1. [20 points] For the $16-\mathrm{QAM}$ constellation shown below calculate $E_{b}$ in terms of $A$. Assume that the transmitted symbol is corrupted by adding $N \sim \mathcal{C N}\left(0, N_{0}\right)$. If all the constellation points are equally likely to be transmitted, calculate the following in terms of $E_{b}$ and $N_{0}$.
(a) The exact error probability of the optimal decision rule.
(b) The union bound on the exact error probability.
(c) The intelligent union bound on the exact error probability.
(d) The nearest neighbor approximation of the exact error probability.

