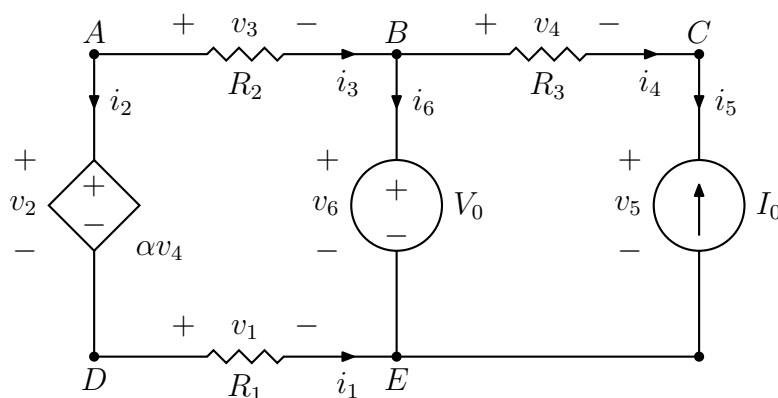


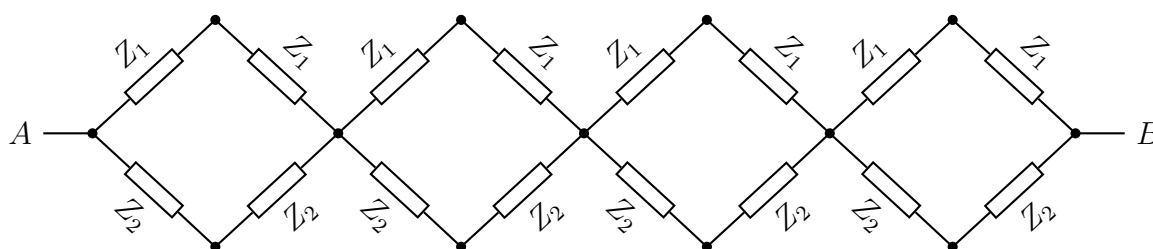
**Question 1)** Consider the circuit shown below. There are 6 components in this circuit other than wires (make sure you can count each of them). Each component is marked with a current and a voltage value, both represented by the same subscript. For example, current  $i_3$  makes a voltage drop of  $v_3$  across the resistor, as shown.

a) Write the current equations for each of the nodes  $A, \dots, E$  using Kirchhoff's current law (KCL). Denoting the currents as a column vector,  $\vec{i} = [i_1, i_2, i_3, i_4, i_5, i_6]^T$ , write KCL equations in matrix form. i.e. find  $A$  such that  $A\vec{i} = 0$ .



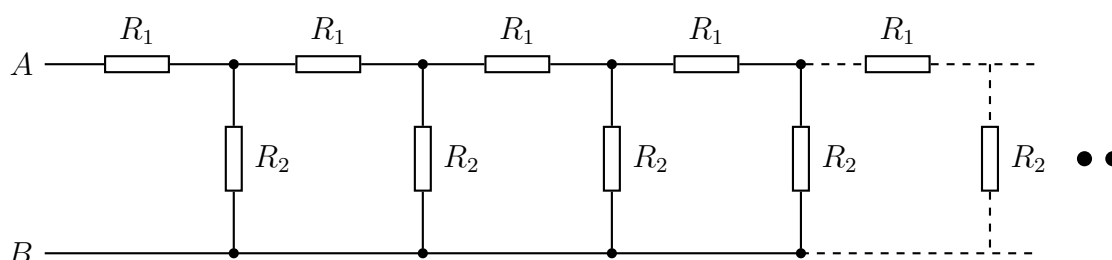
b) Suppose  $V_0 = 10V$  and  $I_0 = 0$ , what is the current flowing through the resistor  $R_1$ . Using this, argue that the component voltages/currents marked in the picture need not be positive or negative.

**Question 2)** Find the equivalent for the following circuit, between terminals  $A$  and  $B$  for various conditions on the **impedance**  $Z_1$  and  $Z_2$ .

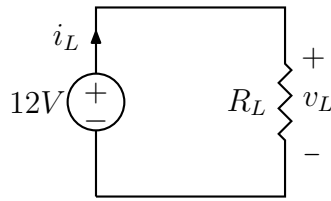


- a) What is the equivalent resistance if  $Z_1 = 1\Omega$  and  $Z_2 = 2\Omega$ .
- b) What is the equivalent inductance if  $Z_1 = 2H$  and  $Z_2 = 4H$ .
- c) What is the equivalent capacitance if  $Z_1 = 1.5F$  and  $Z_2 = 3.0F$ .

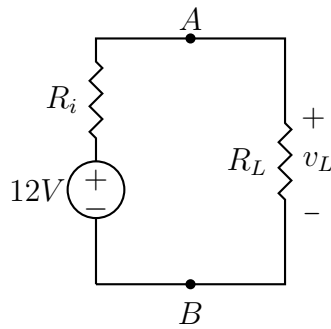
**Question 3)** Find the equivalent resistance of the infinite ladder network shown below.



**Question 4** An ideal voltage source is the one which maintains a fixed voltage across its terminals no matter how much current passes through it. The current supplied can vary, for example, due to a change in load resistance. Let us consider a standard battery, and argue whether it is a voltage source. Consider the model below.



- a) When the load  $R_L$  is  $100\Omega$ , is this battery an ideal voltage source.
- b) Due to some reason, the load is fluctuating between  $100\Omega$  to  $200\Omega$ , is this battery still an ideal voltage source.
- c) Unfortunately life is not that ideal as it looks like, practical batteries have a small internal resistance, and a real circuit looks like,



(Beware that this internal resistance is inherent inside the edge points ( $A$  and  $B$ ) that we can access, and there is no way to physically take it off.) If  $R_i = 10\Omega$ , argue that the above source is not an ideal voltage source when the load varies between  $20\Omega$  and  $100\Omega$ .

- d) When the load resistance is always  $1000\Omega$  and above, can this battery be considered as an ideal voltage source.

**Question 5)** Simplify the following circuits *if possible*. The sources are considered ideal.

