

Test Pattern Generation

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EE 709: Testing & Verification of VLSI Circuits

Lecture – 11 (Jan 26, 2012)

Boolean Difference

- **Shannon's Expansion Theorem:**

$$F(X_1, X_2, \dots, X_n) = X_2 \cdot F(X_1, 1, \dots, X_n) + \overline{X_2} \cdot F(X_1, 0, \dots, X_n)$$

- **Boolean Difference (partial derivative):**

$$\frac{\partial F_j}{\partial g} = F_j(1, X_1, X_2, \dots, X_n) \oplus F_j(0, X_1, \dots, X_n)$$

- **Fault Detection Requirements:**

$$G(X_1, X_2, \dots, X_n) = 1$$

$$\frac{\partial F_j}{\partial g} = F_j(1, X_1, X_2, \dots, X_n) \oplus F_j(0, X_1, \dots, X_n) = 1$$

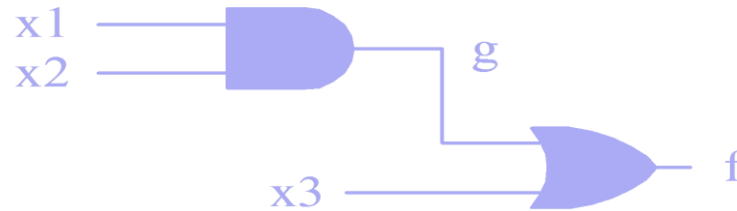
Boolean Difference

$$f(x_1, \dots, x_i = 0, \dots, x_n) \oplus f(x_1, \dots, x_i = 1, \dots, x_n) = 1$$

- Represented by the symbol $df(x)/dx$
- $df(x)/dx_i$ for $x = 0$ and $df(x)/dx_i$ for $x = 1$ are called *the residues/co-factors* of the function for $x = x_i$
- One of the residue is the good-circuit value and the other is the faulty-circuit value for x_i
- To detect the fault, the two residues should be complementary
- Solving the equation yield the values of the primary inputs to detect a stuck-at fault on x_i
- The **test pattern** is: $x_i df(x)/dx_i = 1$ & $x_i' df(x)/dx_i = 1$

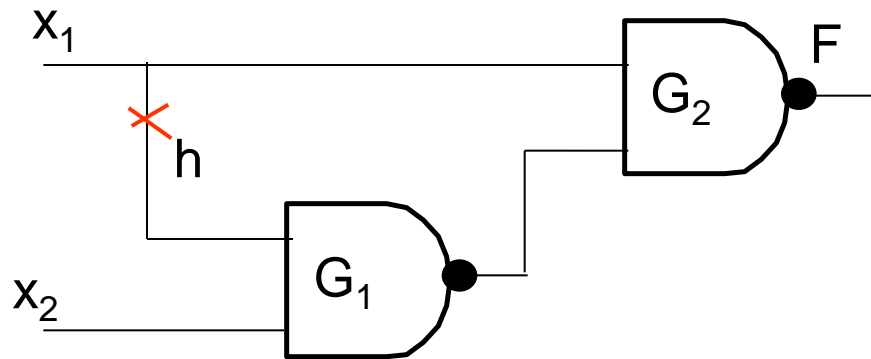
Fault Detection

- ❖ x_i $df(x)/dx_i = 1$ for s-a-0 at x_i
- ❖ x_i' $df(x)/dx_i = 1$ for s-a-1 at x_i
- ❖ As an example, let us consider the function



- ❖ $f(x) = x_1x_2 + x_3$
- ❖ Thus $df(x)/dx_2 = x_3 \oplus (x_1 + x_3) = x_3'x_1 = 1$. Then
- ❖ $x_1 = 1$ and $x_3 = 0$.
- ❖ For the SA1 and SA0 faults on x_2 , the patterns are then $x_1x_2x_3 = (100)$ and (110) , respectively.

Fault Detection



S-a-0 fault at **h**

Test Vector

$$h(X) \frac{dF^*(X,h)}{dh} = 1$$

$$x_1 \cdot x_1 x_2 = x_1 x_2 = 1$$

$$x_1 = 1$$

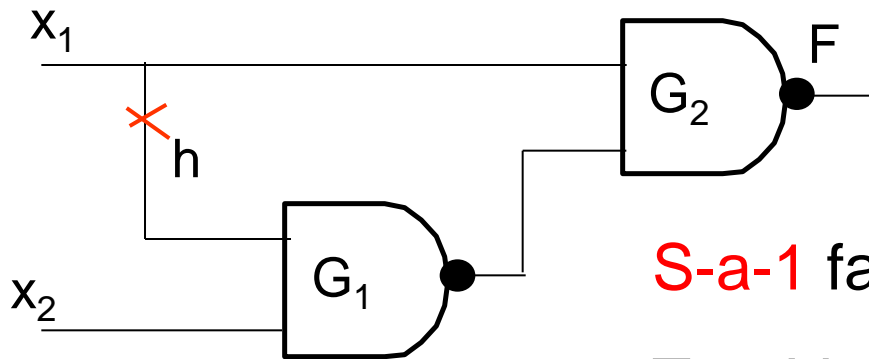
$$x_2 = 1$$

$$F(X,h) = x_1' + hx_2$$

$$h(X) = x_1$$

$$\begin{aligned} \frac{dF^*(X,h)}{dh} &= x_1' \oplus (x_1' + x_2) \\ &= x_1 x_2 \end{aligned}$$

Fault Detection



S-a-1 fault at **h**

Test Vector

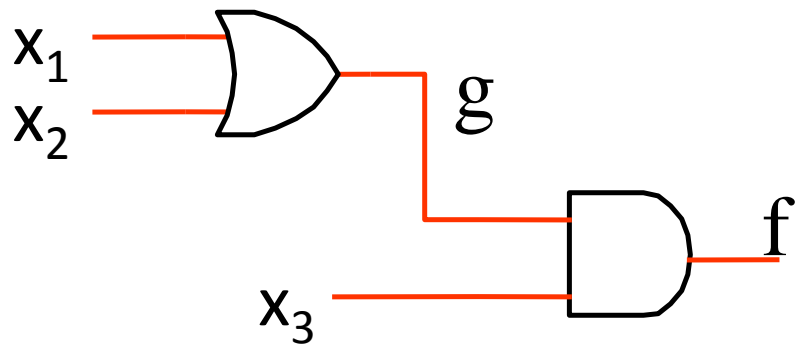
$$h(X)' \frac{dF^*(X,h)}{dh} = 1$$

$$x'_1 x_1 x_2 = x_1 x_2 = 0$$

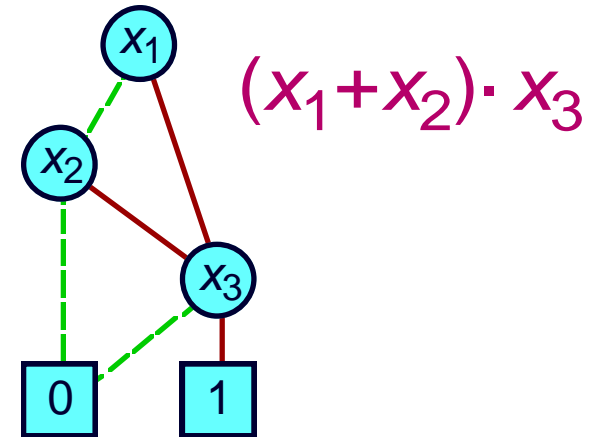
It cannot satisfy required condition

Fault - Redundant

TG using BDDs (1/4)



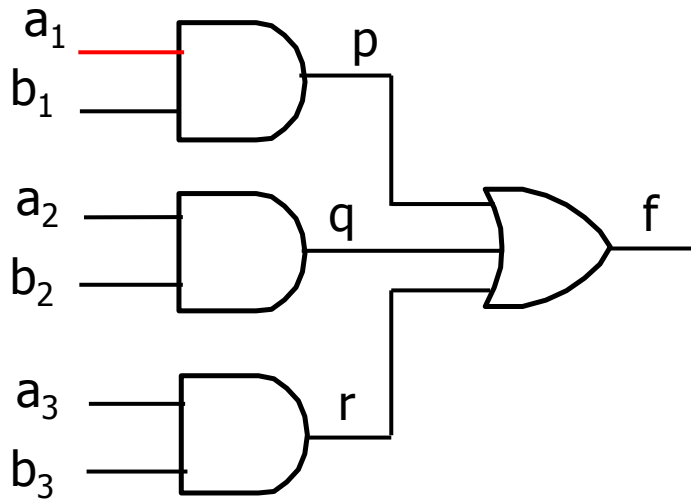
Reduced Graph



- ❖ Trace a path from the root to 0 and 1
- ❖ Value of the variables other than fault should have same value
- ❖ TP for s-a-0 fault at x_1 is $x_1x_2x_3 = 101$
- ❖ TP for s-a-1 fault at x_1 is $x_1x_2x_3 = 001$

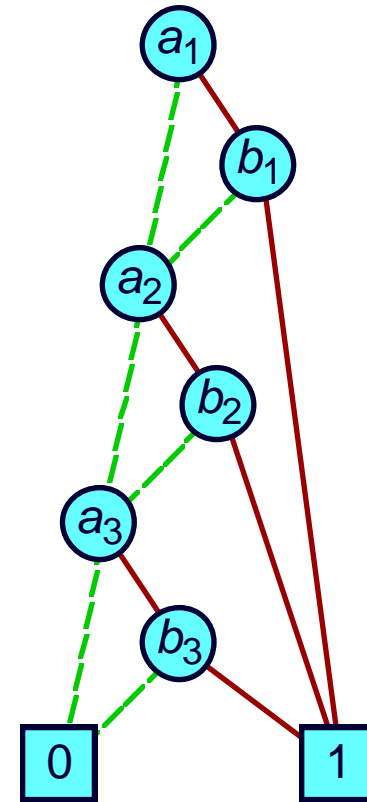
TG using BDDs (2/4)

$$(a_1 \wedge b_1) \vee (a_2 \wedge b_2) \vee (a_3 \wedge b_3)$$



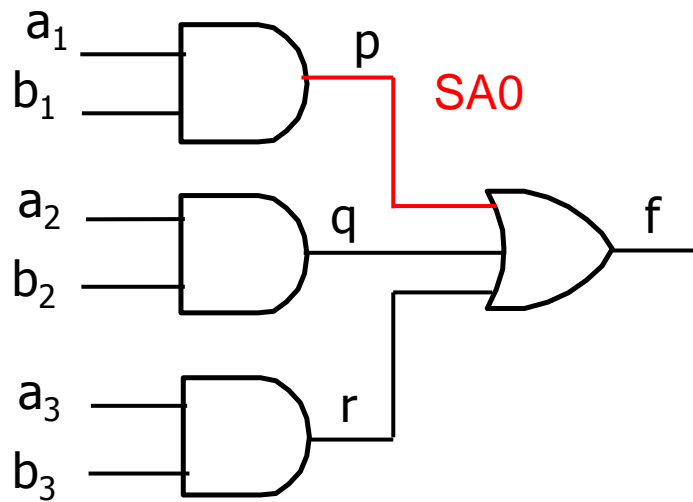
s-a-0 at a_1

$a_1=1, b_1=1, a_2=0, a_3=0$



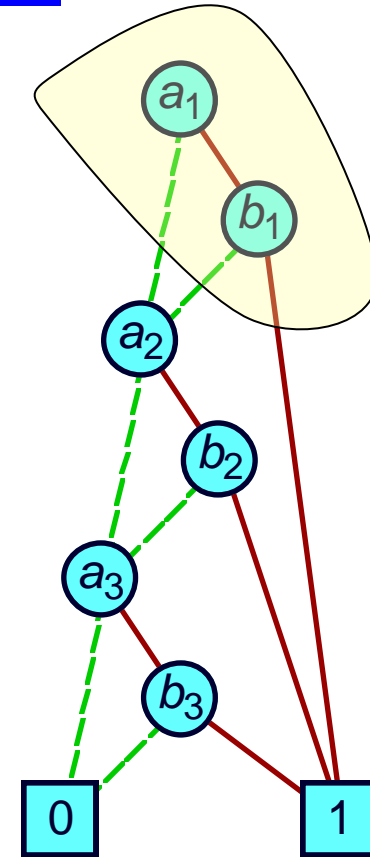
TG using BDDs (3/4)

$$(a_1 \wedge b_1) \vee (a_2 \wedge b_2) \vee (a_3 \wedge b_3)$$



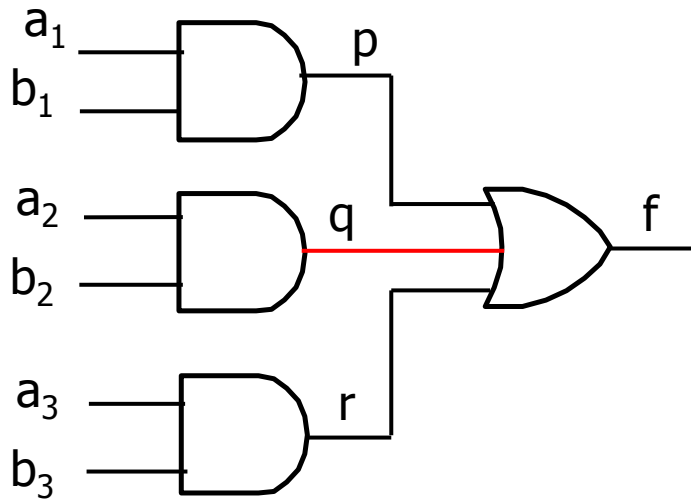
s-a-0 at p

$$a_1=1, b_1=1, a_2=0, a_3=0$$



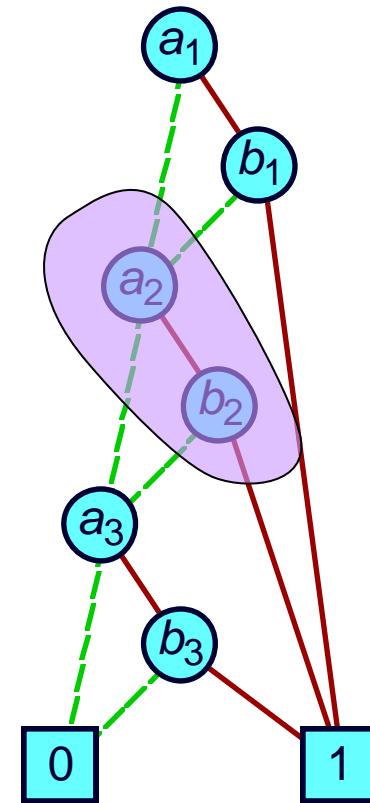
TG using BDDs (4/4)

$$(a_1 \wedge b_1) \vee (a_2 \wedge b_2) \vee (a_3 \wedge b_3)$$



s-a-0 at q

$$a_2=1, b_2=1, a_1=0, a_3=0$$



ATPG - Algorithmic

❖ Path Sensitization Method

- Fault Sensitization
- Fault Propagation
- Line Justification

❖ Path Sensitization Algorithms

- D- Algorithm (Roth)
- PODEM (P. Goel)
- FAN (Fujiwara)
- SOCRATES (Schultz)
- SPIRIT (Emil & Fujiwara)

Path Sensitization

General Structure of TG Algorithm

begin

set all values to x

Justify (l, v)

if ($v = 0$) then *Propagate (l, D)*

else *Propagate (l, D')*

end

Path Sensitization

Justify(I, val)

begin

set I to val

if I is a PI then return

/ I is a gate output */*

c = controlling value of I

i = inversion of I

ival = val \oplus i

if (ival = c')

then for every input j of I

Justify (j, ival)

else

select one input (j) of I

Justify (j, ival)

end

Path Sensitization

Propagate (l, err)

/* err is D or D' */

begin

set l to err

if l is PO then RETURN

k = fanout of l

c = controlling value of k

i = inversion of k

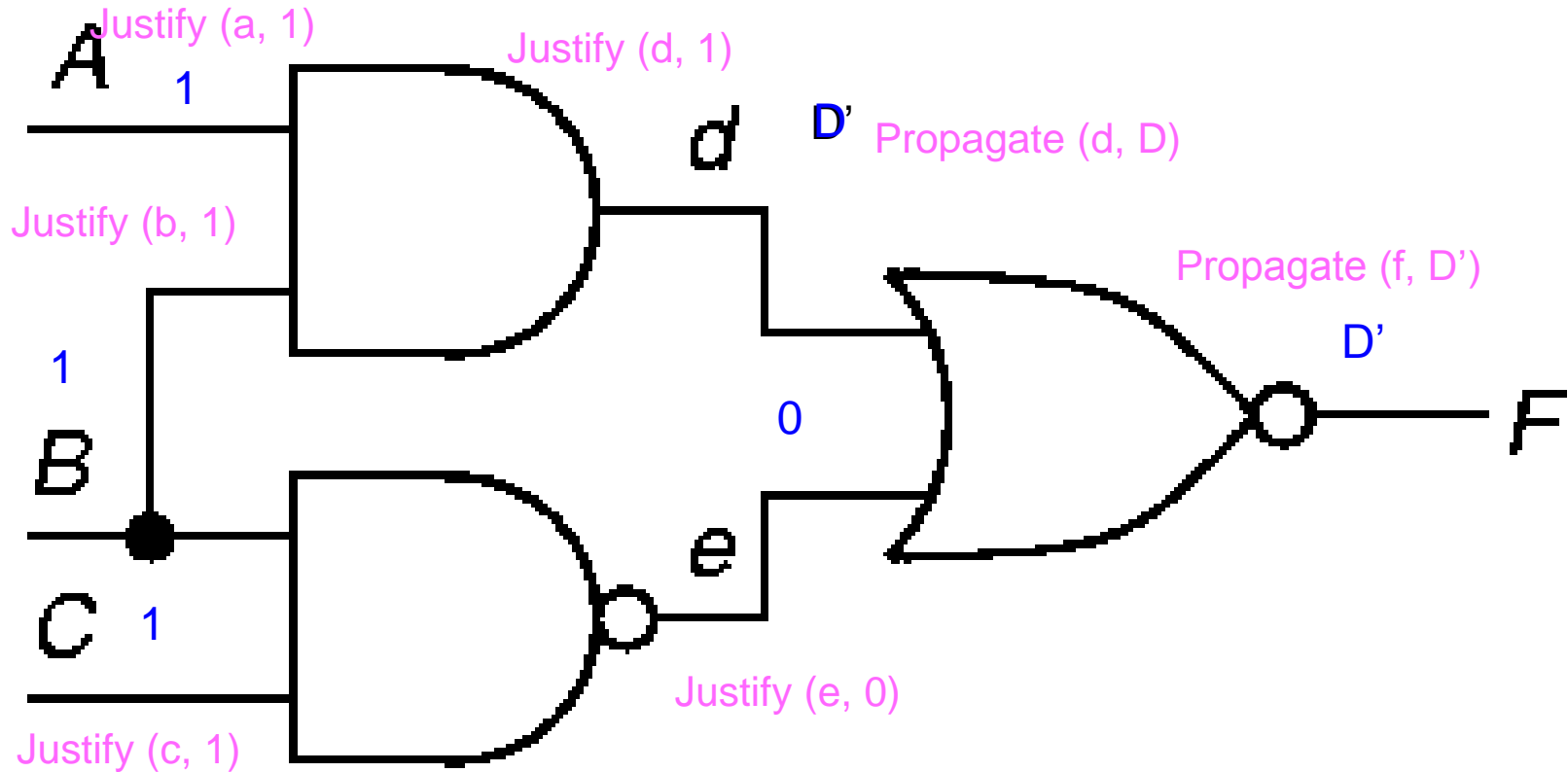
for every input of j of k other than l

Justify (j, c')

Propagate (k, err \oplus i)

end

Path Sensitization



Common Concept

- ❖ Fault Activation problem \rightarrow a LJ Problem
- ❖ The Fault Propagation problem \rightarrow
 1. Select a FP path to PO \rightarrow Decision
 2. Once the path is selected \rightarrow a set of LJ problems
- ❖ The LJ Problems \rightarrow Decisions or Implications



To justify $c = 1 \rightarrow a = 1, b = 1$ (Implication)

To justify $c = 0 \rightarrow a = 0$ or $b = 0$ (Decision)

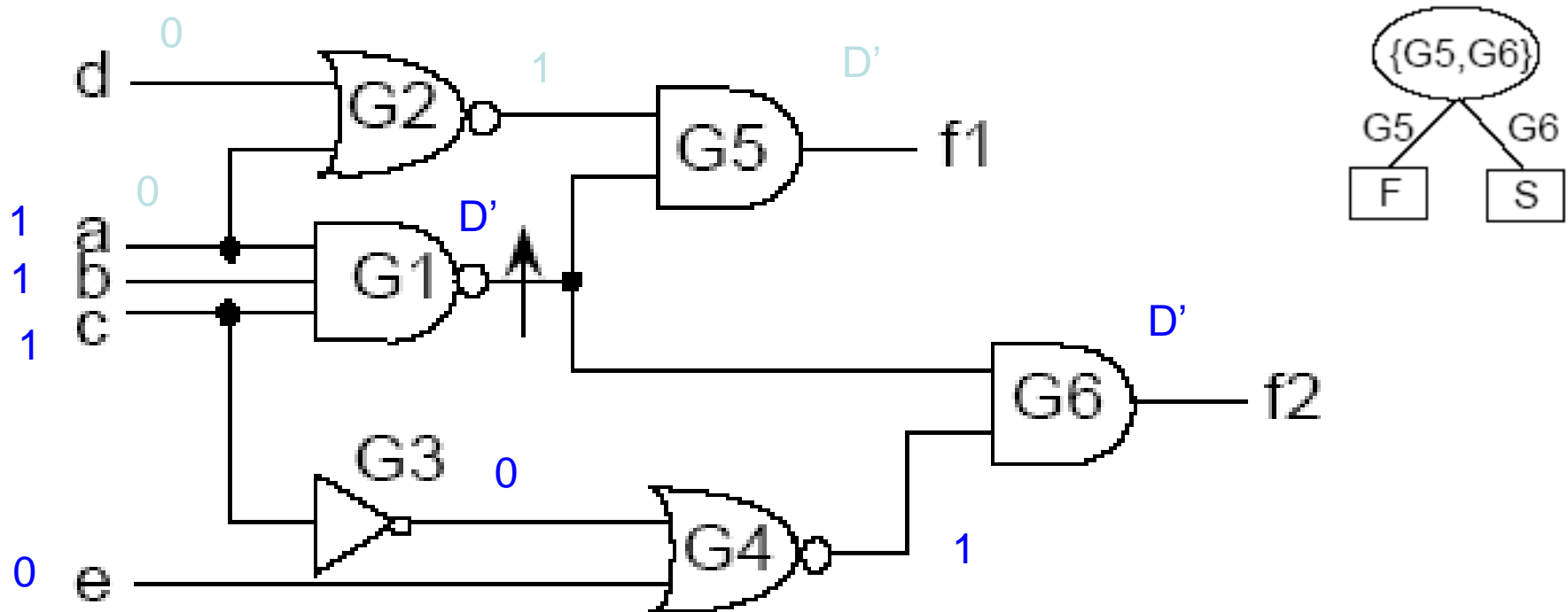
- ❖ Incorrect decision \rightarrow Backtrack \rightarrow Another decision

D-Algorithm

Roth (IBM) - 1966

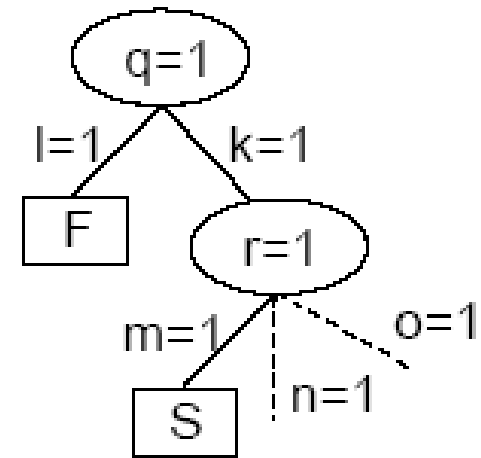
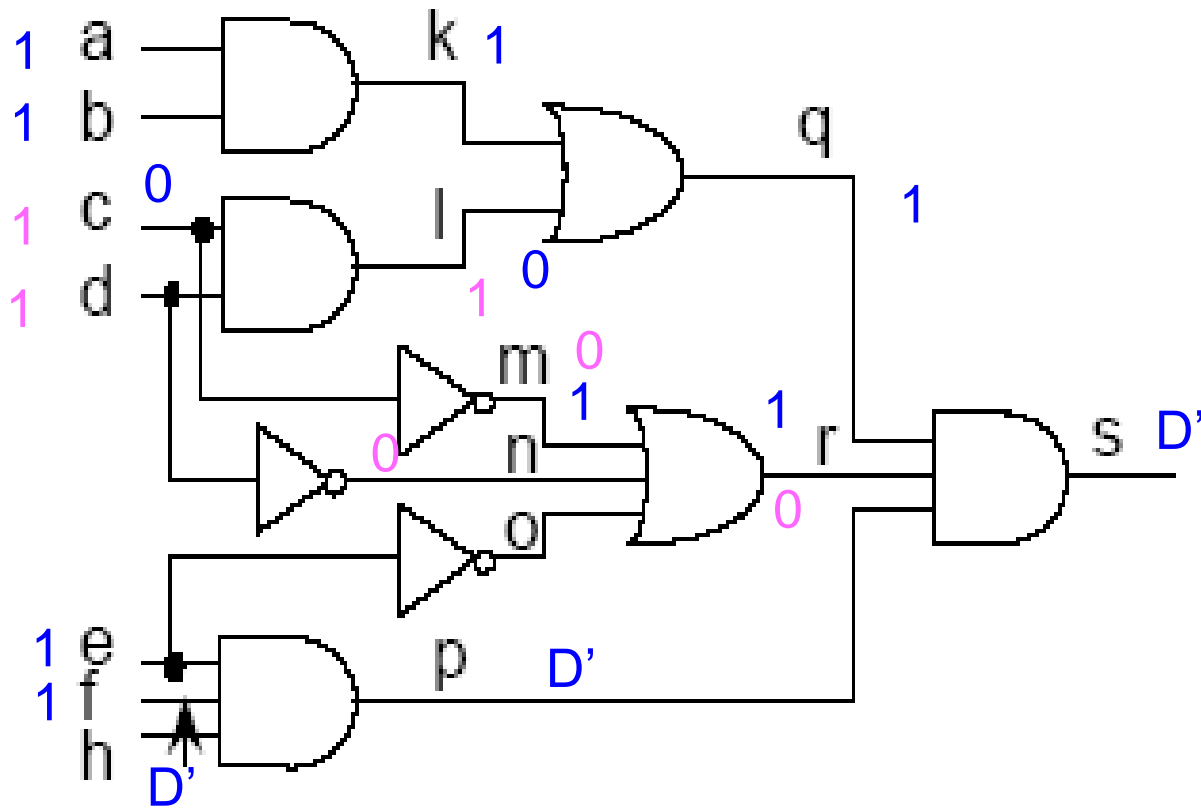
- Fundamental concepts invented:
 - First complete ATPG algorithm
 - **D-Calculus** (5 valued logic)
 - Implications – forward and backward
 - Implication stack
 - **Backtrack**
 - Test Search Space

Decisions during FP



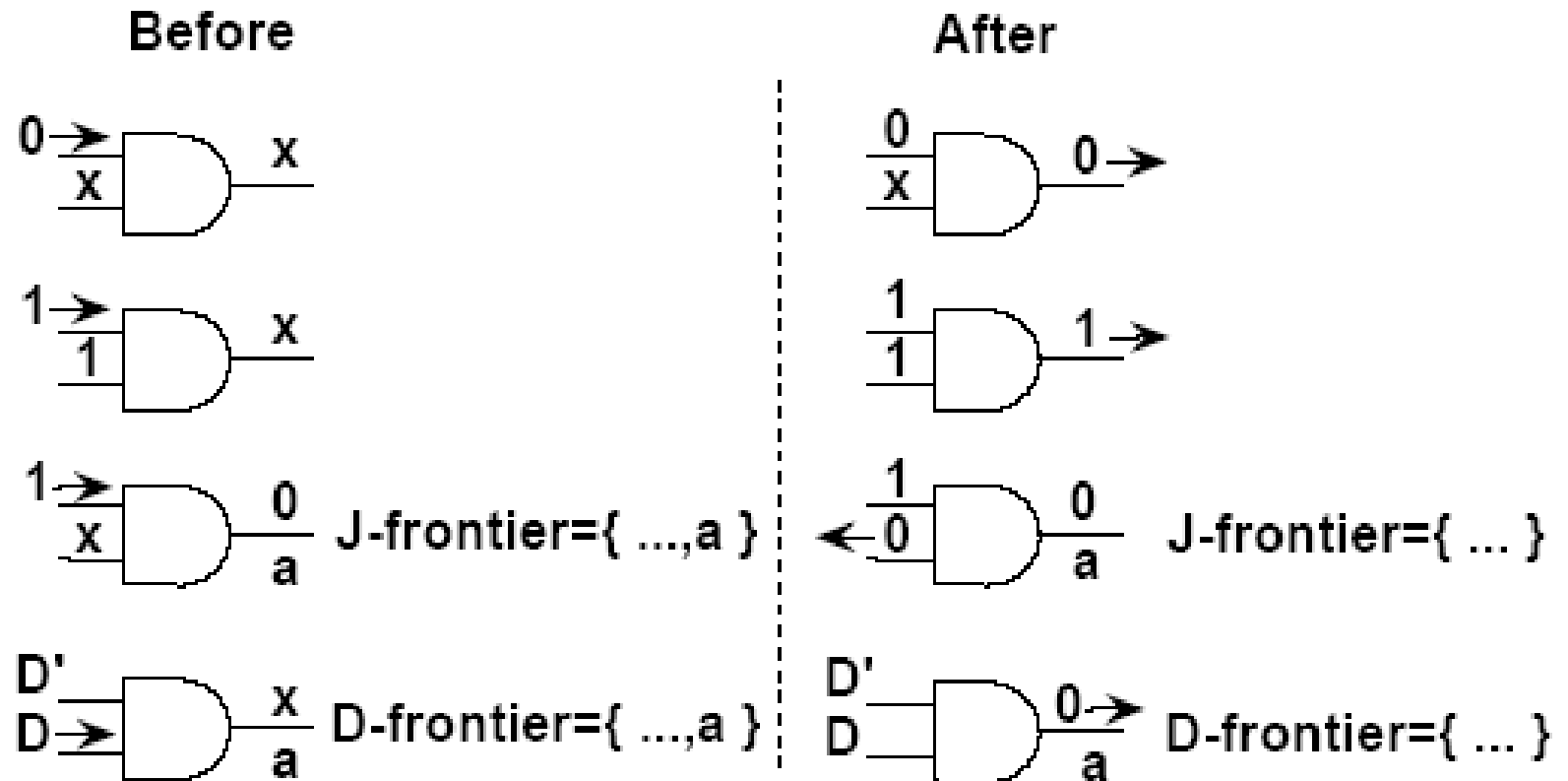
D – frontier: The set of all gates whose output value is currently x but have one or more **fault** signals on their inputs

Decisions during LJ

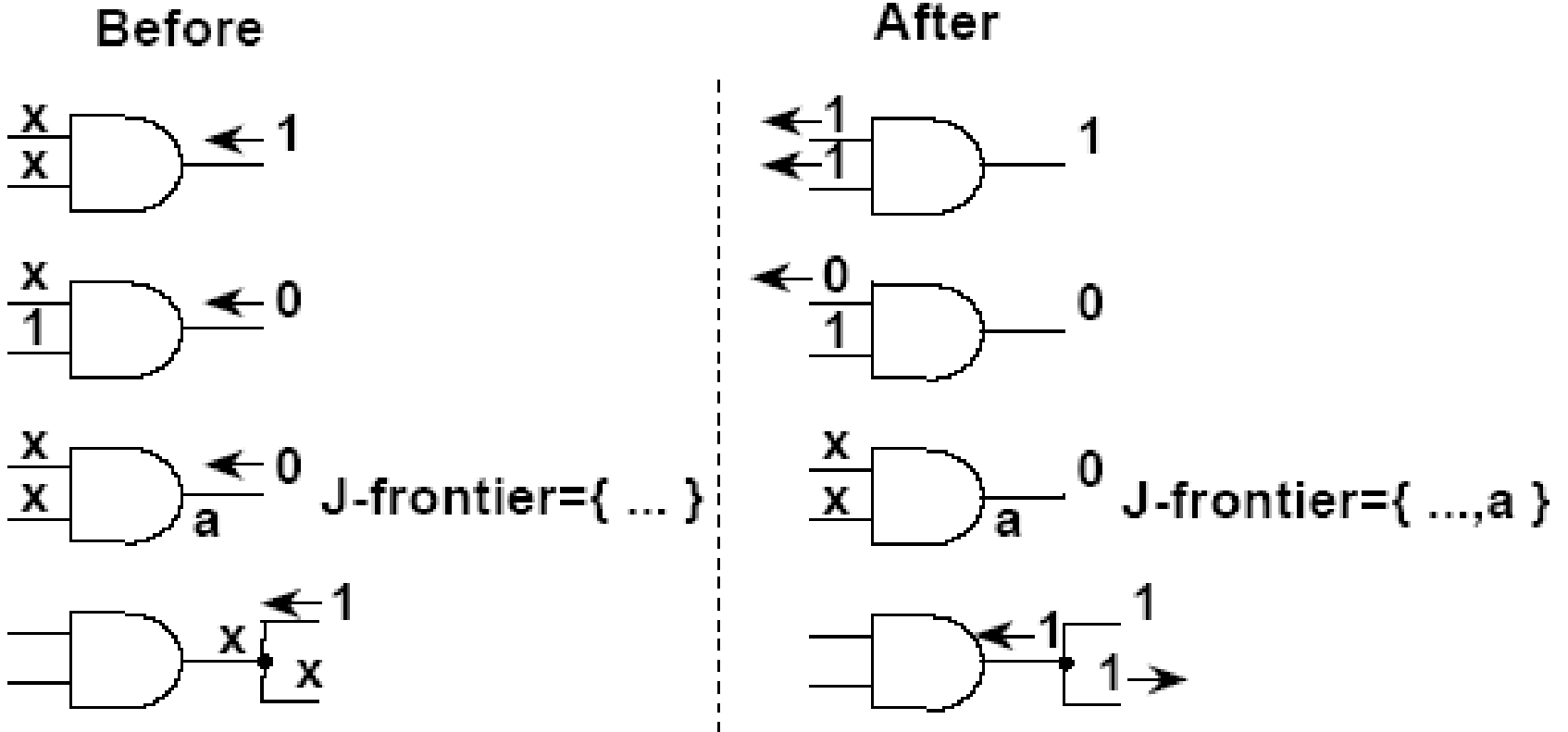


J – Frontier : A set of all gates whose output value is known but not implied by its input value

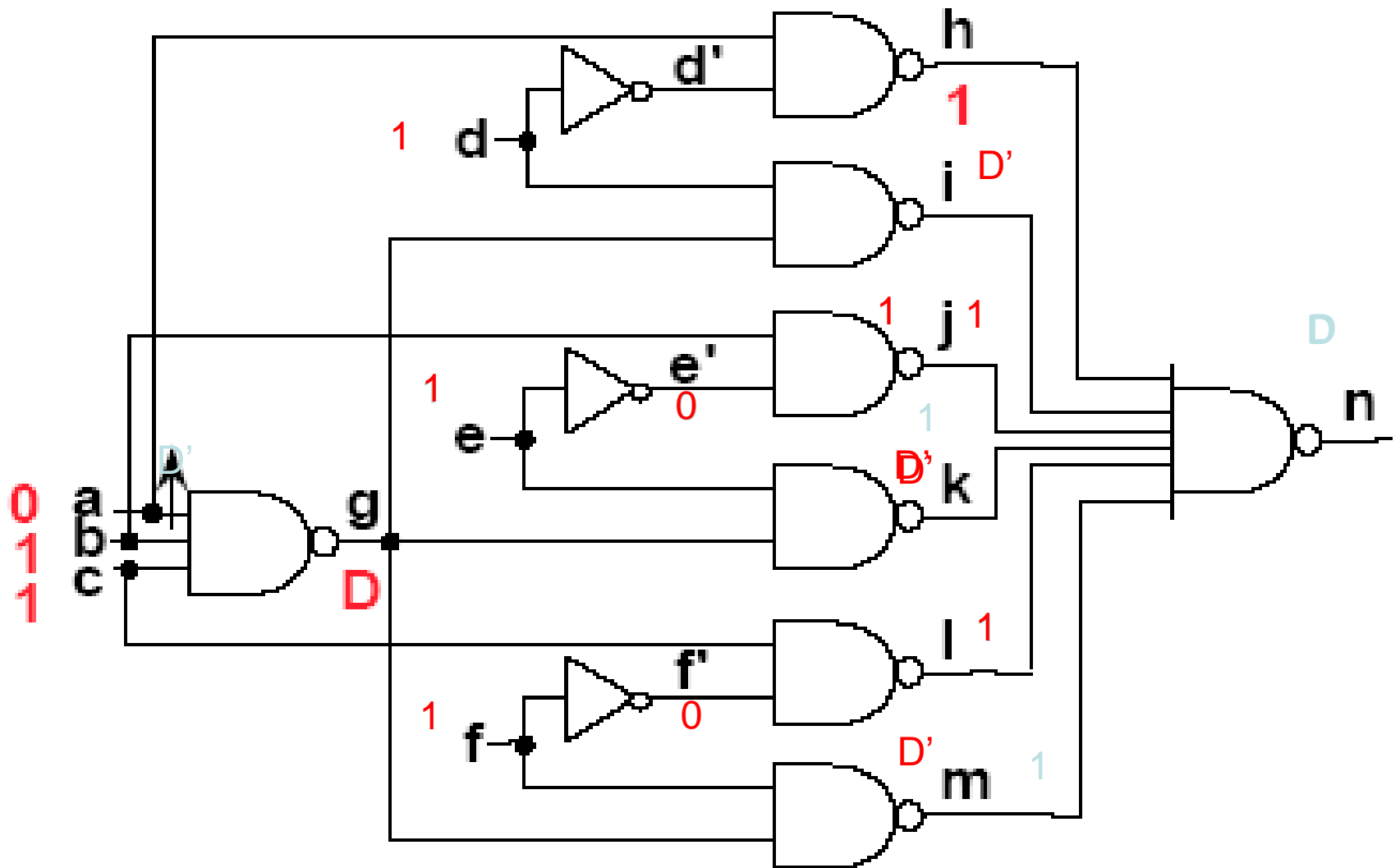
Implications (Forward)



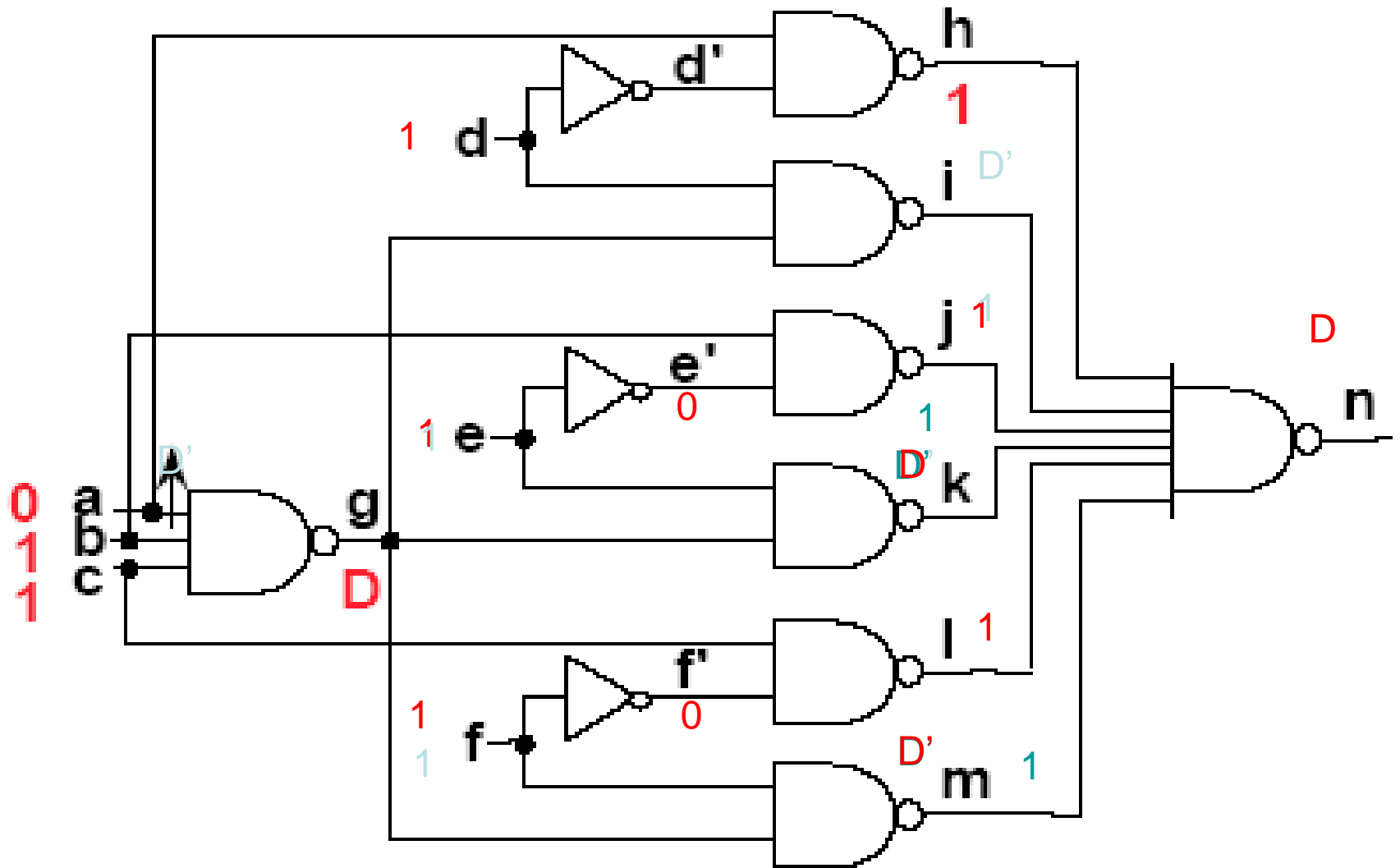
Implications (Backward)



D-Algorithm : Example



D-Algorithm : Example

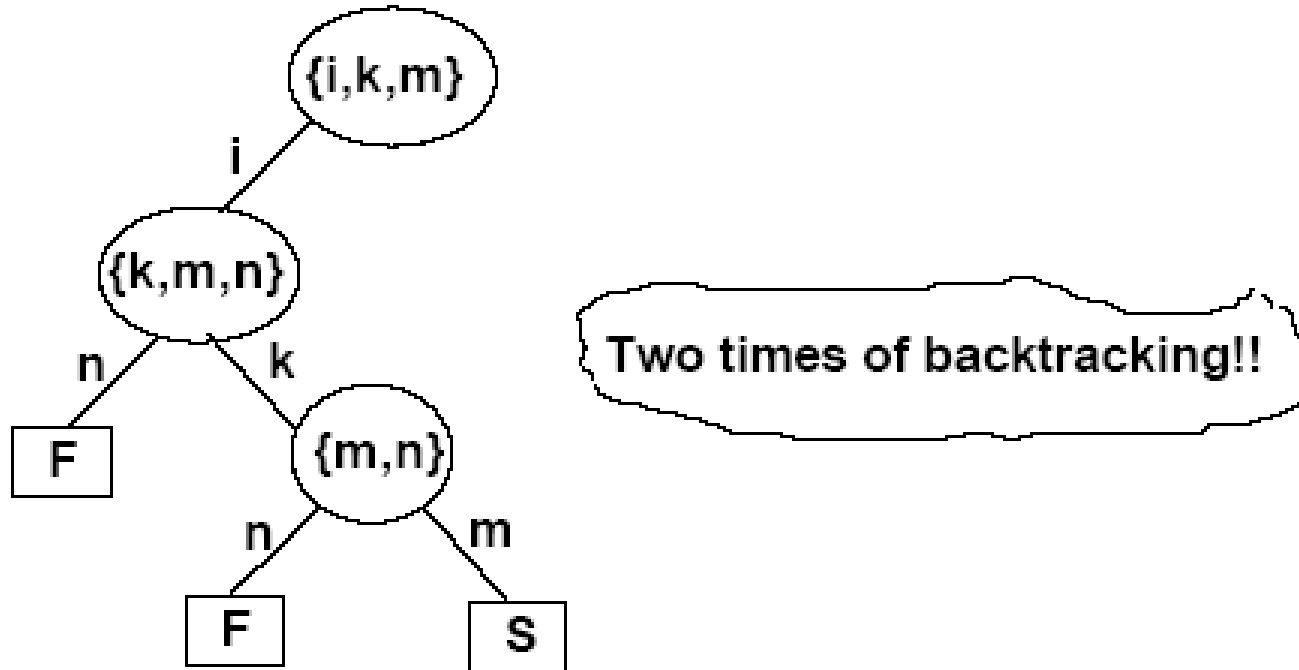


Value Computation

Decision	Implication	Comments
	a=0 h=1 b=1 c=1 g=D	Active the fault Unique D-drive
d=1	i=D d?0	Propagate via i
j=1 k=1 l=1 m=1	n=D e?0 e=1 k=D	Propagate via n Contradiction

e=1	k=D e?0 j=1	Propagate via k
l=1 m=1	n=D f?0 f=1 m=D	Propagate via n Contradiction
f=1	m=D f?0 l=1 n=D	Propagate via m

Decision Tree



Thank You

