Since the Op Amp has a high input resistance,
 $i_{R1} = i_{R2}$, and we get,

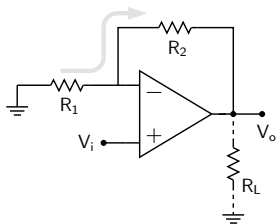
$$V_- = V_o \frac{R_1}{R_1 + R_2} \quad (2)$$

$$V_i \uparrow \rightarrow \boxed{V_o \uparrow} \rightarrow V_- \uparrow \rightarrow \boxed{V_o \downarrow}$$

Eq. 1 Eq. 2 Eq. 1

The circuit reaches a stable equilibrium.

Feedback: noninverting amplifier



$$V_o = A_V(V_+ - V_-) \quad (1)$$

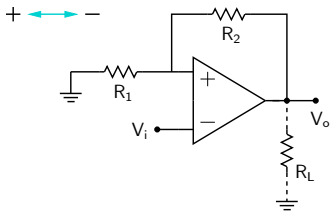
Since the Op Amp has a high input resistance, $i_{R1} = i_{R2}$, and we get,

$$V_- = V_o \frac{R_1}{R_1 + R_2} \quad (2)$$

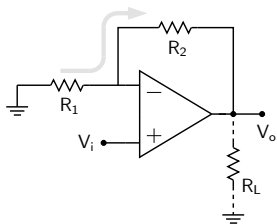
$$V_i \uparrow \rightarrow \boxed{V_o \uparrow} \rightarrow V_- \uparrow \rightarrow \boxed{V_o \downarrow}$$

Eq. 1 Eq. 2 Eq. 1

The circuit reaches a stable equilibrium.



Feedback: noninverting amplifier



$$V_o = A_V(V_+ - V_-) \quad (1)$$

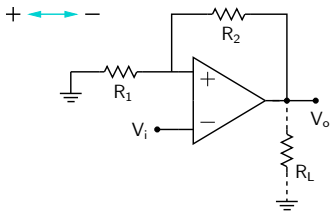
Since the Op Amp has a high input resistance, $i_{R1} = i_{R2}$, and we get,

$$V_- = V_o \frac{R_1}{R_1 + R_2} \quad (2)$$

$$V_i \uparrow \rightarrow \boxed{V_o \uparrow} \rightarrow V_- \uparrow \rightarrow \boxed{V_o \downarrow}$$

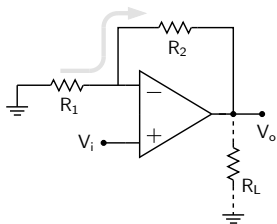
Eq. 1 Eq. 2 Eq. 1

The circuit reaches a stable equilibrium.



$$V_+ = V_o \frac{R_1}{R_1 + R_2} \quad (3)$$

Feedback: noninverting amplifier



$$V_o = A_V(V_+ - V_-) \quad (1)$$

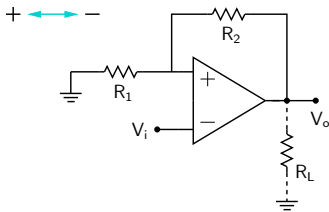
Since the Op Amp has a high input resistance, $i_{R1} = i_{R2}$, and we get,

$$V_- = V_o \frac{R_1}{R_1 + R_2} \quad (2)$$

$$V_i \uparrow \rightarrow \boxed{V_o \uparrow} \rightarrow V_- \uparrow \rightarrow \boxed{V_o \downarrow}$$

Eq. 1 Eq. 2 Eq. 1

The circuit reaches a stable equilibrium.

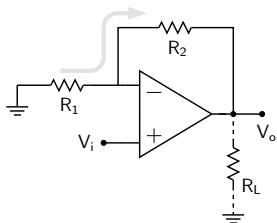


$$V_+ = V_o \frac{R_1}{R_1 + R_2} \quad (3)$$

$$V_i \uparrow \rightarrow V_o \downarrow \rightarrow V_+ \downarrow \rightarrow V_o \downarrow$$

Eq. 1 Eq. 3 Eq. 1

Feedback: noninverting amplifier



$$V_o = A_V(V_+ - V_-) \quad (1)$$

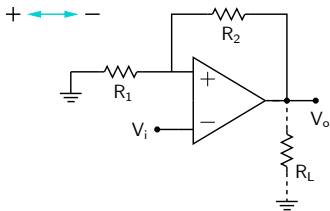
Since the Op Amp has a high input resistance, $i_{R1} = i_{R2}$, and we get,

$$V_- = V_o \frac{R_1}{R_1 + R_2} \quad (2)$$

$$V_i \uparrow \rightarrow \boxed{V_o \uparrow} \rightarrow V_- \uparrow \rightarrow \boxed{V_o \downarrow}$$

Eq. 1 Eq. 2 Eq. 1

The circuit reaches a stable equilibrium.



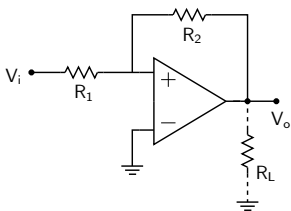
$$V_+ = V_o \frac{R_1}{R_1 + R_2} \quad (3)$$

$$V_i \uparrow \rightarrow \boxed{V_o \downarrow} \rightarrow V_+ \downarrow \rightarrow \boxed{V_o \downarrow}$$

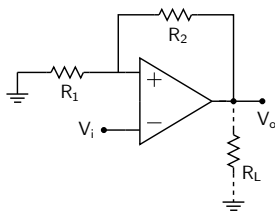
Eq. 1 Eq. 3 Eq. 1

We now have a positive feedback situation. As a result, V_o rises (or falls) indefinitely, limited finally by saturation.

Inverting amplifier with $+ \leftrightarrow -$

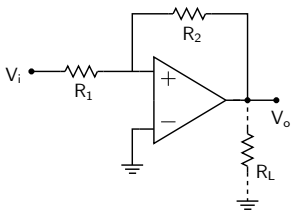


Noninverting amplifier with $+ \leftrightarrow -$

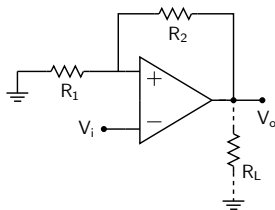


Feedback

Inverting amplifier with $+ \leftrightarrow -$



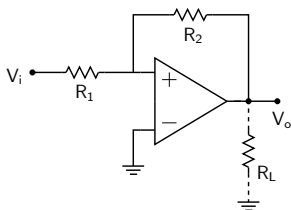
Noninverting amplifier with $+ \leftrightarrow -$



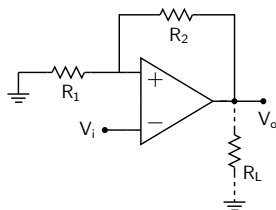
- * Because of positive feedback, both these circuits are unstable.

Feedback

Inverting amplifier with $+ \leftrightarrow -$

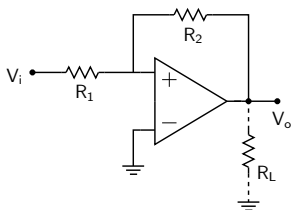


Noninverting amplifier with $+ \leftrightarrow -$

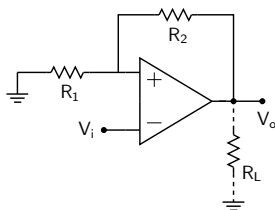


- * Because of positive feedback, both these circuits are unstable.
- * The output at any time is only limited by saturation of the Op Amp, i.e., $V_o = \pm V_{sat}$.

Inverting amplifier with $+ \leftrightarrow -$

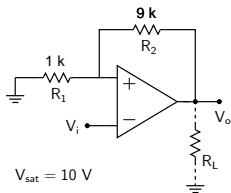


Noninverting amplifier with $+ \leftrightarrow -$



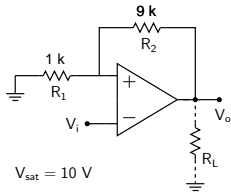
- * Because of positive feedback, both these circuits are unstable.
- * The output at any time is only limited by saturation of the Op Amp, i.e., $V_o = \pm V_{sat}$.
- * Of what use is a circuit that is stuck at $V_o = \pm V_{sat}$? It turns out that these circuits are actually useful! Let us see how.

Inverting Schmitt trigger



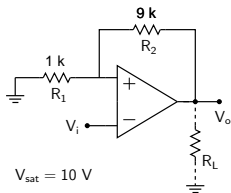
Because of positive feedback, V_o can only be $+V_{\text{sat}}$ (for $V_+ > V_-$) or $-V_{\text{sat}}$ (for $V_+ < V_-$).

Inverting Schmitt trigger



Because of positive feedback, V_o can only be $+V_{\text{sat}}$ (for $V_+ > V_-$) or $-V_{\text{sat}}$ (for $V_+ < V_-$).
Consider $V_i = 5\text{ V}$.

Inverting Schmitt trigger



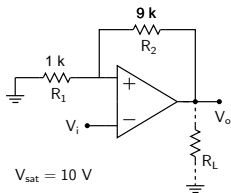
Because of positive feedback, V_o can only be $+V_{\text{sat}}$ (for $V_+ > V_-$) or $-V_{\text{sat}}$ (for $V_+ < V_-$).

Consider $V_i = 5 \text{ V}$.

Case (i): $V_o = +V_{\text{sat}} = +10 \text{ V} \rightarrow V_+ = \frac{R_1}{R_1 + R_2} V_o = 1 \text{ V}$.

$(V_+ - V_-) = (1 - 5) = -4 \text{ V} \rightarrow V_o = -V_{\text{sat}}$.

Inverting Schmitt trigger



Because of positive feedback, V_o can only be $+V_{\text{sat}}$ (for $V_+ > V_-$) or $-V_{\text{sat}}$ (for $V_+ < V_-$).

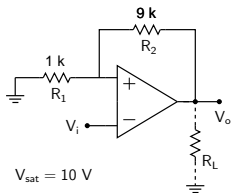
Consider $V_i = 5 \text{ V}$.

$$\text{Case (i): } V_o = +V_{\text{sat}} = +10 \text{ V} \rightarrow V_+ = \frac{R_1}{R_1 + R_2} V_o = 1 \text{ V}.$$

$$(V_+ - V_-) = (1 - 5) = -4 \text{ V} \rightarrow V_o = -V_{\text{sat}}.$$

This is inconsistent with our assumption ($V_o = +V_{\text{sat}}$).

Inverting Schmitt trigger



Because of positive feedback, V_o can only be $+V_{\text{sat}}$ (for $V_+ > V_-$) or $-V_{\text{sat}}$ (for $V_+ < V_-$).
Consider $V_i = 5 \text{ V}$.

$$\text{Case (i): } V_o = +V_{\text{sat}} = +10 \text{ V} \rightarrow V_+ = \frac{R_1}{R_1 + R_2} V_o = 1 \text{ V}.$$

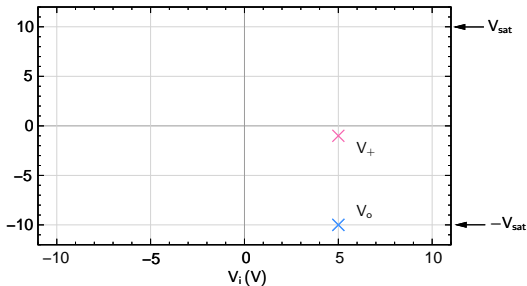
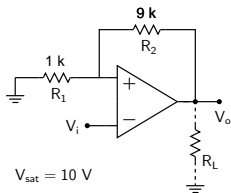
$$(V_+ - V_-) = (1 - 5) = -4 \text{ V} \rightarrow V_o = -V_{\text{sat}}.$$

This is inconsistent with our assumption ($V_o = +V_{\text{sat}}$).

$$\text{Case (ii): } V_o = -V_{\text{sat}} = -10 \text{ V} \rightarrow V_+ = \frac{R_1}{R_1 + R_2} V_o = -1 \text{ V}.$$

$$(V_+ - V_-) = (-1 - 5) = -6 \text{ V} \rightarrow V_o = -V_{\text{sat}} \text{ (consistent)}$$

Inverting Schmitt trigger



Because of positive feedback, V_o can only be $+V_{\text{sat}}$ (for $V_+ > V_-$) or $-V_{\text{sat}}$ (for $V_+ < V_-$).

Consider $V_i = 5 \text{ V}$.

$$\text{Case (i): } V_o = +V_{\text{sat}} = +10 \text{ V} \rightarrow V_+ = \frac{R_1}{R_1 + R_2} V_o = 1 \text{ V}.$$

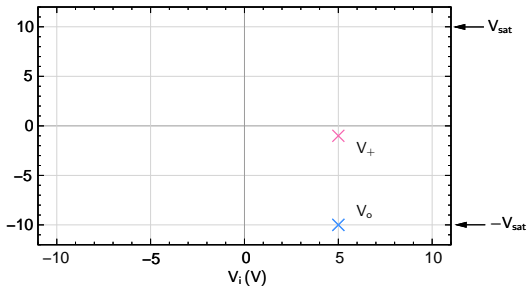
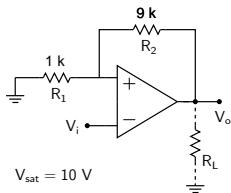
$$(V_+ - V_-) = (1 - 5) = -4 \text{ V} \rightarrow V_o = -V_{\text{sat}}.$$

This is inconsistent with our assumption ($V_o = +V_{\text{sat}}$).

$$\text{Case (ii): } V_o = -V_{\text{sat}} = -10 \text{ V} \rightarrow V_+ = \frac{R_1}{R_1 + R_2} V_o = -1 \text{ V}.$$

$$(V_+ - V_-) = (-1 - 5) = -6 \text{ V} \rightarrow V_o = -V_{\text{sat}} \text{ (consistent)}$$

Inverting Schmitt trigger



Because of positive feedback, V_o can only be $+V_{sat}$ (for $V_+ > V_-$) or $-V_{sat}$ (for $V_+ < V_-$). Consider $V_i = 5 \text{ V}$.

$$\text{Case (i): } V_o = +V_{sat} = +10 \text{ V} \rightarrow V_+ = \frac{R_1}{R_1 + R_2} V_o = 1 \text{ V}.$$

$$(V_+ - V_-) = (1 - 5) = -4 \text{ V} \rightarrow V_o = -V_{sat}.$$

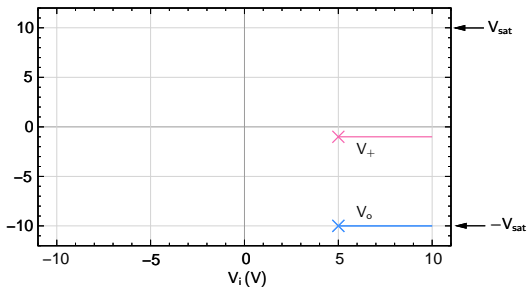
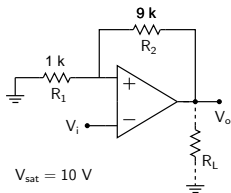
This is inconsistent with our assumption ($V_o = +V_{sat}$).

$$\text{Case (ii): } V_o = -V_{sat} = -10 \text{ V} \rightarrow V_+ = \frac{R_1}{R_1 + R_2} V_o = -1 \text{ V}.$$

$$(V_+ - V_-) = (-1 - 5) = -6 \text{ V} \rightarrow V_o = -V_{sat} \text{ (consistent)}$$

If we move to the right (increasing V_i), the same situation applies, i.e., $V_o = -V_{sat}$.

Inverting Schmitt trigger



Because of positive feedback, V_o can only be $+V_{sat}$ (for $V_+ > V_-$) or $-V_{sat}$ (for $V_+ < V_-$).

Consider $V_i = 5 \text{ V}$.

$$\text{Case (i): } V_o = +V_{sat} = +10 \text{ V} \rightarrow V_+ = \frac{R_1}{R_1 + R_2} V_o = 1 \text{ V}.$$

$$(V_+ - V_-) = (1 - 5) = -4 \text{ V} \rightarrow V_o = -V_{sat}.$$

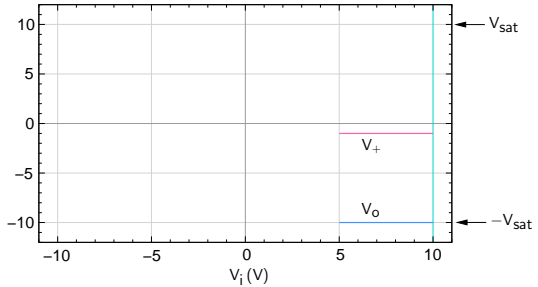
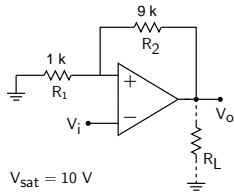
This is inconsistent with our assumption ($V_o = +V_{sat}$).

$$\text{Case (ii): } V_o = -V_{sat} = -10 \text{ V} \rightarrow V_+ = \frac{R_1}{R_1 + R_2} V_o = -1 \text{ V}.$$

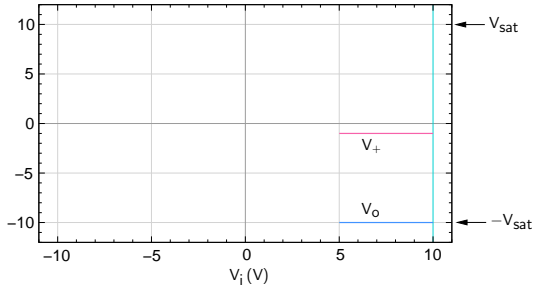
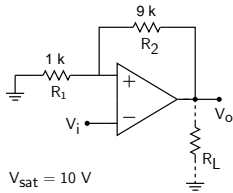
$$(V_+ - V_-) = (-1 - 5) = -6 \text{ V} \rightarrow V_o = -V_{sat} \text{ (consistent)}$$

If we move to the right (increasing V_i), the same situation applies, i.e., $V_o = -V_{sat}$.

Inverting Schmitt trigger

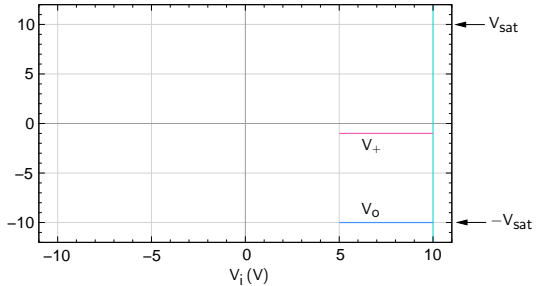
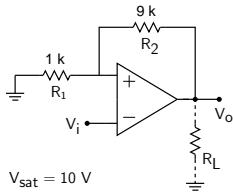


Inverting Schmitt trigger



Consider decreasing values of V_i .

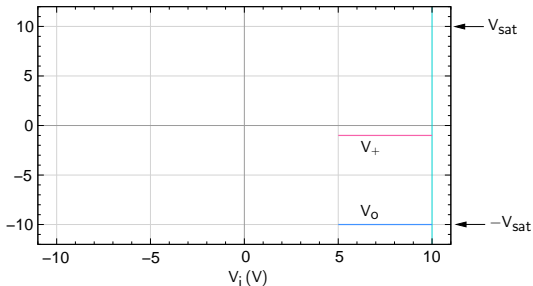
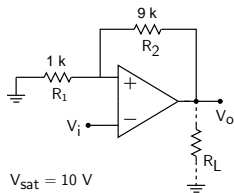
Inverting Schmitt trigger



Consider decreasing values of V_i .

$$V_+ = \frac{R_1}{R_1 + R_2} V_o = \frac{1 \text{ k}}{10 \text{ k}} (-V_{\text{sat}}) = -1 \text{ V}.$$

Inverting Schmitt trigger

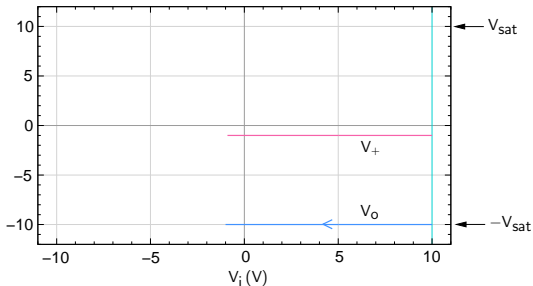
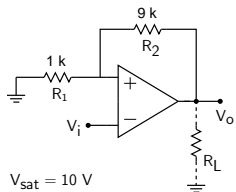


Consider decreasing values of V_i .

$$V_+ = \frac{R_1}{R_1 + R_2} V_o = \frac{1 \text{ k}}{10 \text{ k}} (-V_{\text{sat}}) = -1 \text{ V}.$$

As long as $V_i = V_- > V_+ = -1 \text{ V}$, V_o remains at $-V_{\text{sat}}$.

Inverting Schmitt trigger

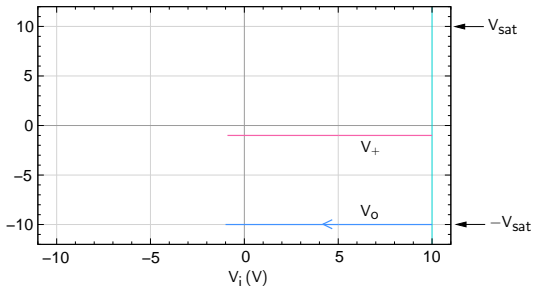
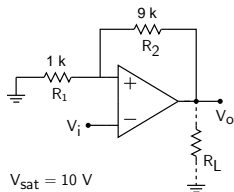


Consider decreasing values of V_i .

$$V_+ = \frac{R_1}{R_1 + R_2} V_o = \frac{1 \text{ k}}{10 \text{ k}} (-V_{\text{sat}}) = -1 \text{ V}.$$

As long as $V_i = V_- > V_+ = -1 \text{ V}$, V_o remains at $-V_{\text{sat}}$.

Inverting Schmitt trigger



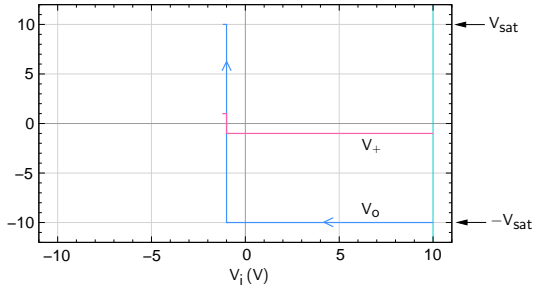
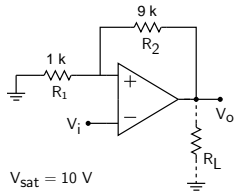
Consider decreasing values of V_i .

$$V_+ = \frac{R_1}{R_1 + R_2} V_o = \frac{1 \text{ k}}{10 \text{ k}} (-V_{\text{sat}}) = -1 \text{ V}.$$

As long as $V_i = V_- > V_+ = -1 \text{ V}$, V_o remains at $-V_{\text{sat}}$.

When $V_i < V_+ = -1 \text{ V}$, V_o changes sign, i.e., $V_o = +V_{\text{sat}}$.

Inverting Schmitt trigger



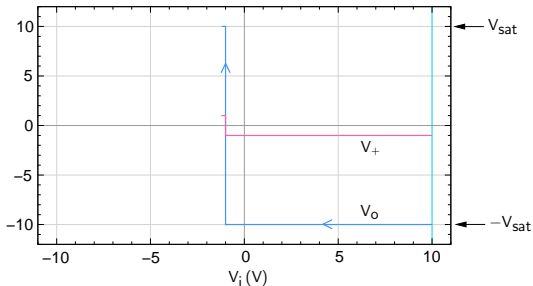
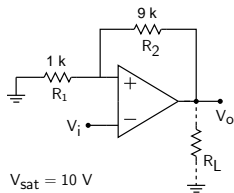
Consider decreasing values of V_i .

$$V_+ = \frac{R_1}{R_1 + R_2} V_o = \frac{1 \text{ k}}{10 \text{ k}} (-V_{\text{sat}}) = -1 \text{ V}.$$

As long as $V_i = V_- > V_+ = -1 \text{ V}$, V_o remains at $-V_{\text{sat}}$.

When $V_i < V_+ = -1 \text{ V}$, V_o changes sign, i.e., $V_o = +V_{\text{sat}}$.

Inverting Schmitt trigger



Consider decreasing values of V_i .

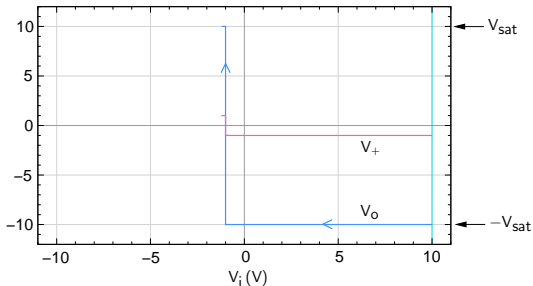
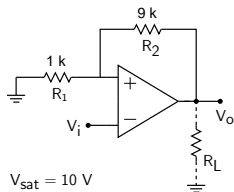
$$V_+ = \frac{R_1}{R_1 + R_2} V_o = \frac{1 \text{ k}}{10 \text{ k}} (-V_{\text{sat}}) = -1 \text{ V}.$$

As long as $V_i = V_- > V_+ = -1 \text{ V}$, V_o remains at $-V_{\text{sat}}$.

When $V_i < V_+ = -1 \text{ V}$, V_o changes sign, i.e., $V_o = +V_{\text{sat}}$.

$$V_+ \text{ now becomes } \frac{R_1}{R_1 + R_2} (+V_{\text{sat}}) = +1 \text{ V}.$$

Inverting Schmitt trigger



Consider decreasing values of V_i .

$$V_+ = \frac{R_1}{R_1 + R_2} V_o = \frac{1 \text{ k}}{10 \text{ k}} (-V_{\text{sat}}) = -1 \text{ V}.$$

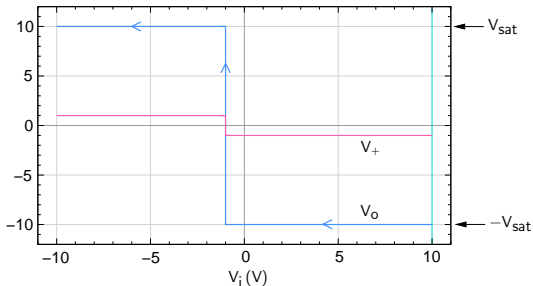
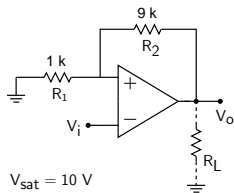
As long as $V_i = V_- > V_+ = -1 \text{ V}$, V_o remains at $-V_{\text{sat}}$.

When $V_i < V_+ = -1 \text{ V}$, V_o changes sign, i.e., $V_o = +V_{\text{sat}}$.

$$V_+ \text{ now becomes } \frac{R_1}{R_1 + R_2} (+V_{\text{sat}}) = +1 \text{ V}.$$

Decreasing V_i further makes no difference to V_o (since $V_i = V_- < V_+ = +1 \text{ V}$ holds).

Inverting Schmitt trigger



Consider decreasing values of V_i .

$$V_+ = \frac{R_1}{R_1 + R_2} V_o = \frac{1 \text{ k}}{10 \text{ k}} (-V_{\text{sat}}) = -1 \text{ V}.$$

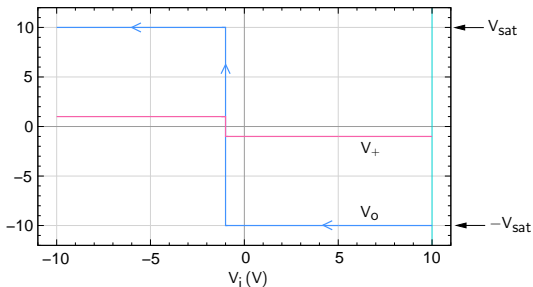
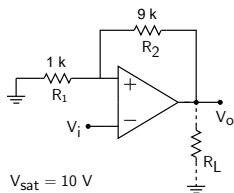
As long as $V_i = V_- > V_+ = -1 \text{ V}$, V_o remains at $-V_{\text{sat}}$.

When $V_i < V_+ = -1 \text{ V}$, V_o changes sign, i.e., $V_o = +V_{\text{sat}}$.

$$V_+ \text{ now becomes } \frac{R_1}{R_1 + R_2} (+V_{\text{sat}}) = +1 \text{ V}.$$

Decreasing V_i further makes no difference to V_o (since $V_i = V_- < V_+ = +1 \text{ V}$ holds).

Inverting Schmitt trigger



Consider decreasing values of V_i .

$$V_+ = \frac{R_1}{R_1 + R_2} V_o = \frac{1 \text{ k}}{10 \text{ k}} (-V_{\text{sat}}) = -1 \text{ V}.$$

As long as $V_i = V_- > V_+ = -1 \text{ V}$, V_o remains at $-V_{\text{sat}}$.

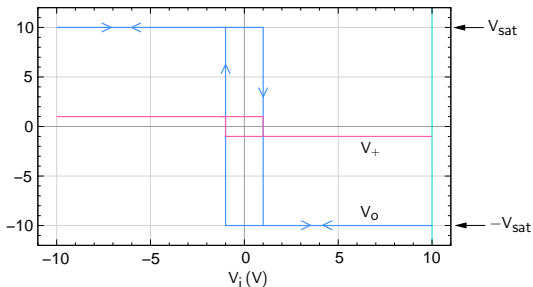
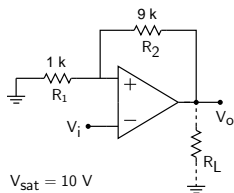
When $V_i < V_+ = -1 \text{ V}$, V_o changes sign, i.e., $V_o = +V_{\text{sat}}$.

$$V_+ \text{ now becomes } \frac{R_1}{R_1 + R_2} (+V_{\text{sat}}) = +1 \text{ V}.$$

Decreasing V_i further makes no difference to V_o (since $V_i = V_- < V_+ = +1 \text{ V}$ holds).

Now, the threshold at which V_o flips is $V_i = +1 \text{ V}$.

Inverting Schmitt trigger



Consider decreasing values of V_i .

$$V_+ = \frac{R_1}{R_1 + R_2} V_o = \frac{1 \text{ k}}{10 \text{ k}} (-V_{\text{sat}}) = -1 \text{ V}.$$

As long as $V_i = V_- > V_+ = -1 \text{ V}$, V_o remains at $-V_{\text{sat}}$.

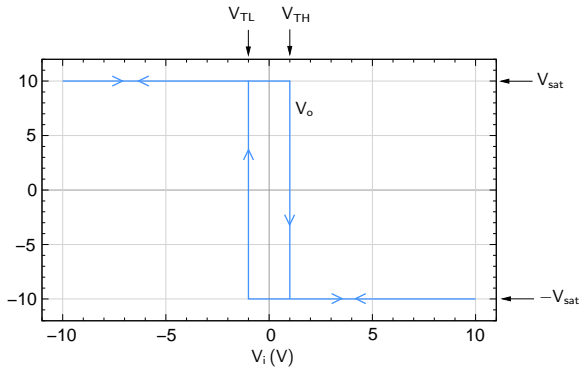
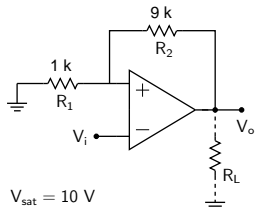
When $V_i < V_+ = -1 \text{ V}$, V_o changes sign, i.e., $V_o = +V_{\text{sat}}$.

$$V_+ \text{ now becomes } \frac{R_1}{R_1 + R_2} (+V_{\text{sat}}) = +1 \text{ V}.$$

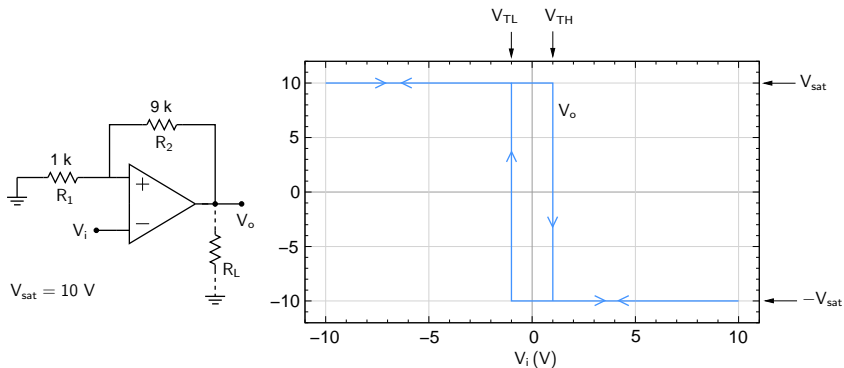
Decreasing V_i further makes no difference to V_o (since $V_i = V_- < V_+ = +1 \text{ V}$ holds).

Now, the threshold at which V_o flips is $V_i = +1 \text{ V}$.

Inverting Schmitt trigger



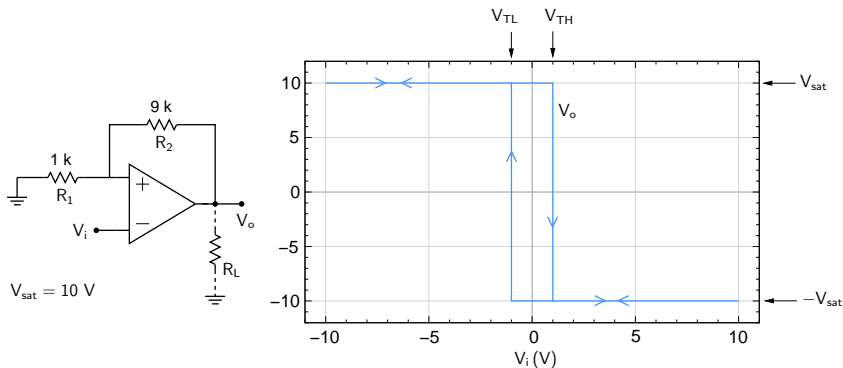
Inverting Schmitt trigger



- * The threshold values (or “tripping points”), V_{TH} and V_{TL} , are given by

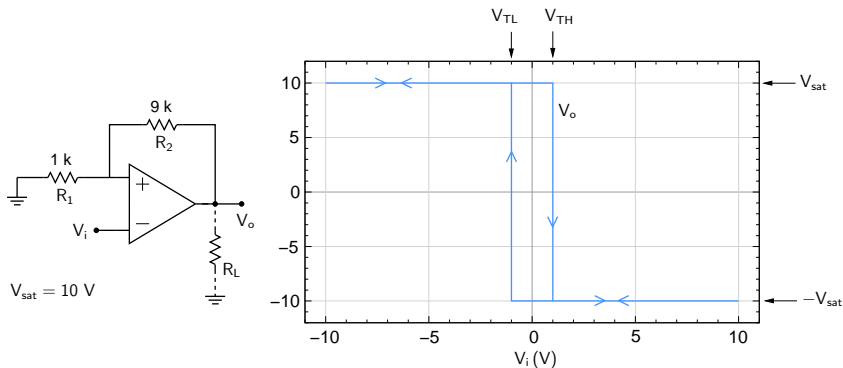
$$\pm \left(\frac{R_1}{R_1 + R_2} \right) V_{\text{sat}}$$

Inverting Schmitt trigger



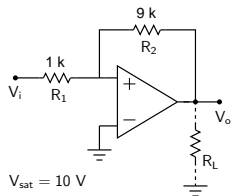
- * The threshold values (or “tripping points”), V_{TH} and V_{TL} , are given by
$$\pm \left(\frac{R_1}{R_1 + R_2} \right) V_{\text{sat}}.$$
- * The tripping point (whether V_{TH} or V_{TL}) depends on where we are on the V_o axis. In that sense, the circuit has a memory.

Inverting Schmitt trigger



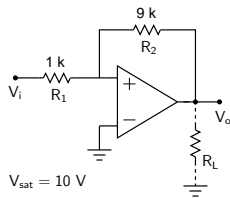
- * The threshold values (or “tripping points”), V_{TH} and V_{TL} , are given by
$$\pm \left(\frac{R_1}{R_1 + R_2} \right) V_{\text{sat}}.$$
- * The tripping point (whether V_{TH} or V_{TL}) depends on where we are on the V_o axis. In that sense, the circuit has a memory.
- * $\Delta V_T = V_{\text{TH}} - V_{\text{TL}}$ is called the “hysteresis width.”

Noninverting Schmitt trigger



Because of positive feedback, V_o can only be $+V_{\text{sat}}$ (for $V_+ > V_-$) or $-V_{\text{sat}}$ (for $V_+ < V_-$).

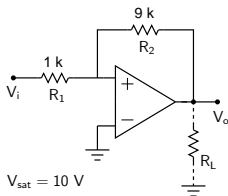
Noninverting Schmitt trigger



Because of positive feedback, V_o can only be $+V_{\text{sat}}$ (for $V_+ > V_-$) or $-V_{\text{sat}}$ (for $V_+ < V_-$).

Consider $V_i = 5 \text{ V}$.

Noninverting Schmitt trigger



Because of positive feedback, V_o can only be $+V_{\text{sat}}$ (for $V_+ > V_-$) or $-V_{\text{sat}}$ (for $V_+ < V_-$).

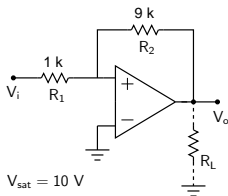
Consider $V_i = 5 \text{ V}$.

Case (i): $V_o = -V_{\text{sat}} = -10 \text{ V}$

$$\rightarrow V_+ = \frac{R_2}{R_1 + R_2} V_i + \frac{R_1}{R_1 + R_2} V_o = \frac{9 \text{ k}}{10 \text{ k}} \times 5 + \frac{1 \text{ k}}{10 \text{ k}} \times (-10) = 3.5 \text{ V}.$$

$$(V_+ - V_-) = (3.5 - 0) = 3.5 \text{ V} \rightarrow V_o = +V_{\text{sat}}.$$

Noninverting Schmitt trigger



Because of positive feedback, V_o can only be $+V_{\text{sat}}$ (for $V_+ > V_-$) or $-V_{\text{sat}}$ (for $V_+ < V_-$).

Consider $V_i = 5 \text{ V}$.

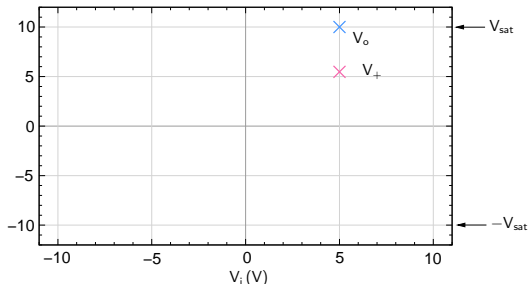
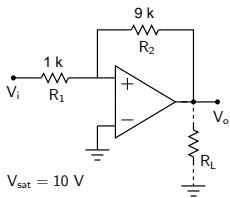
Case (i): $V_o = -V_{\text{sat}} = -10 \text{ V}$

$$\rightarrow V_+ = \frac{R_2}{R_1 + R_2} V_i + \frac{R_1}{R_1 + R_2} V_o = \frac{9 \text{ k}}{10 \text{ k}} \times 5 + \frac{1 \text{ k}}{10 \text{ k}} \times (-10) = 3.5 \text{ V}.$$

$$(V_+ - V_-) = (3.5 - 0) = 3.5 \text{ V} \rightarrow V_o = +V_{\text{sat}}.$$

This is inconsistent with our assumption ($V_o = -V_{\text{sat}}$).

Noninverting Schmitt trigger



Because of positive feedback, V_o can only be $+V_{sat}$ (for $V_+ > V_-$) or $-V_{sat}$ (for $V_+ < V_-$).

Consider $V_i = 5 V$.

Case (i): $V_o = -V_{sat} = -10 V$

$$\rightarrow V_+ = \frac{R_2}{R_1 + R_2} V_i + \frac{R_1}{R_1 + R_2} V_o = \frac{9 \text{ k}}{10 \text{ k}} \times 5 + \frac{1 \text{ k}}{10 \text{ k}} \times (-10) = 3.5 V.$$

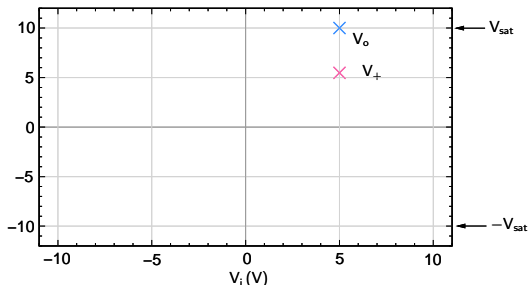
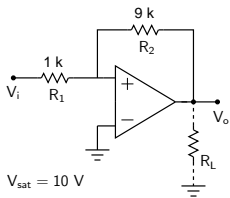
$$(V_+ - V_-) = (3.5 - 0) = 3.5 V \rightarrow V_o = +V_{sat}.$$

This is inconsistent with our assumption ($V_o = -V_{sat}$).

$$\text{Case (ii): } V_o = \frac{9 \text{ k}}{10 \text{ k}} \times 5 + \frac{1 \text{ k}}{10 \text{ k}} \times 10 = 5.5 V.$$

$$(V_+ - V_-) = (5.5 - 0) = 5.5 V \rightarrow V_o = +V_{sat} \text{ (consistent)}$$

Noninverting Schmitt trigger



Because of positive feedback, V_o can only be $+V_{\text{sat}}$ (for $V_+ > V_-$) or $-V_{\text{sat}}$ (for $V_+ < V_-$).

Consider $V_i = 5 \text{ V}$.

Case (i): $V_o = -V_{\text{sat}} = -10 \text{ V}$

$$\rightarrow V_+ = \frac{R_2}{R_1 + R_2} V_i + \frac{R_1}{R_1 + R_2} V_o = \frac{9 \text{ k}}{10 \text{ k}} \times 5 + \frac{1 \text{ k}}{10 \text{ k}} \times (-10) = 3.5 \text{ V}.$$

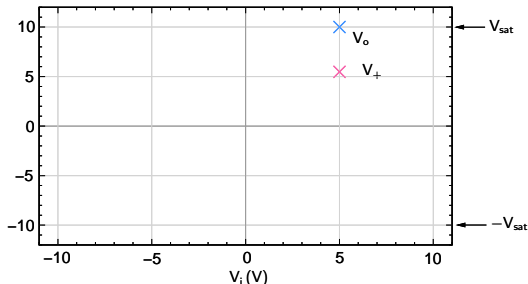
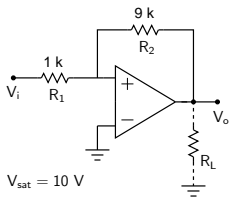
$$(V_+ - V_-) = (3.5 - 0) = 3.5 \text{ V} \rightarrow V_o = +V_{\text{sat}}.$$

This is inconsistent with our assumption ($V_o = -V_{\text{sat}}$).

Case (ii): $V_o = \frac{9 \text{ k}}{10 \text{ k}} \times 5 + \frac{1 \text{ k}}{10 \text{ k}} \times 10 = 5.5 \text{ V}.$

$$(V_+ - V_-) = (5.5 - 0) = 5.5 \text{ V} \rightarrow V_o = +V_{\text{sat}} \text{ (consistent)}$$

Noninverting Schmitt trigger



Because of positive feedback, V_o can only be $+V_{\text{sat}}$ (for $V_+ > V_-$) or $-V_{\text{sat}}$ (for $V_+ < V_-$).
Consider $V_i = 5 \text{ V}$.

Case (i): $V_o = -V_{\text{sat}} = -10 \text{ V}$

$$\rightarrow V_+ = \frac{R_2}{R_1 + R_2} V_i + \frac{R_1}{R_1 + R_2} V_o = \frac{9 \text{ k}}{10 \text{ k}} \times 5 + \frac{1 \text{ k}}{10 \text{ k}} \times (-10) = 3.5 \text{ V}.$$

$$(V_+ - V_-) = (3.5 - 0) = 3.5 \text{ V} \rightarrow V_o = +V_{\text{sat}}.$$

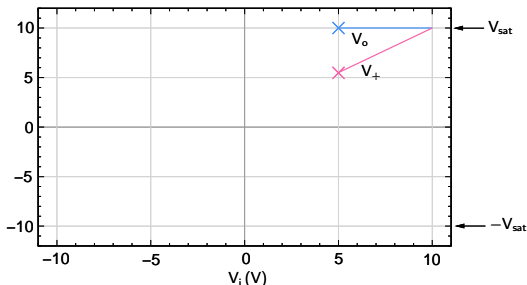
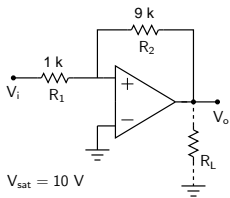
This is inconsistent with our assumption ($V_o = -V_{\text{sat}}$).

Case (ii): $V_o = \frac{9 \text{ k}}{10 \text{ k}} \times 5 + \frac{1 \text{ k}}{10 \text{ k}} \times 10 = 5.5 \text{ V}.$

$$(V_+ - V_-) = (5.5 - 0) = 5.5 \text{ V} \rightarrow V_o = +V_{\text{sat}} \text{ (consistent)}$$

If we move to the right (increasing V_i), the same situation applies, i.e., $V_o = +V_{\text{sat}}$.

Noninverting Schmitt trigger



Because of positive feedback, V_o can only be $+V_{sat}$ (for $V_+ > V_-$) or $-V_{sat}$ (for $V_+ < V_-$).

Consider $V_i = 5 V$.

Case (i): $V_o = -V_{sat} = -10 V$

$$\rightarrow V_+ = \frac{R_2}{R_1 + R_2} V_i + \frac{R_1}{R_1 + R_2} V_o = \frac{9 k}{10 k} \times 5 + \frac{1 k}{10 k} \times (-10) = 3.5 V.$$

$$(V_+ - V_-) = (3.5 - 0) = 3.5 V \rightarrow V_o = +V_{sat}.$$

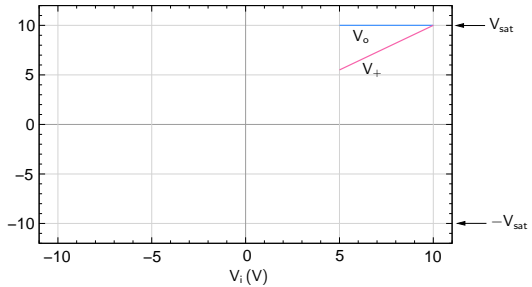
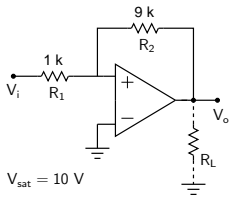
This is inconsistent with our assumption ($V_o = -V_{sat}$).

$$\text{Case (ii): } V_o = \frac{9 k}{10 k} \times 5 + \frac{1 k}{10 k} \times 10 = 5.5 V.$$

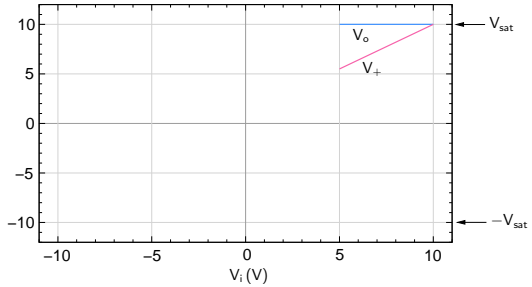
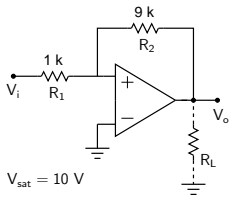
$$(V_+ - V_-) = (5.5 - 0) = 5.5 V \rightarrow V_o = +V_{sat} \text{ (consistent)}$$

If we move to the right (increasing V_i), the same situation applies, i.e., $V_o = +V_{sat}$.

Noninverting Schmitt trigger

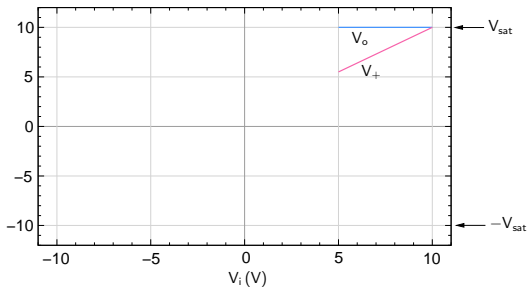
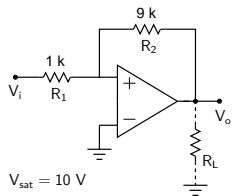


Noninverting Schmitt trigger



Consider decreasing values of V_i .

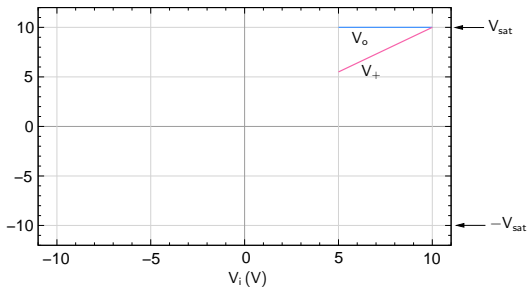
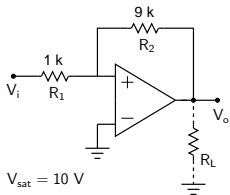
Noninverting Schmitt trigger



Consider decreasing values of V_i .

$$V_{+} = \frac{R_2}{R_1 + R_2} V_i + \frac{R_1}{R_1 + R_2} V_{\text{o}} = \frac{9 \text{ k}}{10 \text{ k}} V_i + \frac{1 \text{ k}}{10 \text{ k}} V_{\text{o}} .$$

Noninverting Schmitt trigger

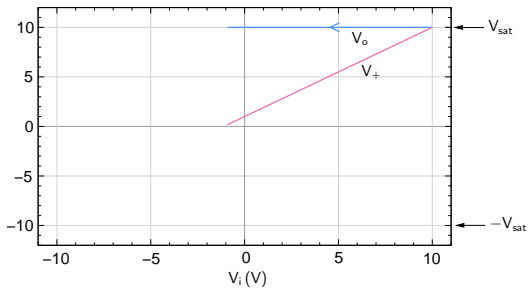
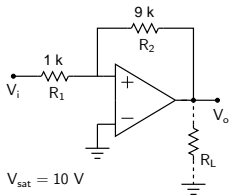


Consider decreasing values of V_i .

$$V_{+} = \frac{R_2}{R_1 + R_2} V_i + \frac{R_1}{R_1 + R_2} V_{\text{o}} = \frac{9 \text{ k}}{10 \text{ k}} V_i + \frac{1 \text{ k}}{10 \text{ k}} V_{\text{o}} .$$

As long as $V_{+} > 0 \text{ V}$, V_{o} remains at $+V_{\text{sat}}$.

Noninverting Schmitt trigger

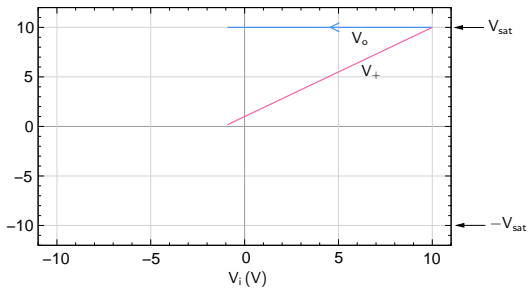
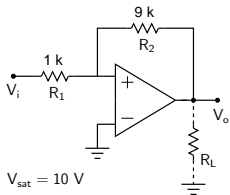


Consider decreasing values of V_i .

$$V_{+} = \frac{R_2}{R_1 + R_2} V_i + \frac{R_1}{R_1 + R_2} V_{\text{o}} = \frac{9 \text{ k}}{10 \text{ k}} V_i + \frac{1 \text{ k}}{10 \text{ k}} V_{\text{o}} .$$

As long as $V_{+} > 0 \text{ V}$, V_{o} remains at $+V_{\text{sat}}$.

Noninverting Schmitt trigger



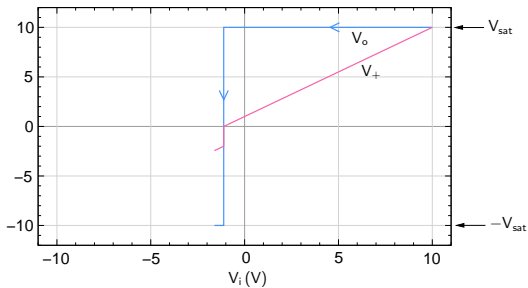
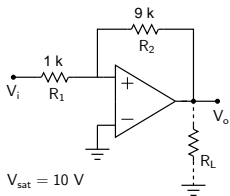
Consider decreasing values of V_i .

$$V_+ = \frac{R_2}{R_1 + R_2} V_i + \frac{R_1}{R_1 + R_2} V_o = \frac{9 \text{ k}}{10 \text{ k}} V_i + \frac{1 \text{ k}}{10 \text{ k}} V_o.$$

As long as $V_+ > 0 \text{ V}$, V_o remains at $+V_{\text{sat}}$.

When $V_+ = 0 \text{ V}$, i.e., $V_i = -\frac{R_1}{R_2} V_{\text{sat}} = -1.11 \text{ V}$, V_o changes sign, i.e., $V_o = -V_{\text{sat}}$.

Noninverting Schmitt trigger



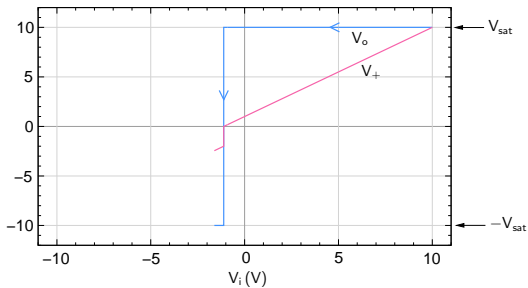
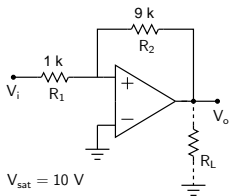
Consider decreasing values of V_i .

$$V_+ = \frac{R_2}{R_1 + R_2} V_i + \frac{R_1}{R_1 + R_2} V_o = \frac{9 \text{ k}}{10 \text{ k}} V_i + \frac{1 \text{ k}}{10 \text{ k}} V_o.$$

As long as $V_+ > 0 \text{ V}$, V_o remains at $+V_{\text{sat}}$.

When $V_+ = 0 \text{ V}$, i.e., $V_i = -\frac{R_1}{R_2} V_{\text{sat}} = -1.11 \text{ V}$, V_o changes sign, i.e., $V_o = -V_{\text{sat}}$.

Noninverting Schmitt trigger



Consider decreasing values of V_i .

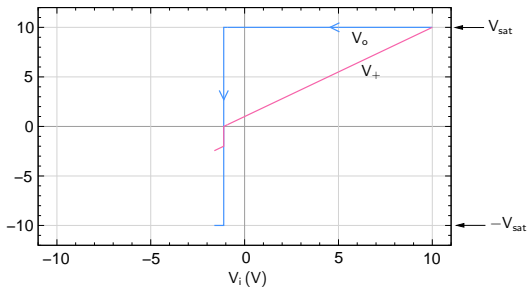
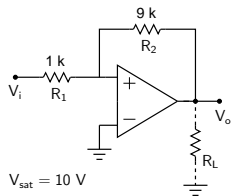
$$V_+ = \frac{R_2}{R_1 + R_2} V_i + \frac{R_1}{R_1 + R_2} V_o = \frac{9 \text{ k}}{10 \text{ k}} V_i + \frac{1 \text{ k}}{10 \text{ k}} V_o.$$

As long as $V_+ > 0 \text{ V}$, V_o remains at $+V_{\text{sat}}$.

When $V_+ = 0 \text{ V}$, i.e., $V_i = -\frac{R_1}{R_2} V_{\text{sat}} = -1.11 \text{ V}$, V_o changes sign, i.e., $V_o = -V_{\text{sat}}$.

V_+ now follows the equation, $V_+ = \frac{9 \text{ k}}{10 \text{ k}} V_i - \frac{1 \text{ k}}{10 \text{ k}} V_{\text{sat}}$.

Noninverting Schmitt trigger



Consider decreasing values of V_i .

$$V_+ = \frac{R_2}{R_1 + R_2} V_i + \frac{R_1}{R_1 + R_2} V_o = \frac{9 \text{ k}}{10 \text{ k}} V_i + \frac{1 \text{ k}}{10 \text{ k}} V_o.$$

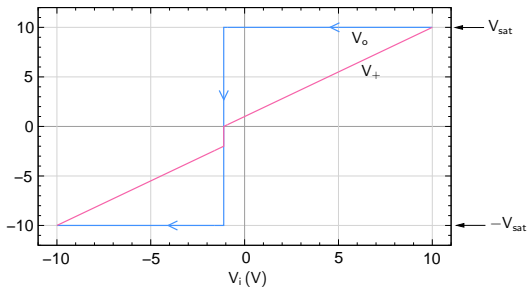
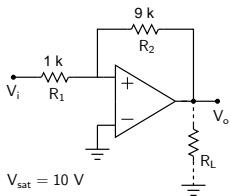
As long as $V_+ > 0 \text{ V}$, V_o remains at $+V_{\text{sat}}$.

When $V_+ = 0 \text{ V}$, i.e., $V_i = -\frac{R_1}{R_2} V_{\text{sat}} = -1.11 \text{ V}$, V_o changes sign, i.e., $V_o = -V_{\text{sat}}$.

V_+ now follows the equation, $V_+ = \frac{9 \text{ k}}{10 \text{ k}} V_i - \frac{1 \text{ k}}{10 \text{ k}} V_{\text{sat}}$.

Decreasing V_i further makes no difference to V_o (since V_+ remains negative).

Noninverting Schmitt trigger



Consider decreasing values of V_i .

$$V_+ = \frac{R_2}{R_1 + R_2} V_i + \frac{R_1}{R_1 + R_2} V_o = \frac{9\text{ k}}{10\text{ k}} V_i + \frac{1\text{ k}}{10\text{ k}} V_o.$$

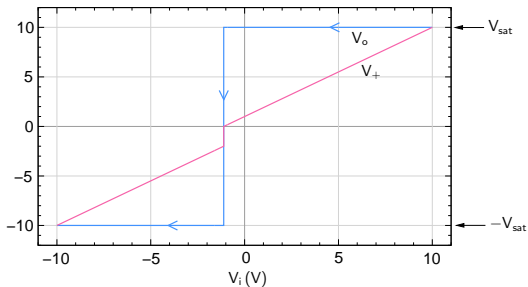
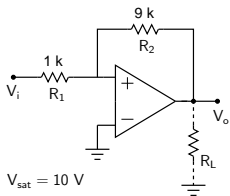
As long as $V_+ > 0\text{ V}$, V_o remains at $+V_{\text{sat}}$.

When $V_+ = 0\text{ V}$, i.e., $V_i = -\frac{R_1}{R_2} V_{\text{sat}} = -1.11\text{ V}$, V_o changes sign, i.e., $V_o = -V_{\text{sat}}$.

V_+ now follows the equation, $V_+ = \frac{9\text{ k}}{10\text{ k}} V_i - \frac{1\text{ k}}{10\text{ k}} V_{\text{sat}}$.

Decreasing V_i further makes no difference to V_o (since V_+ remains negative).

Noninverting Schmitt trigger



Consider decreasing values of V_i .

$$V_+ = \frac{R_2}{R_1 + R_2} V_i + \frac{R_1}{R_1 + R_2} V_o = \frac{9 \text{ k}}{10 \text{ k}} V_i + \frac{1 \text{ k}}{10 \text{ k}} V_o.$$

As long as $V_+ > 0 \text{ V}$, V_o remains at $+V_{\text{sat}}$.

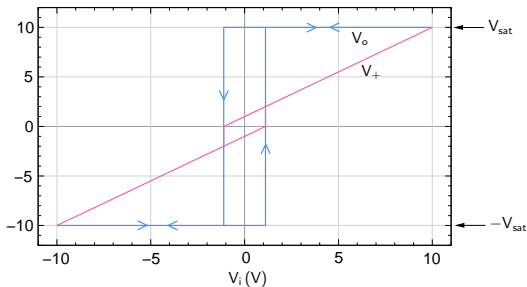
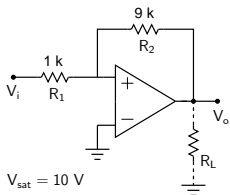
When $V_+ = 0 \text{ V}$, i.e., $V_i = -\frac{R_1}{R_2} V_{\text{sat}} = -1.11 \text{ V}$, V_o changes sign, i.e., $V_o = -V_{\text{sat}}$.

V_+ now follows the equation, $V_+ = \frac{9 \text{ k}}{10 \text{ k}} V_i - \frac{1 \text{ k}}{10 \text{ k}} V_{\text{sat}}$.

Decreasing V_i further makes no difference to V_o (since V_+ remains negative).

Now, the threshold at which V_o flips is $V_+ = 0$, i.e., $V_i = +\frac{R_1}{R_2} V_{\text{sat}} = +1.11 \text{ V}$

Noninverting Schmitt trigger



Consider decreasing values of V_i .

$$V_+ = \frac{R_2}{R_1 + R_2} V_i + \frac{R_1}{R_1 + R_2} V_o = \frac{9 \text{ k}}{10 \text{ k}} V_i + \frac{1 \text{ k}}{10 \text{ k}} V_o.$$

As long as $V_+ > 0 \text{ V}$, V_o remains at $+V_{\text{sat}}$.

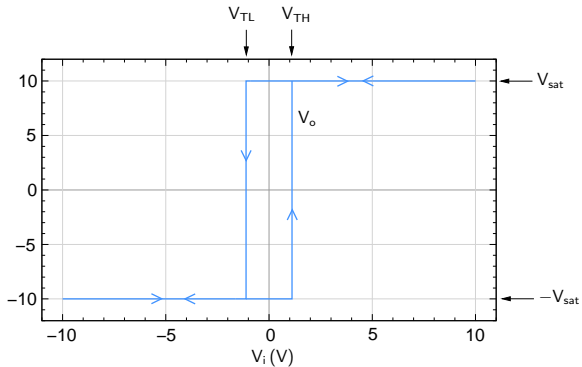
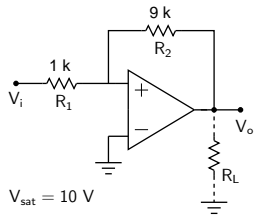
When $V_+ = 0 \text{ V}$, i.e., $V_i = -\frac{R_1}{R_2} V_{\text{sat}} = -1.11 \text{ V}$, V_o changes sign, i.e., $V_o = -V_{\text{sat}}$.

V_+ now follows the equation, $V_+ = \frac{9 \text{ k}}{10 \text{ k}} V_i - \frac{1 \text{ k}}{10 \text{ k}} V_{\text{sat}}$.

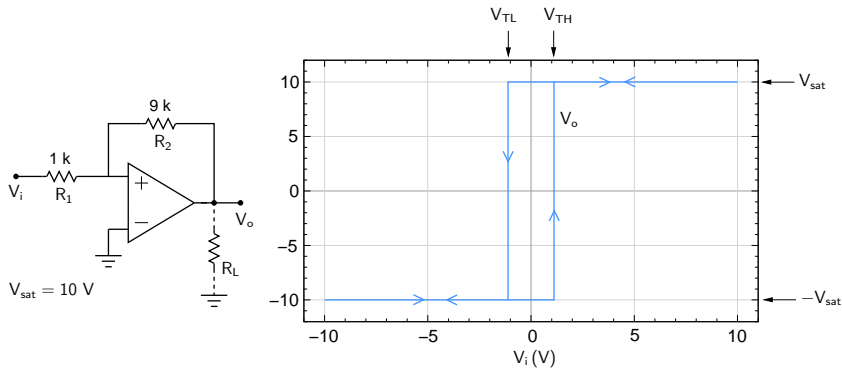
Decreasing V_i further makes no difference to V_o (since V_+ remains negative).

Now, the threshold at which V_o flips is $V_+ = 0$, i.e., $V_i = +\frac{R_1}{R_2} V_{\text{sat}} = +1.11 \text{ V}$

Noninverting Schmitt trigger

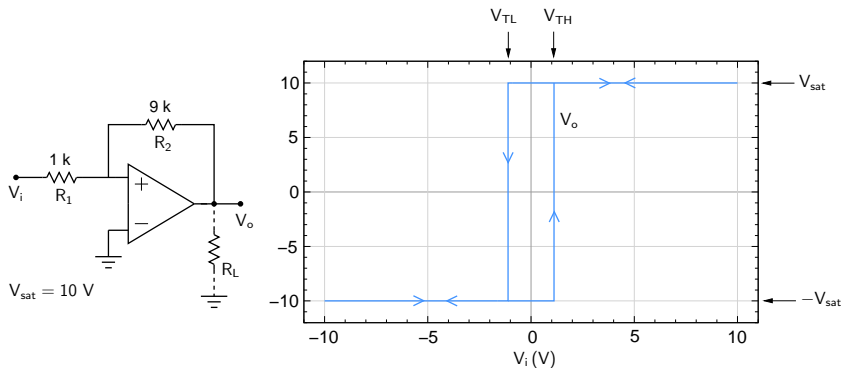


Noninverting Schmitt trigger



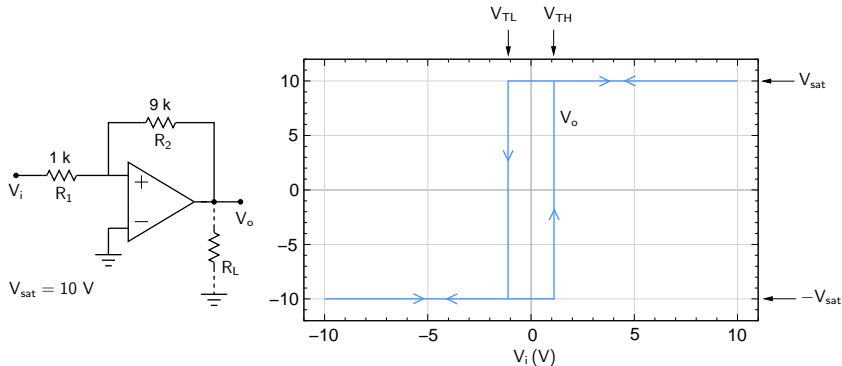
* The threshold values V_{TH} and V_{TL} are given by $\pm \left(\frac{R_1}{R_2} \right) V_{sat}$.

Noninverting Schmitt trigger



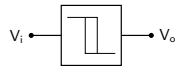
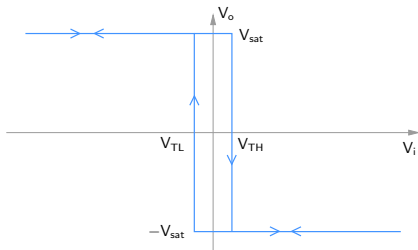
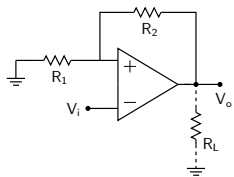
- * The threshold values V_{TH} and V_{TL} are given by $\pm \left(\frac{R_1}{R_2} \right) V_{\text{sat}}$.
- * As in the inverting Schmitt trigger, this circuit has a memory, i.e., the tripping point (whether V_{TH} or V_{TL}) depends on where we are on the V_o axis.

Noninverting Schmitt trigger

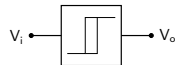
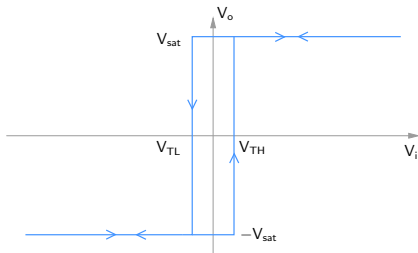
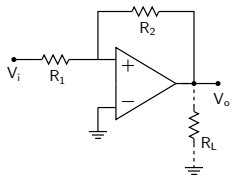


- * The threshold values V_{TH} and V_{TL} are given by $\pm \left(\frac{R_1}{R_2} \right) V_{sat}$.
- * As in the inverting Schmitt trigger, this circuit has a memory, i.e., the tripping point (whether V_{TH} or V_{TL}) depends on where we are on the V_o axis.
- * $\Delta V_T = V_{TH} - V_{TL}$ is called the “hysteresis width.”

Schmitt triggers

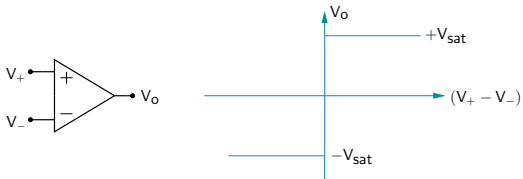


Inverting

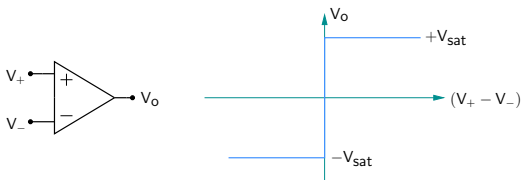


Noninverting

Comparators

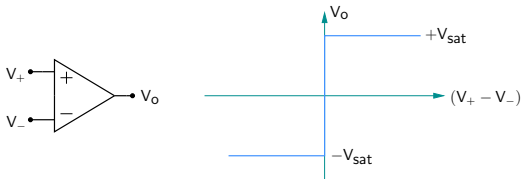


Comparators



An Op Amp in the open-loop configuration serves as a comparator because of its high gain ($\sim 10^5$) in the linear region.

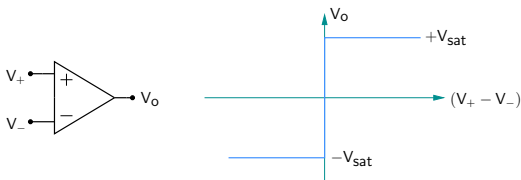
Comparators



An Op Amp in the open-loop configuration serves as a comparator because of its high gain ($\sim 10^5$) in the linear region.

As seen earlier, the width of the linear region, $[V_{sat} - (-V_{sat})]/A_V$, is small ($\sim 0.1 \text{ mV}$), and could be treated as 0.

Comparators

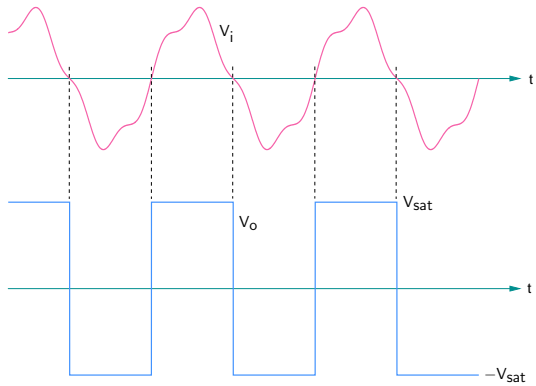
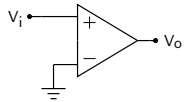


An Op Amp in the open-loop configuration serves as a comparator because of its high gain ($\sim 10^5$) in the linear region.

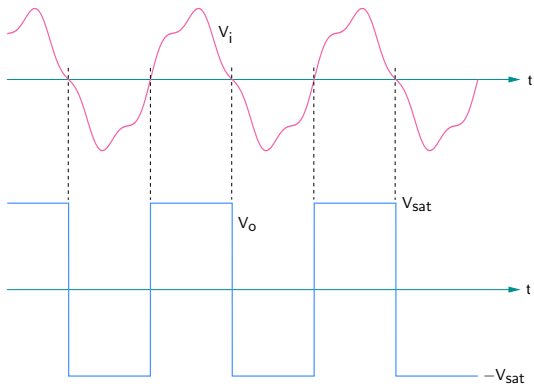
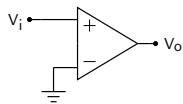
As seen earlier, the width of the linear region, $[V_{sat} - (-V_{sat})]/A_V$, is small ($\sim 0.1 \text{ mV}$), and could be treated as 0.

i.e., if $V_+ > V_-$, $V_o = +V_{sat}$,
if $V_+ < V_-$, $V_o = -V_{sat}$.

Comparators

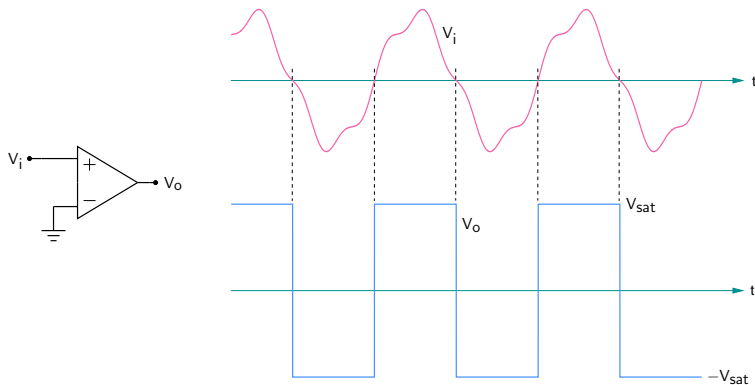


Comparators



A comparator can be used to convert an analog signal into a digital (high/low) signal for further processing with digital circuits.

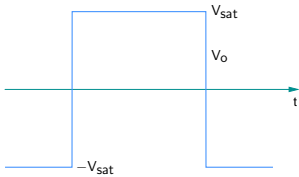
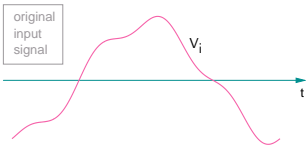
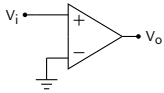
Comparators



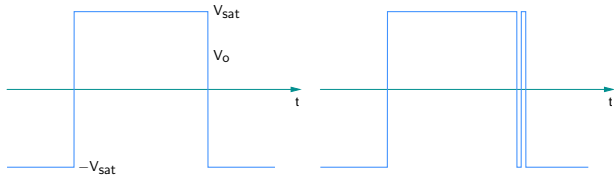
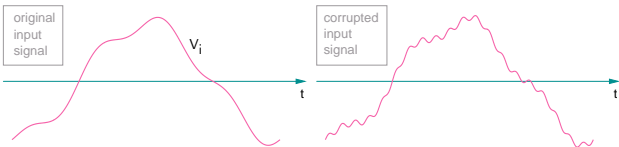
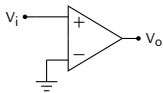
A comparator can be used to convert an analog signal into a digital (high/low) signal for further processing with digital circuits.

In practice, the input (analog) signal can have noise or electromagnetic pick-up superimposed on it. As a result, erroneous operation of the circuit may result
→ next slide.

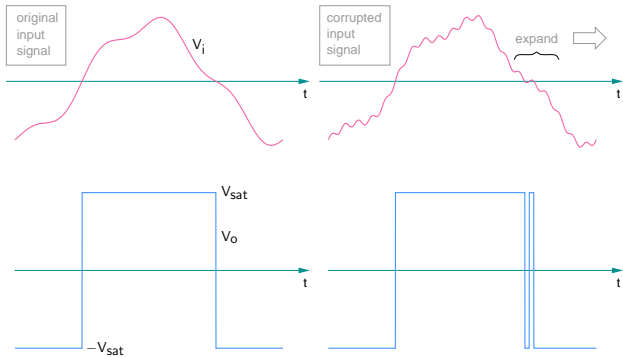
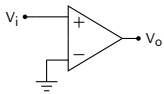
Comparators



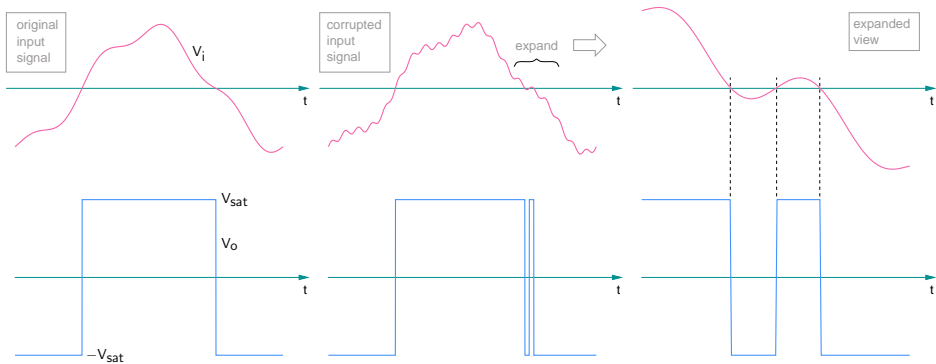
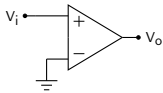
Comparators



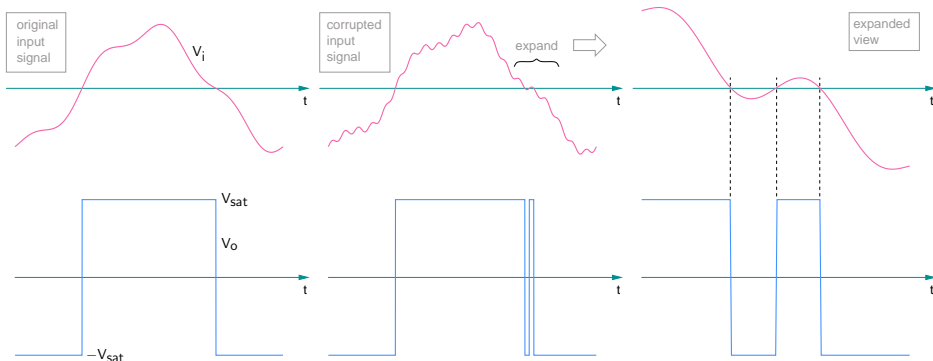
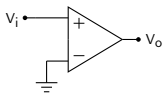
Comparators



Comparators

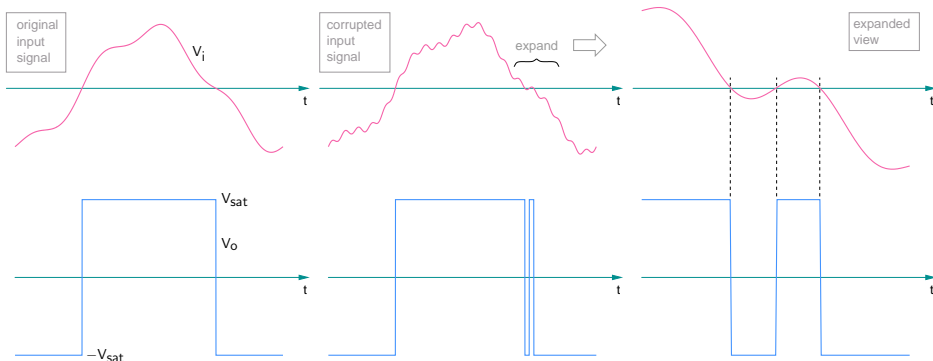
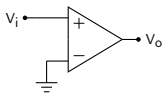


Comparators



The comparator has produced multiple (spurious) transitions or "bounces," referred to as "comparator chatter."

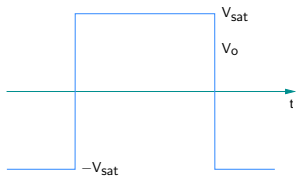
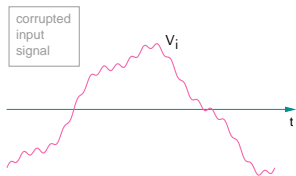
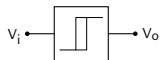
Comparators



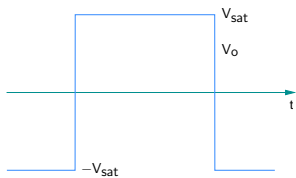
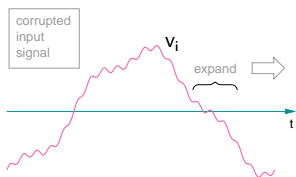
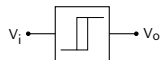
The comparator has produced multiple (spurious) transitions or “bounces,” referred to as “comparator chatter.”

A Schmitt trigger can be used to eliminate the chatter
→ next slide.

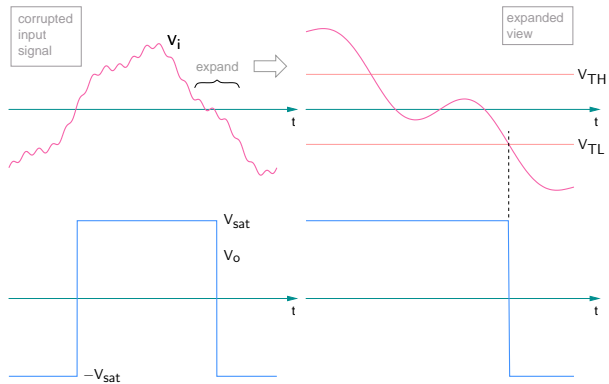
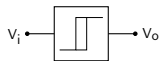
Comparators



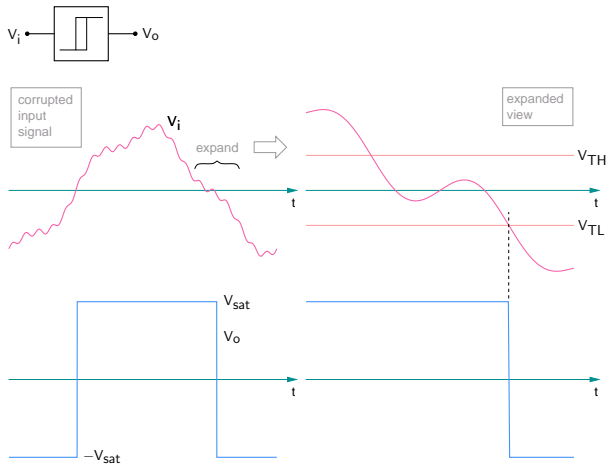
Comparators



Comparators

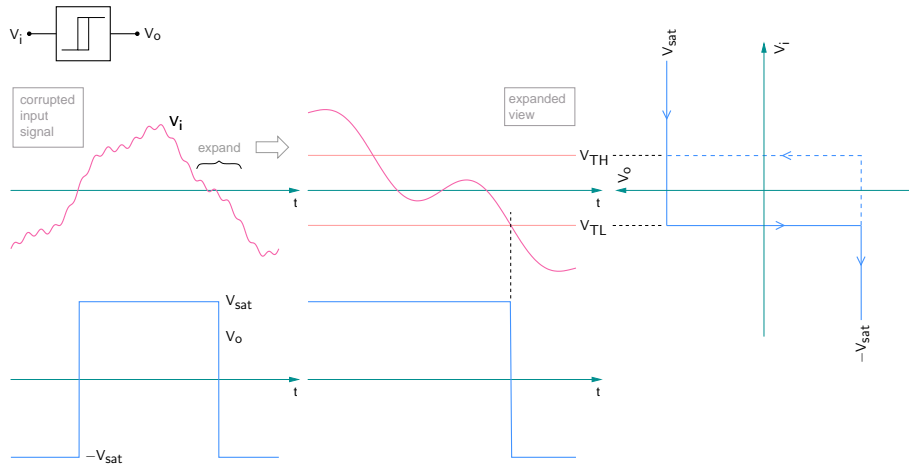


Comparators



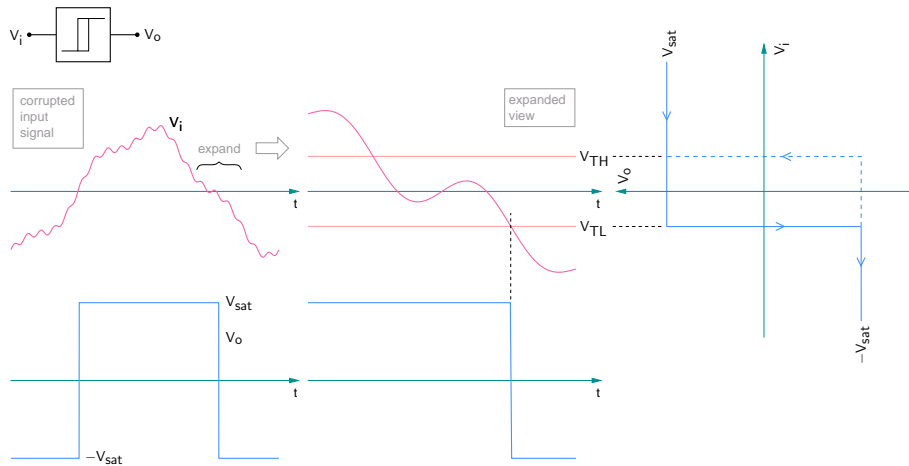
- * While going from positive to negative values, V_i needs to cross V_{TL} (and not 0 V) to cause a change in V_o .

Comparators



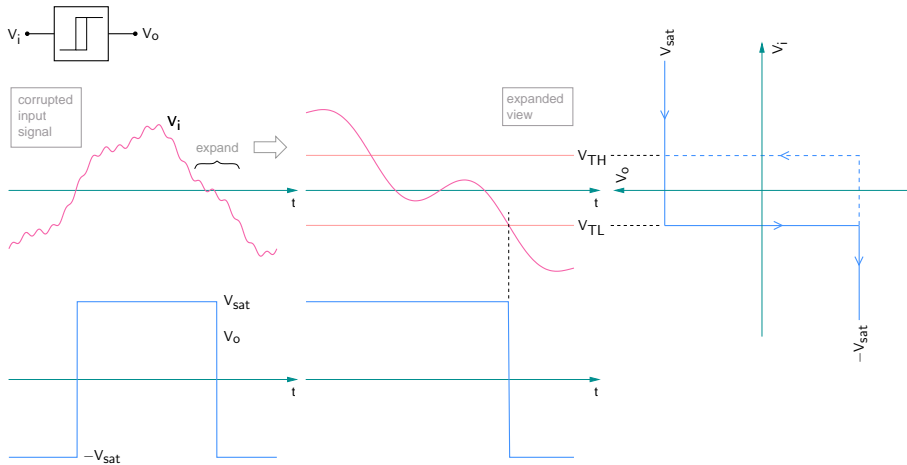
- * While going from positive to negative values, V_i needs to cross V_{TL} (and not 0 V) to cause a change in V_o .

Comparators



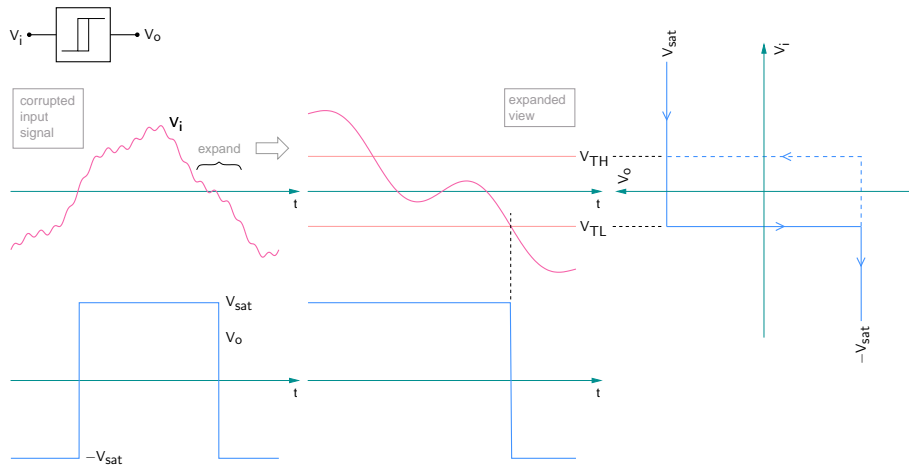
- * While going from positive to negative values, V_i needs to cross V_{TL} (and not 0 V) to cause a change in V_o .
- * In the reverse direction (negative to positive), V_i needs to cross V_{TH} .

Comparators



- * While going from positive to negative values, V_i needs to cross V_{TL} (and not 0 V) to cause a change in V_o .
- * In the reverse direction (negative to positive), V_i needs to cross V_{TH} .
- * The circuit gets rid of spurious transitions, a major advantage over the simple comparator.

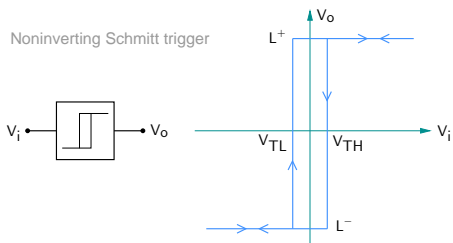
Comparators



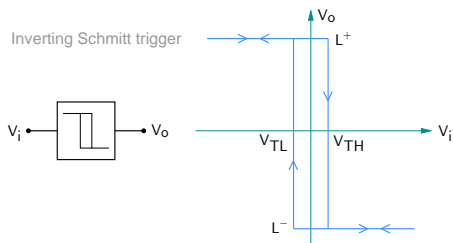
- * While going from positive to negative values, V_i needs to cross V_{TL} (and not 0 V) to cause a change in V_o .
- * In the reverse direction (negative to positive), V_i needs to cross V_{TH} .
- * The circuit gets rid of spurious transitions, a major advantage over the simple comparator.
- * The hysteresis width ($V_{TH} - V_{TL}$) should be designed to be larger than the spurious excursions riding on V_i .

Waveform generation using Schmitt triggers

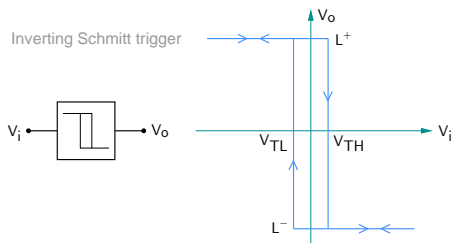
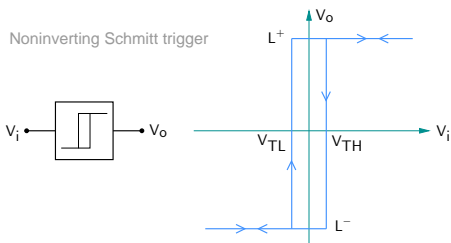
Noninverting Schmitt trigger



Inverting Schmitt trigger

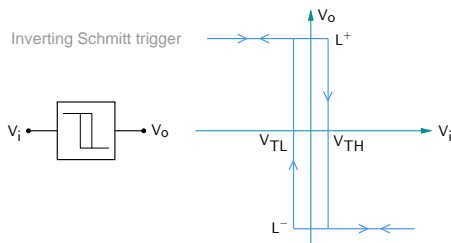
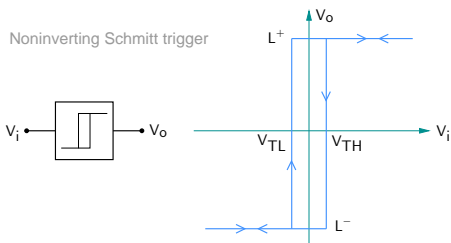


Waveform generation using Schmitt triggers



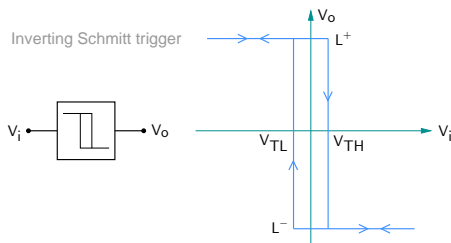
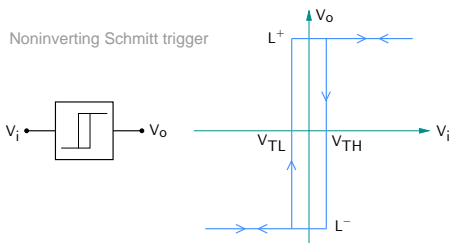
* A Schmitt trigger has two states, $V_o = L^+$ and $V_o = L^-$.

Waveform generation using Schmitt triggers



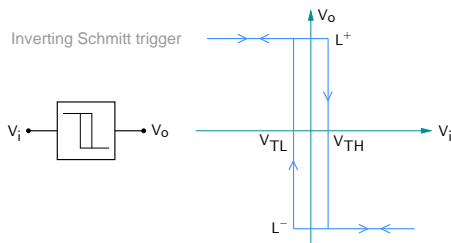
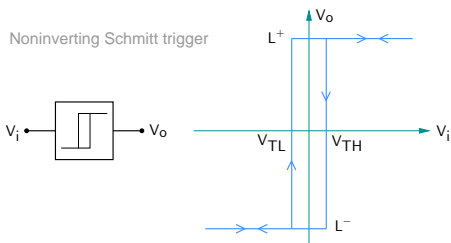
- * A Schmitt trigger has two states, $V_o = L^+$ and $V_o = L^-$.
- * With a suitable RC network, it can be made to freely oscillate between L^+ and L^- . Such a circuit is called an “astable multivibrator” or a “free-running multivibrator.”

Waveform generation using Schmitt triggers



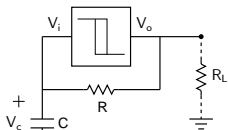
- * A Schmitt trigger has two states, $V_o = L^+$ and $V_o = L^-$.
- * With a suitable RC network, it can be made to freely oscillate between L^+ and L^- . Such a circuit is called an “astable multivibrator” or a “free-running multivibrator.”
- * An astable multivibrator produces oscillations *without* an input signal, the frequency being controlled by the component values.

Waveform generation using Schmitt triggers



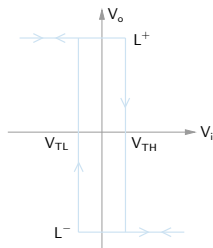
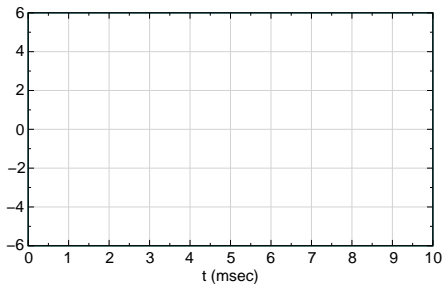
- * A Schmitt trigger has two states, $V_o = L^+$ and $V_o = L^-$.
- * With a suitable RC network, it can be made to freely oscillate between L^+ and L^- . Such a circuit is called an “astable multivibrator” or a “free-running multivibrator.”
- * An astable multivibrator produces oscillations *without* an input signal, the frequency being controlled by the component values.
- * The maximum operating frequency of these oscillators is typically ~ 10 kHz, due to Op Amp speed limitations.

Waveform generation using a Schmitt trigger

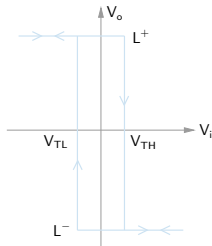
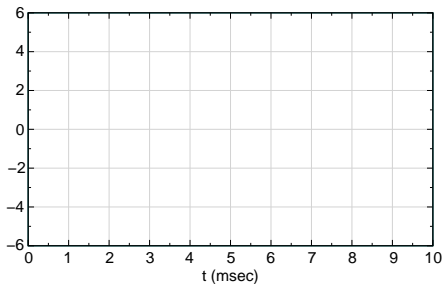
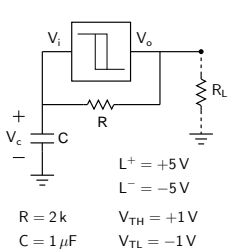


$$\begin{aligned}L^+ &= +5\text{V} \\L^- &= -5\text{V} \\V_{TH} &= +1\text{V} \\V_{TL} &= -1\text{V}\end{aligned}$$

$$\begin{aligned}R &= 2\text{k} \\C &= 1\mu\text{F}\end{aligned}$$

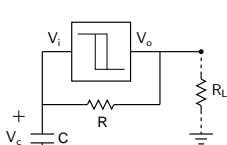


Waveform generation using a Schmitt trigger

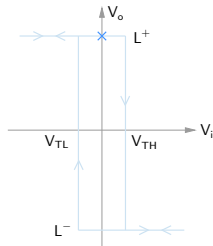
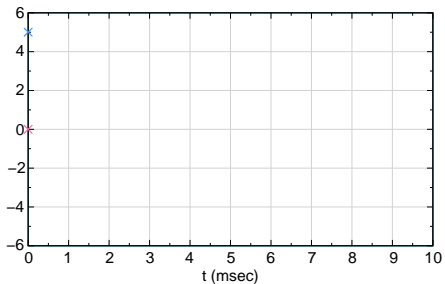


At $t = 0$, let $V_o = L^+$, and $V_c = 0\text{V}$.

Waveform generation using a Schmitt trigger

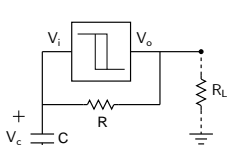


$$\begin{aligned}L^+ &= +5\text{V} \\L^- &= -5\text{V} \\V_{TH} &= +1\text{V} \\V_{TL} &= -1\text{V}\end{aligned}$$

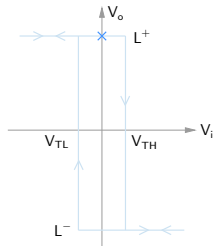
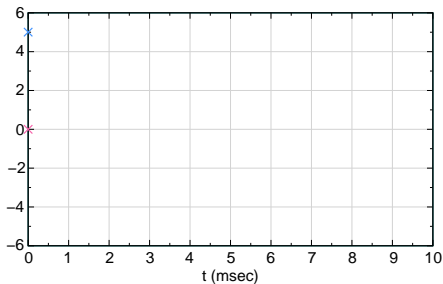


At $t = 0$, let $V_o = L^+$, and $V_c = 0\text{V}$.

Waveform generation using a Schmitt trigger



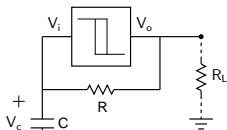
$$\begin{aligned}L^+ &= +5\text{ V} \\L^- &= -5\text{ V} \\V_{TH} &= +1\text{ V} \\V_{TL} &= -1\text{ V}\end{aligned}$$



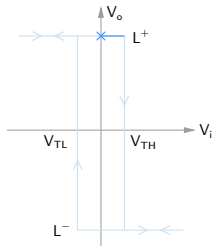
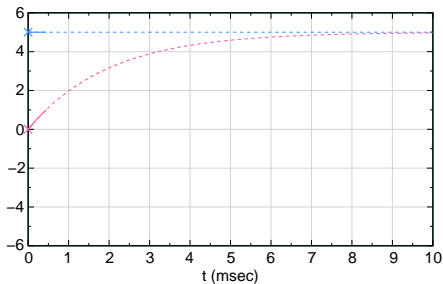
At $t = 0$, let $V_o = L^+$, and $V_c = 0$ V.

The capacitor starts charging toward L^+ .

Waveform generation using a Schmitt trigger



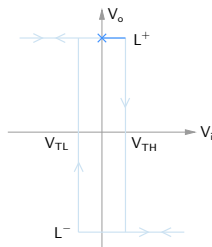
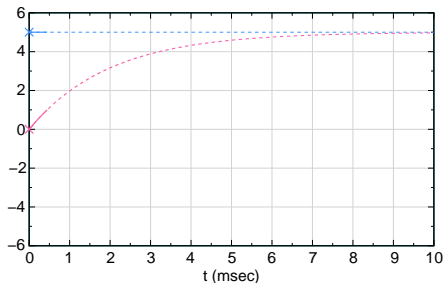
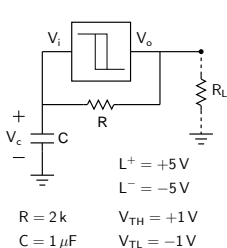
$$\begin{aligned}L^+ &= +5\text{V} \\L^- &= -5\text{V} \\V_{TH} &= +1\text{V} \\V_{TL} &= -1\text{V}\end{aligned}$$



At $t = 0$, let $V_o = L^+$, and $V_c = 0\text{V}$.

The capacitor starts charging toward L^+ .

Waveform generation using a Schmitt trigger

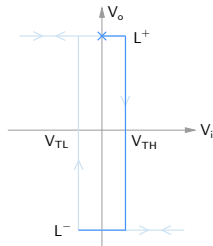
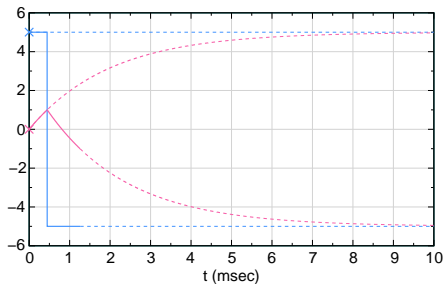
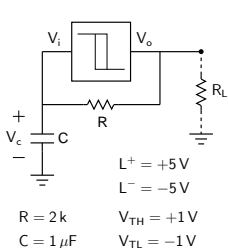


At $t = 0$, let $V_o = L^+$, and $V_c = 0\text{V}$.

The capacitor starts charging toward L^+ .

When V_c crosses V_{TH} , the output flips. Now, the capacitor starts discharging toward L^- .

Waveform generation using a Schmitt trigger

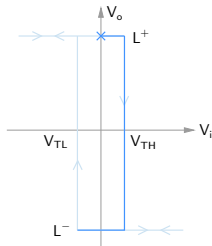
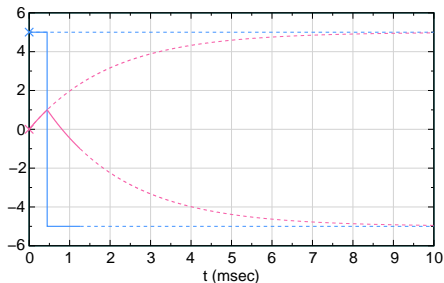
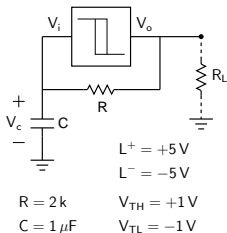


At $t = 0$, let $V_o = L^+$, and $V_c = 0\text{V}$.

The capacitor starts charging toward L^+ .

When V_c crosses V_{TH} , the output flips. Now, the capacitor starts discharging toward L^- .

Waveform generation using a Schmitt trigger



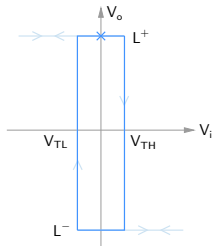
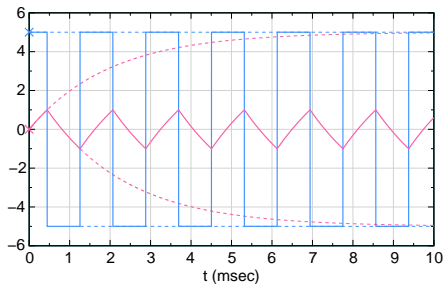
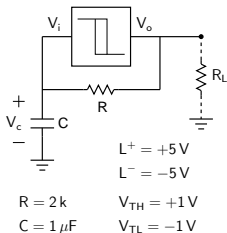
At $t = 0$, let $V_o = L^+$, and $V_c = 0$ V.

The capacitor starts charging toward L^+ .

When V_c crosses V_{TH} , the output flips. Now, the capacitor starts discharging toward L^- .

When V_c crosses V_{TL} , the output flips again \rightarrow oscillations.

Waveform generation using a Schmitt trigger



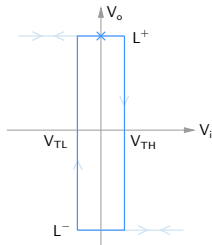
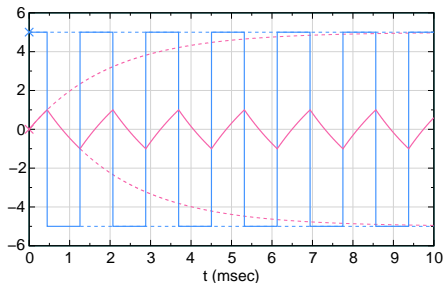
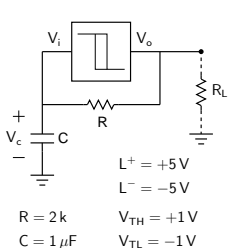
At $t = 0$, let $V_o = L^+$, and $V_c = 0V$.

The capacitor starts charging toward L^+ .

When V_c crosses V_{TH} , the output flips. Now, the capacitor starts discharging toward L^- .

When V_c crosses V_{TL} , the output flips again \rightarrow oscillations.

Waveform generation using a Schmitt trigger



At $t = 0$, let $V_o = L^+$, and $V_c = 0V$.

The capacitor starts charging toward L^+ .

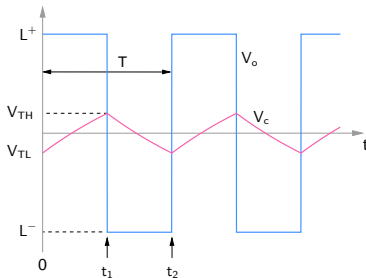
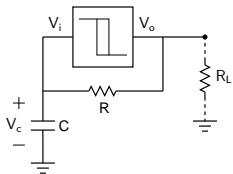
When V_c crosses V_{TH} , the output flips. Now, the capacitor starts discharging toward L^- .

When V_c crosses V_{TL} , the output flips again → oscillations.

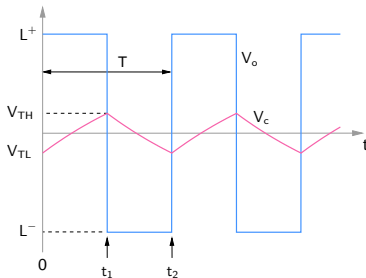
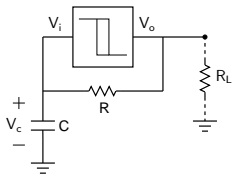
Note that the circuit oscillates *on its own*, i.e., without any input.

Q: Where is the energy coming from?

Waveform generation using a Schmitt trigger



Waveform generation using a Schmitt trigger

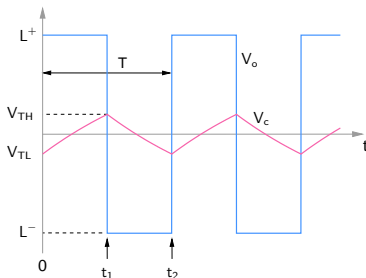
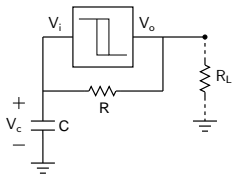


Charging: Let $V_c(t) = A_1 \exp(-t/\tau) + B_1$, with $\tau = RC$.

Using $V_c(0) = V_{TL}$, $V_c(\infty) = L^+$, find A_1 and B_1 .

At $t = t_1$, $V_c = V_{TH} \rightarrow V_{TH} = A_1 \exp(-t_1/\tau) + B_1 \rightarrow$ find t_1 .

Waveform generation using a Schmitt trigger



Charging: Let $V_c(t) = A_1 \exp(-t/\tau) + B_1$, with $\tau = RC$.

Using $V_c(0) = V_{TL}$, $V_c(\infty) = L^+$, find A_1 and B_1 .

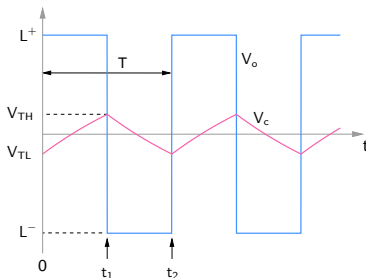
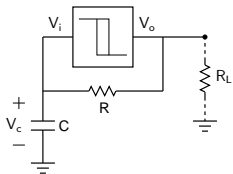
At $t = t_1$, $V_c = V_{TH} \rightarrow V_{TH} = A_1 \exp(-t_1/\tau) + B_1 \rightarrow$ find t_1 .

Discharging: Let $V_c(t) = A_2 \exp(-(t - t_1)/\tau) + B_2$.

Using $V_c(t_1) = V_{TH}$, $V_c(\infty) = L^-$, find A_2 and B_2 .

At $t = t_2$, $V_c = V_{TL} \rightarrow V_{TL} = A_2 \exp(-(t_2 - t_1)/\tau) + B_2 \rightarrow$ find $(t_2 - t_1)$.

Waveform generation using a Schmitt trigger



Charging: Let $V_c(t) = A_1 \exp(-t/\tau) + B_1$, with $\tau = RC$.

Using $V_c(0) = V_{TL}$, $V_c(\infty) = L^+$, find A_1 and B_1 .

At $t = t_1$, $V_c = V_{TH} \rightarrow V_{TH} = A_1 \exp(-t_1/\tau) + B_1 \rightarrow$ find t_1 .

Discharging: Let $V_c(t) = A_2 \exp(-(t - t_1)/\tau) + B_2$.

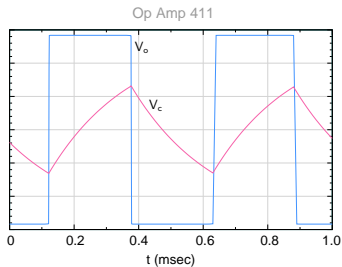
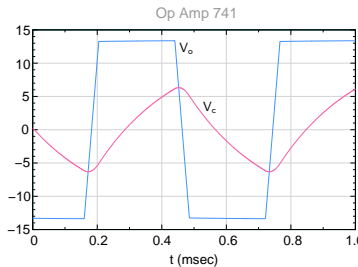
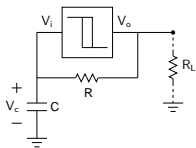
Using $V_c(t_1) = V_{TH}$, $V_c(\infty) = L^-$, find A_2 and B_2 .

At $t = t_2$, $V_c = V_{TL} \rightarrow V_{TL} = A_2 \exp(-(t_2 - t_1)/\tau) + B_2 \rightarrow$ find $(t_2 - t_1)$.

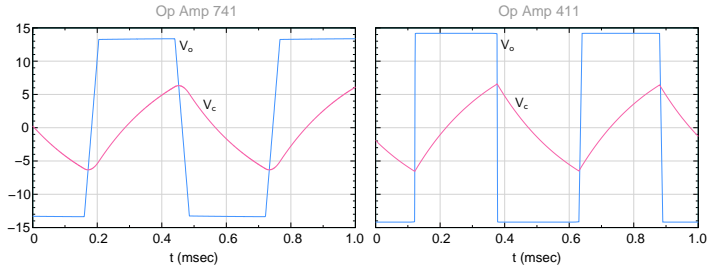
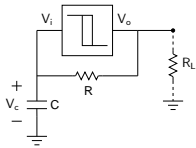
If $L^+ = L$, $L^- = -L$, $V_{TH} = V_T$, $V_{TL} = -V_T$, show that

$$T = 2RC \ln \left(\frac{L + V_T}{L - V_T} \right).$$

Waveform generation using a Schmitt trigger

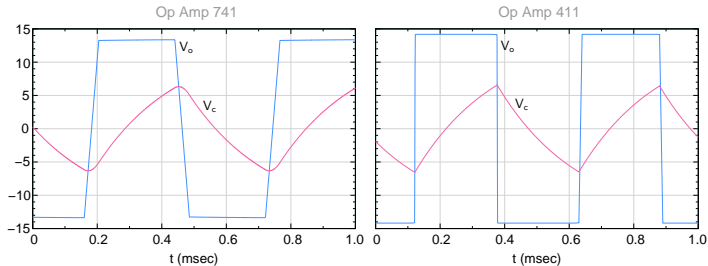
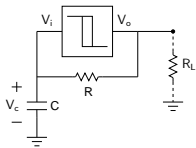


Waveform generation using a Schmitt trigger



Note that Op Amp 411 (slew rate: $10 \text{ V}/\mu\text{s}$) gives sharper waveforms as compared to Op Amp 741 (slew rate: $0.5 \text{ V}/\mu\text{s}$).

Waveform generation using a Schmitt trigger

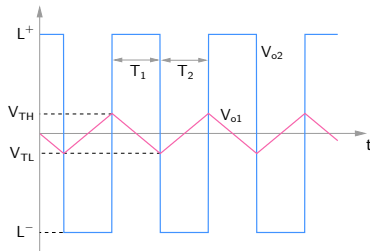
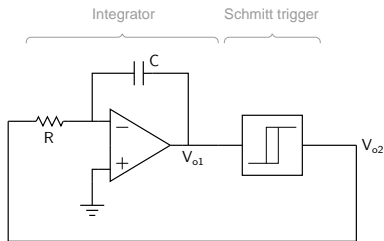


Note that Op Amp 411 (slew rate: $10 \text{ V}/\mu\text{s}$) gives sharper waveforms as compared to Op Amp 741 (slew rate: $0.5 \text{ V}/\mu\text{s}$).

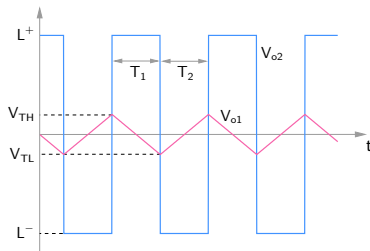
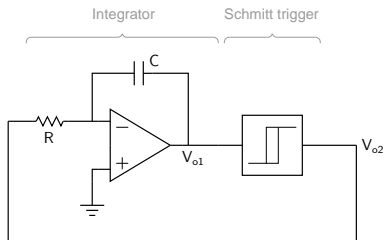
SEQUEL files: [schmitt_osc_741.sqproj](#), [schmitt_osc_411.sqproj](#)

(Ref: J. M. Fiore, "Op Amps and linear ICs")

Waveform generation using a Schmitt trigger

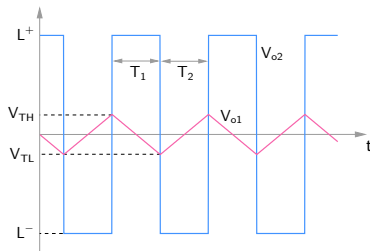
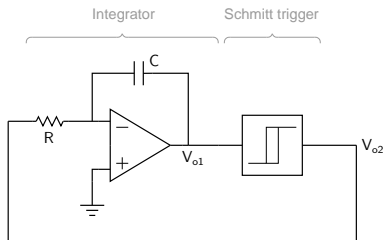


Waveform generation using a Schmitt trigger



For the integrator,
$$V_{o1} = -\frac{1}{RC} \int V_{o2} dt,$$

Waveform generation using a Schmitt trigger

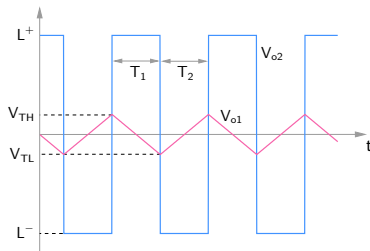
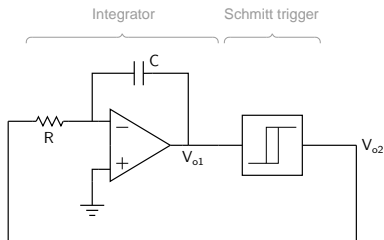


For the integrator, $V_{o1} = -\frac{1}{RC} \int V_{o2} dt$,

$V_{o2} = L^+ \rightarrow V_{o1}$ decreases linearly.

$V_{o2} = L^- \rightarrow V_{o1}$ increases linearly.

Waveform generation using a Schmitt trigger



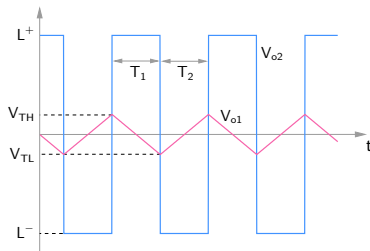
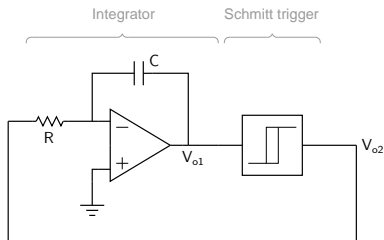
$$\text{For the integrator, } V_{o1} = -\frac{1}{RC} \int V_{o2} dt,$$

$V_{o2} = L^+ \rightarrow V_{o1}$ decreases linearly.

$V_{o2} = L^- \rightarrow V_{o1}$ increases linearly.

$$T_1 = \frac{V_{TH} - V_{TL}}{L^+ / RC} = RC \frac{V_{TH} - V_{TL}}{L^+}.$$

Waveform generation using a Schmitt trigger



$$\text{For the integrator, } V_{o1} = -\frac{1}{RC} \int V_{o2} dt,$$

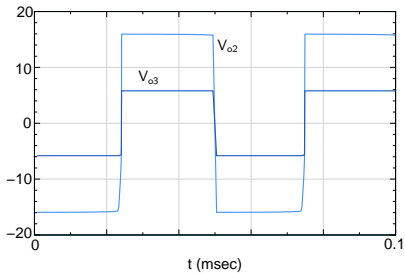
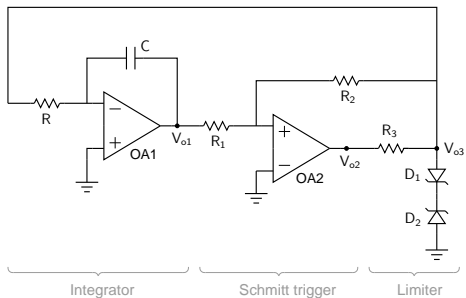
$V_{o2} = L^+ \rightarrow V_{o1}$ decreases linearly.

$V_{o2} = L^- \rightarrow V_{o1}$ increases linearly.

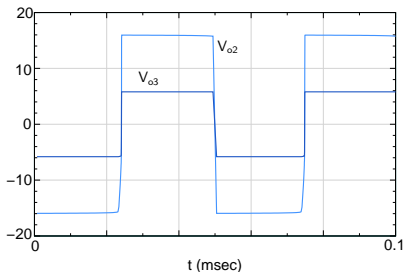
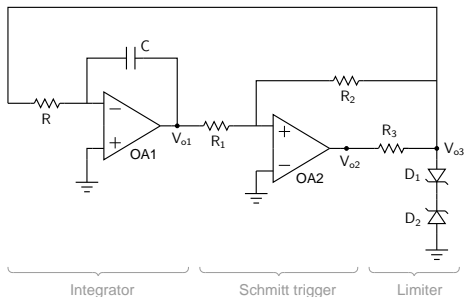
$$T_1 = \frac{V_{TH} - V_{TL}}{L^+ / RC} = RC \frac{V_{TH} - V_{TL}}{L^+}.$$

$$T_2 = \frac{V_{TH} - V_{TL}}{-L^- / RC} = RC \frac{V_{TH} - V_{TL}}{-L^-}.$$

Limiting the output voltage

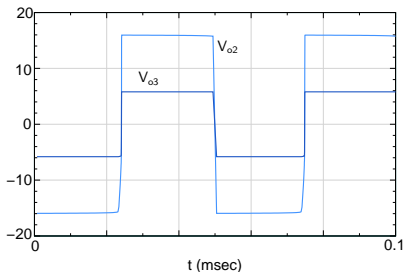
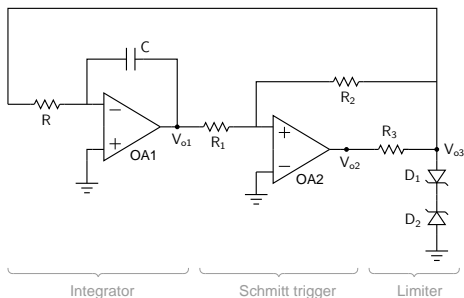


Limiting the output voltage



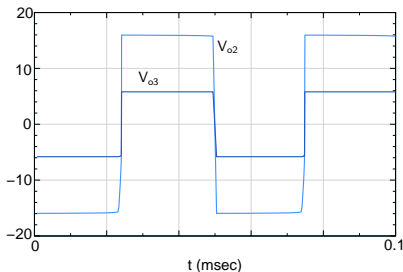
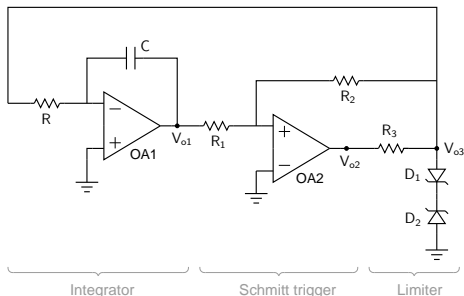
- * When $V_{o2} = +V_{sat}$, D_1 is forward-biased (with a voltage drop of V_{on}), and D_2 is reverse-biased. The Zener breakdown voltage (V_Z) is chosen so that D_2 operates under breakdown condition.
→ $V_{o3} = V_{on} + V_Z$.

Limiting the output voltage



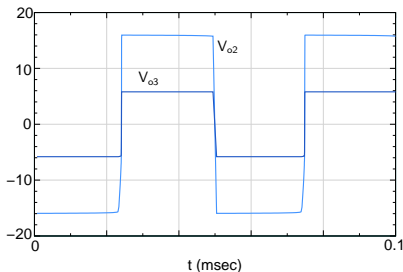
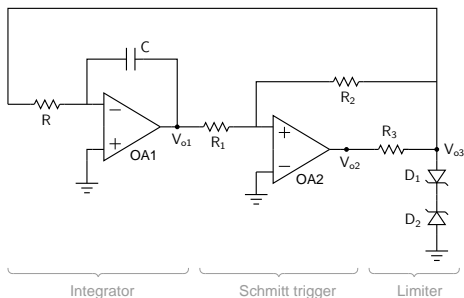
- * When $V_{o2} = +V_{sat}$, D_1 is forward-biased (with a voltage drop of V_{on}), and D_2 is reverse-biased. The Zener breakdown voltage (V_Z) is chosen so that D_2 operates under breakdown condition.
→ $V_{o3} = V_{on} + V_Z$.
- * When $V_{o2} = -V_{sat}$, D_2 is forward-biased (with a voltage drop of V_{on}), and D_1 is reverse-biased.
→ $V_{o3} = -V_{on} - V_Z$.

Limiting the output voltage



- * When $V_{o2} = +V_{sat}$, D_1 is forward-biased (with a voltage drop of V_{on}), and D_2 is reverse-biased. The Zener breakdown voltage (V_Z) is chosen so that D_2 operates under breakdown condition.
 $\rightarrow V_{o3} = V_{on} + V_Z$.
- * When $V_{o2} = -V_{sat}$, D_2 is forward-biased (with a voltage drop of V_{on}), and D_1 is reverse-biased.
 $\rightarrow V_{o3} = -V_{on} - V_Z$.
- * R_3 serves to limit the output current for OA2.

Limiting the output voltage



- * When $V_{o2} = +V_{sat}$, D_1 is forward-biased (with a voltage drop of V_{on}), and D_2 is reverse-biased. The Zener breakdown voltage (V_Z) is chosen so that D_2 operates under breakdown condition.
 $\rightarrow V_{o3} = V_{on} + V_Z$.
- * When $V_{o2} = -V_{sat}$, D_2 is forward-biased (with a voltage drop of V_{on}), and D_1 is reverse-biased.
 $\rightarrow V_{o3} = -V_{on} - V_Z$.
- * R_3 serves to limit the output current for OA2.

SEQUEL file: opamp_osc.1.sqproj