

1 Lecture Plan

- Define CCA-security
- Describe the padding oracle attack

2 Chosen-Ciphertext Attack Security

- Previously, we considered ciphertext-only attacks and chosen-plaintext attacks. Known-plaintext attacks are weaker than chosen-plaintext attacks, so an encryption scheme which is CPA-secure will also be KPA-secure.
- We now consider *chosen-ciphertext attacks*. Here, the adversary has access to a decryption oracle $\text{Dec}_k(\cdot)$ which decrypts ciphertexts chosen by the adversary. The adversary is not allowed to send the ciphertext exchanged between the honest parties to the decryption oracle.
- For a formal definition of the CCA threat model, consider the *CCA indistinguishability experiment* $\text{PrivK}_{\mathcal{A},\Pi}^{\text{cca}}(n)$:
 1. A key k is generated by running $\text{Gen}(1^n)$.
 2. The adversary \mathcal{A} is given 1^n and oracle access to $\text{Enc}_k(\cdot)$ and $\text{Dec}_k(\cdot)$. It outputs a pair of messages $m_0, m_1 \in \mathcal{M}$ with $|m_0| = |m_1|$.
 3. A uniform bit $b \in \{0, 1\}$ is chosen. Ciphertext $c \leftarrow \text{Enc}_k(m_b)$ is computed and given to \mathcal{A} . c is called the *challenge ciphertext*.
 4. The adversary \mathcal{A} continues to have oracle access to $\text{Enc}_k(\cdot)$ and $\text{Dec}_k(\cdot)$, but is not allowed to query the latter on the challenge ciphertext itself. Eventually, \mathcal{A} outputs a bit b' .
 5. The output of the experiment is defined to be 1 if $b' = b$, and 0 otherwise. If output is 1, we say that \mathcal{A} succeeds.

Definition. A private-key encryption scheme $\Pi = (\text{Gen}, \text{Enc}, \text{Dec})$ has *indistinguishable encryptions under a chosen-ciphertext attack*, or is **CCA-secure**, if for all probabilistic polynomial-time adversaries \mathcal{A} there is a negligible function negl such that, for all n ,

$$\Pr [\text{PrivK}_{\mathcal{A},\Pi}^{\text{cca}}(n) = 1] \leq \frac{1}{2} + \text{negl}(n).$$

- None of the encryption schemes we have seen so far is CCA-secure. Consider the CPA-secure scheme where $\text{Enc}_k(m) = \langle r, F_k(r) \oplus m \rangle$. Consider the following adversary \mathcal{A} in the CCA indistinguishability experiment.

1. \mathcal{A} chooses $m_0 = 0^n$ and $m_1 = 1^n$.
2. Upon receiving the challenge ciphertext $c = \langle r, s \rangle = \langle r, F_k(r) \oplus m_b \rangle$, \mathcal{A} asks for the decryption of $c' = \langle r, s' \rangle = \langle r, s \oplus 10^{n-1} \rangle$ i.e. the bit $n + 1$ in c is flipped.
3. The oracle answers with $m' = s' \oplus F_k(r) = F_k(r) \oplus m_b \oplus 10^{n-1} \oplus F_k(r) = m_b \oplus 10^{n-1}$.
4. m' is 10^{n-1} if $b = 0$ and 01^{n-1} if $b = 1$. So the adversary succeeds with probability 1.

3 Padding Oracle Attack

- Do chosen-ciphertext attacks model any real-world attack? The answer is yes. Padding oracle attacks are one such example.
- Recall the CBC block cipher mode used encrypt plaintext whose length is longer than the block length of a block cipher.
 - Let $m = m_1, m_2, \dots, m_l$ where $m_i \in \{0, 1\}^n$.
 - Let F be a length-preserving block cipher with block length n .
 - A uniform *initialization vector* (IV) of length n is first chosen.
 - $c_0 = IV$. For $i = 1, \dots, l$, $c_i := F_k(c_{i-1} \oplus m_i)$.
 - For $i = 1, 2, \dots, l$, $m_i := F_k^{-1}(c_i) \oplus c_{i-1}$.
- The above scheme assumes that the plaintext length is a multiple of n . The plaintext is usually *padded* to satisfy this constraint. For convenience we will refer to the original plaintext as the *message* and the result after padding as the *encoded data*.
- A popular padding scheme is the PKCS #7 padding.
 - Assume that the original message m has an integral number of bytes. Let L be the blocklength of the block cipher in bytes.
 - Let b denote the number of bytes required to be appended to the original message to make the encoded data have length which is a multiple of L . Here, b is an integer from 1 to L ($b = 0$ is not allowed).
 - We append to the message the integer b (represented in 1 byte) repeated b times. For example, if 4 bytes are needed then the `0x04040404` is appended. Note that L needs to be less than 256. Also, if the message length is already a multiple of L , then L bytes need to be appended each of which is equal to L .
- The encoded data is encrypted using CBC mode. When decrypting, the receiver first applies CBC mode decryption and then checks that the encoded data is correctly padded. The value b of the last byte is read and then the final b bytes of the encoded data is checked to be equal to b .
- If the padding is incorrect, the standard procedure is to return a “bad padding” error. The presence of such an error message provides the an adversary with a *partial* decryption oracle. While this may seem like meaningless information, it enables the adversary *to completely recover the original message for any ciphertext of its choice*.
- See pages 99–100 for a complete description of the attack.
- One solution is to use message authentication codes.

4 References and Additional Reading

- Section 3.7 from Katz/Lindell