

1. For the 16-QAM constellation shown below calculate  $E_b$  in terms of  $A$ . Assume that the transmitted symbol is corrupted by adding  $N = N_c + jN_s$  where  $N_c$  and  $N_s$  are independent zero-mean Gaussian random variables with variance  $\frac{N_0}{2}$ . If all the constellation points are equally likely to be transmitted, calculate the following in terms of  $E_b$  and  $N_0$ .

- [5 points] The exact error probability of the optimal decision rule.
- [5 points] The union bound on the exact error probability.
- [5 points] The intelligent union bound on the exact error probability.
- [5 points] The nearest neighbor approximation of the exact error probability.

