Tornado Cash Using SNARKs for Privacy and Scalability

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Motivation

- Consider the following scenario
 - You have 100 ETH stored in a self-custodial wallet
 - You take your family on a vacation to an exotic country
 - The hotel accepts ETH as a mode of payment
 - You pay the room rent of 1 ETH while checking in
 - The front desk clerk notices that you love your family and that your ETH address has 99 ETH
 - He has friends in the kidnapping industry
- How can you prevent leaking the total amount of ETH you hold?
 - **Option A:** You could store your ETH on an exchange and pay using their interface.
 - You risk losing funds due to exchange hacks
 - Hackers can steal customer data and sell it to their kidnapper friends
 - **Option B:** You could send 1 ETH to a fresh address from your 100 ETH address and use that to pay the room rent
 - Now suppose you decide to extend your stay
 - You make another 1 ETH transfer from your main ETH address
 - The clerk can now infer that you control a large amount of ETH
- Tornado Cash is a better Option B
 - It is a smart contract on Ethereum which implements a mixer

Tornado Cash Overview

Pre-Nova Version



- Desired functionality
 - Soundness
 - Only past depositors should be able to withdraw
 - No double withdrawal (only one withdrawal per deposit)
 - Privacy: A withdrawal should not be linkable to a particular past deposit

Deposit Workflow (1/2)

Choose amount and chain

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Deposit Workflow (2/2)

Connect wallet, save note, and deposit



Deposit Steps (1/2)

Anatomy of a Tornado Cash private note



- The 62 bytes in the nullifier and secret are randomly generated on the user's computer
- A **commitment** (Pedersen hash of the 62 bytes) is calculated and submitted to the contract

Pedersen hash of bitstring $b_1 b_2 \dots b_n = g_1^{b_1} g_2^{b_2} \dots g_n^{b_n}$.

• Contract checks that _commitment has not been seen before
 mapping(bytes32 => bool) public commitments;
 // <snip>
 require(!commitments[commitment], "The commitment has been submitted");

Deposit Steps (2/2)

- Contract inserts __commitment into a Merkle tree uint32 insertedIndex = _insert(_commitment);
 - Tree has 20 levels
 - insertedIndex is the index of new leaf



- No leaf deletions allowed Maximum of 2²⁰ deposits
- Stores the fact that _commitment has been seen commitments[_commitment] = true;
- Checks that ETH being sent equals contract denomination

require(msg.value == denomination, "Please send 1 ETH with transaction");

Emits an event

emit Deposit(_commitment, insertedIndex, block.timestamp);

Withdrawal Workflow (1/3)

Enter note string and recipient address

A https://app.tornado.cash			☆
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Deposit	Withdraw	Statistics IETH	
Note 🛓 1167d7af3e1ba93af14b77de3b6d4 Amount	2ab375e0ea19f4	Anonymity set s 4087 equal user deposi: Latest deposits	
Time passed Subsequent deposits	2 hours 3 deposits	4087. an hour ago	4082.11 hours ago
Recipient Address 0x3081b6978f7374e6427Db8b78dA	Donate 2985b6C5D6483	4085. an hour ago 4084. 2 hours ago 4083. 5 hours ago	4080. a day ago 4079. a day ago 4078. a day ago
Total Gas Price Network fee	4 Gwei 0 0022 cFTH		Your IP 103.21.127.60, Mumbai, IN
Relayer fee Total fee	0.008099 ETH 0.002299 ETH		
Tokens to receive Withdraw	0.997701 ETH		
eth-1.tornadocash.eth			

Withdrawal Workflow (2/3)

Choose relayer

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O tornado Airdrop M			
	Withdrawal settings		
	Relayer	Wallet	
	Relayer		
	goerli-v2.tornadosolu		
	Relayer fee	0.1%	
	Relayer status: OK		
	Total		
	Gas Price	4 Gwei	
	Network fee	0.0022 gETH	
	Relayer fee	0.001 ETH	
	Tokens to receive	0.9968 ETH	
	Reset	Save	

Withdrawal Workflow (2/3)

Choose relayer

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Withdrawal Workflow (2/3)

Choose wallet if you have an unlinkable address with ETH

https://app.tornado.cash				☆
tornado Airdrop Mi				
	Withdrawal settings			
	Relayer	Wallet		
	Make sure that gETH used to pay for the gas fee is not linkable to ANY of your			
	addresses. Otherwise, th withdrawal will be compr	ne anonymity of the comised. We recommend		
	using a Relayer instead.			
	Total			
	Tokens to receive	1 ETr		
	Durat	Cours	4079.	
	Reset	Save	4078.	

Withdrawal Workflow (3/3)

Generate proof and confirm withdrawal



Withdrawal Steps (1/2)

- Recall our requirements
 - Soundness
 - Only past depositors should be able to withdraw
 - No double withdrawal (only one withdrawal per deposit)
 - **Privacy**: A withdrawal should not be linkable to a particular past deposit
- The withdraw method is executed

```
function withdraw(
    bytes calldata _proof,
    bytes32 _root,
    bytes32 _nullifierHash,
    address payable _recipient,
    address payable _relayer,
    uint256 _fee
    // <snip>
)
```

• _proof is a SNARK proof for the following statement: I know the secret and nullifier for a commitment which is included in the Merkle tree with root_root. Furthermore, _nullifierHash is the Pedersen hash of the commitment's nullifier.

Withdrawal Steps (2/2)

• Contract checks that _nullifierHash has not been seen before.

```
mapping(bytes32 => bool) public nullifierHashes;
// <snip>
require(!nullifierHashes[_nullifierHash], "Note already spent");
This prevents double withdrawal
```

- Checks that _root is any of the last 100 Merkle roots require (isKnownRoot (_root), "Cannot find your merkle root");
- It then verifies the SNARK proof on-chain

```
require(
   verifier.verifyProof(_proof,
     [uint256(_root), uint256(_nullifierHash), ...]
   ),
   "Invalid withdraw proof"
);
```

- Stores the fact that _nullifierHash has been seen nullifierHashes[_nullifierHash] = true;
- Sends relevant amounts to _recipient and _relayer _recipient.call.value(denomination _fee)(""); _relayer.call.value(_fee)("");
- The SNARK proof also "signs" the _recipient, _relayer, _fee fields to prevent tampering
- The verifier contract is generated using the circom compiler.

withdraw.circom

template Withdraw(levels) {

```
signal input root;
signal input nullifierHash;
signal input recipient; // not taking part in any computations
signal input relayer; // not taking part in any computations
signal input fee; // not taking part in any computations
signal private input nullifier;
signal private input secret;
signal private input settert;
signal private input pathElements[levels];
signal private input pathElments[levels];
```

```
component hasher = CommitmentHasher();
hasher.nullifier <== nullifier;
hasher.secret <== secret;
hasher.nullifierHash === nullifierHash;
```

```
component tree = MerkleTreeChecker(levels);
tree.leaf <== hasher.commitment;
tree.root <== root;
for (var i = 0; i < levels; i++) {
tree.pathElements[i] <== pathElements[i];
}
}
```

```
// Add hidden signals to make sure that tampering with recipient or fee will invalidate the snark proof
// Most likely it is not required, but it's better to stay on the safe side and it only takes 2 constraints
signal recipientSquare;
signal relayerSquare;
signal relayerSquare;
recipientSquare <== recipient * recipient;
feeSquare <== fee * fee;
relayerSquare <== relayer * relayer;</pre>
```

OFAC Sanctions

- On Aug 8, 2022, the US Office of Foreign Assets Control placed Tornado Cash addresses on a sanction list
- US residents/businesses cannot interact with entities on the list
- Allegations include facilitating money laundering by ransomware operators and smart contract attackers
- Github removed source repos and three contributors had Github accounts suspended
- Due to the efforts of Prof. Matthew Green and EFF, OFAC allowed use of code for educational purposes
- Github repositories and accounts restored in 2023
- Developer Alexey Pertsev arrested in Netherlands in Aug 2022; released on bail in April 2023
- Developer Roman Storm arrested in US on Aug 23, 2023 and later released on bail
- Pertsev's trial began on March 26, 2024. Verdict expected on May 14

References

- Tornado Cash App https://tornadoeth.cash/
- Tornado Cash Docs https://docs.tornadoeth.cash/
- Circom https://docs.circom.io/
- https://github.com/tornadocash/tornado-core
- EFF article on OFAC sanctions
- EFF update in April 2023