

Bipolar Junction Transistors: Part 1



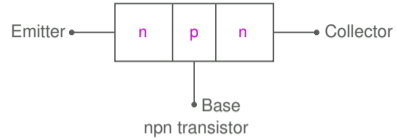
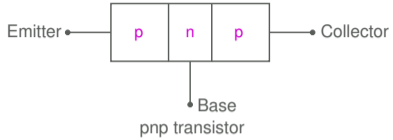
M. B. Patil

mbpatil@ee.iitb.ac.in

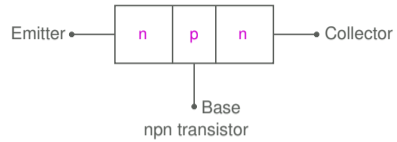
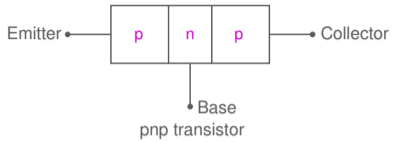
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Department of Electrical Engineering
Indian Institute of Technology Bombay

Bipolar Junction Transistors

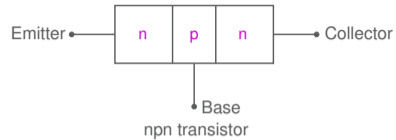
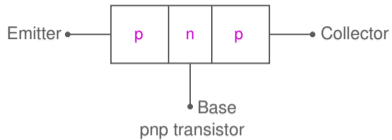


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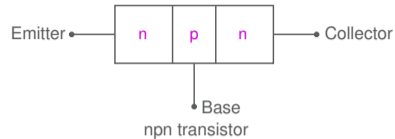
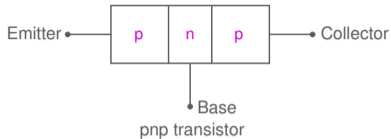
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Bipolar Junction Transistors



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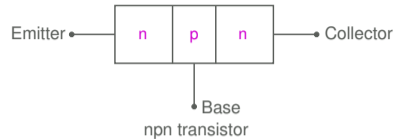
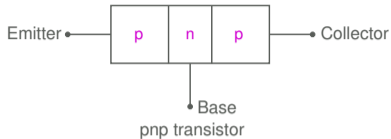


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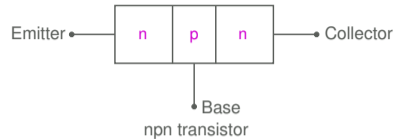
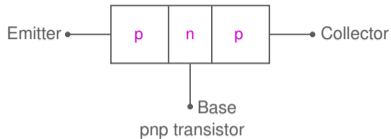
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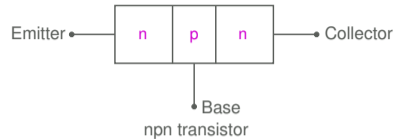
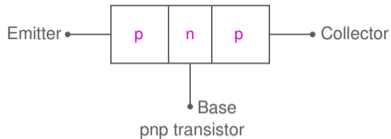
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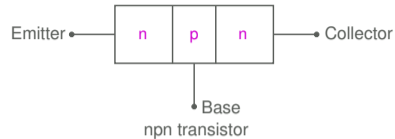
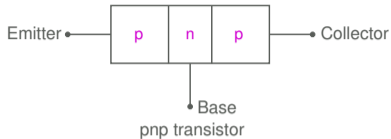
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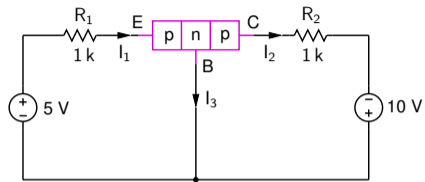
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WRONG! Let us see why.

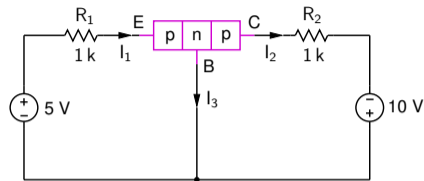
Bipolar Junction Transistors

Consider a *pnp* BJT in the following circuit:

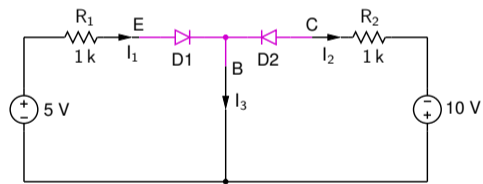


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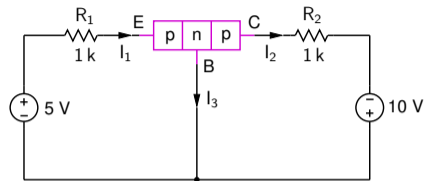


If the transistor is replaced with two diodes connected back-to-back, we get

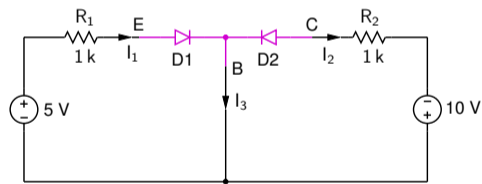


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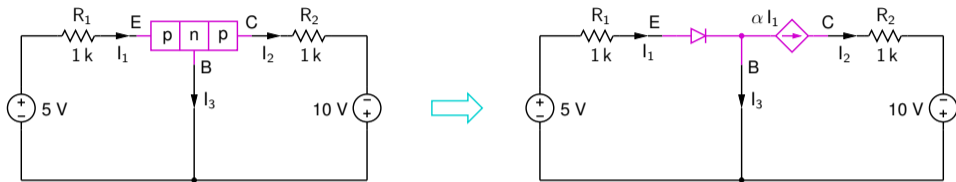
Assuming $V_{on} = 0.7 \text{ V}$ for D1, we get

$$I_1 = \frac{5 \text{ V} - 0.7 \text{ V}}{R_1} = 4.3 \text{ mA},$$

$I_2 = 0$ (since D2 is reverse biased), and $I_3 \approx I_1 = 4.3 \text{ mA}$.

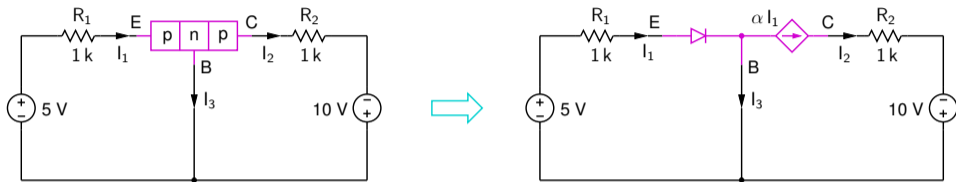
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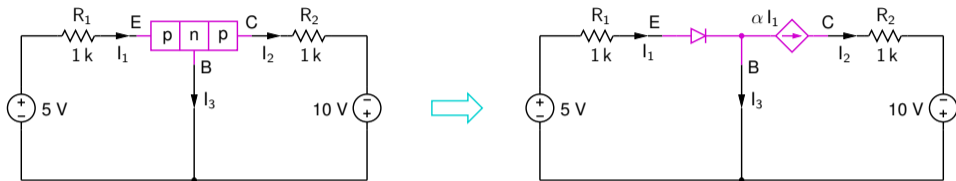


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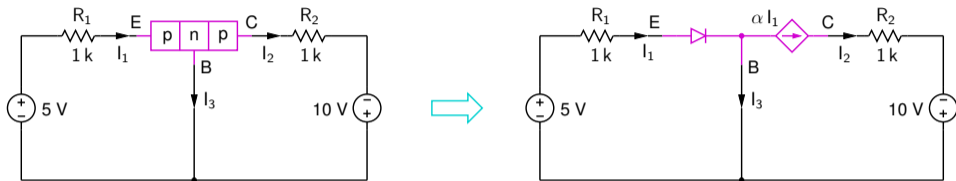
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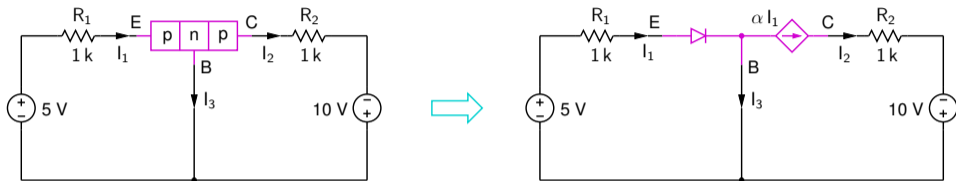
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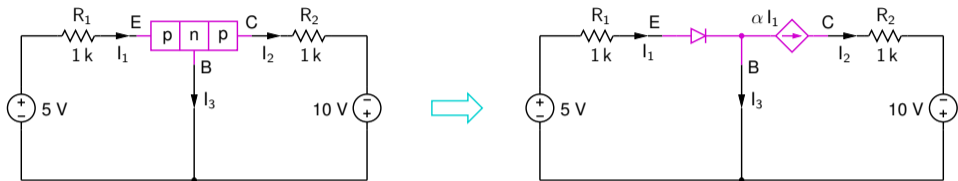
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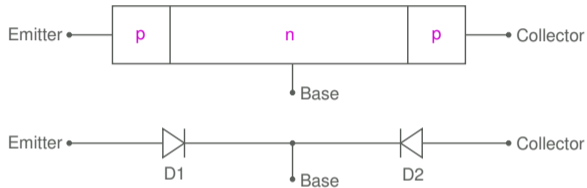
Conclusion: A BJT is NOT the same as two diodes connected back-to-back (although it does have two *p-n* junctions).

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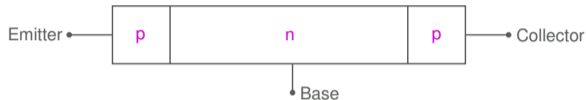
- * When we replace a BJT with two diodes, we assume that there is no interaction between the two diodes, which may be expected if they are “far apart.”



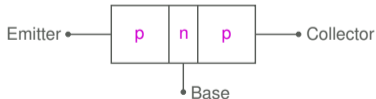
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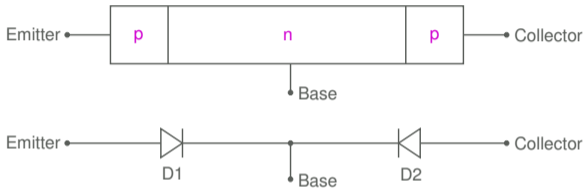
- * However, in a BJT, exactly the opposite is true. For a higher performance, the base region is made as short as possible, and the two diodes cannot be treated as independent devices.



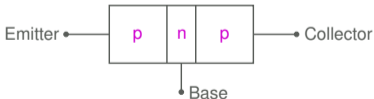
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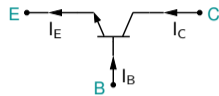
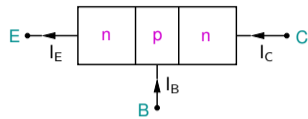
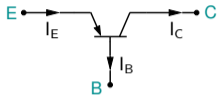
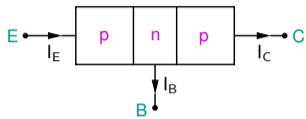


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- * Later, we will look at the “Ebers-Moll model” of a BJT, which is a fairly accurate representation of the transistor action.

BJT in active mode



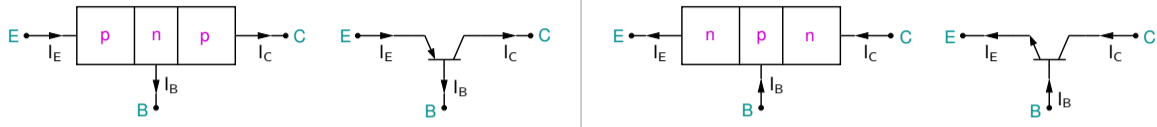
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- * Since the B-E junction is under forward bias, the voltage (magnitude) is typically 0.6 to 0.75 V.
- * The B-C voltage can be several Volts (or even hundreds of Volts), and is limited by the breakdown voltage of the B-C junction.

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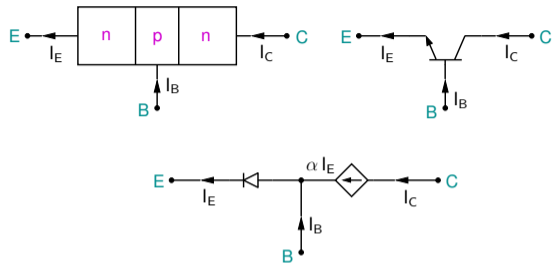
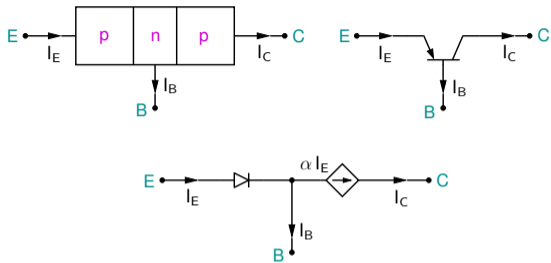
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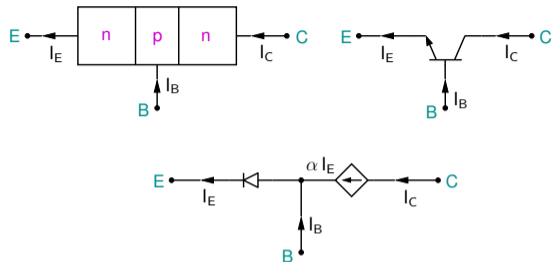
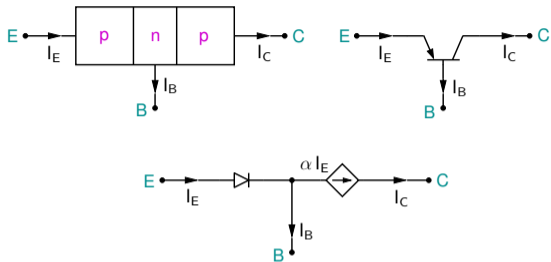


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- * The symbol for a BJT includes an arrow for the emitter terminal, its direction indicating the current direction when the transistor is in active mode.
- * Analog circuits, including amplifiers, are generally designed to ensure that the BJTs are operating in the active mode.

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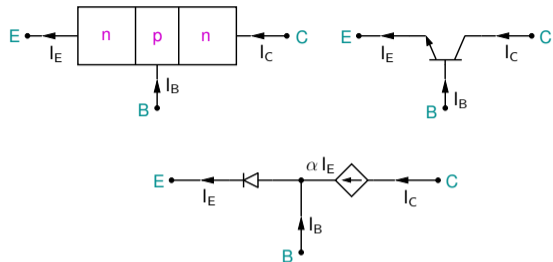
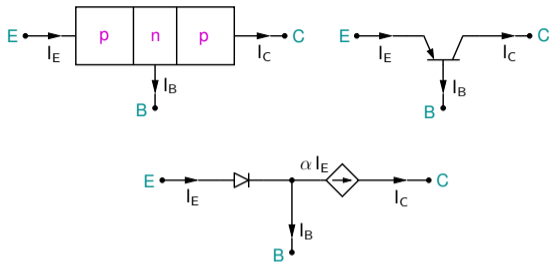


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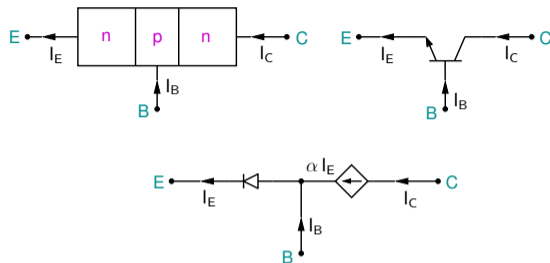
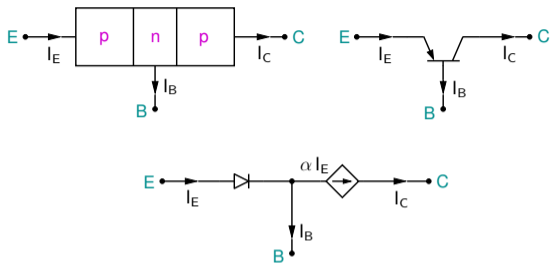
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- * $I_B = I_E - I_C = I_E(1 - \alpha)$.

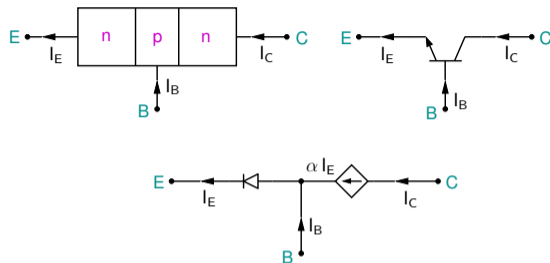
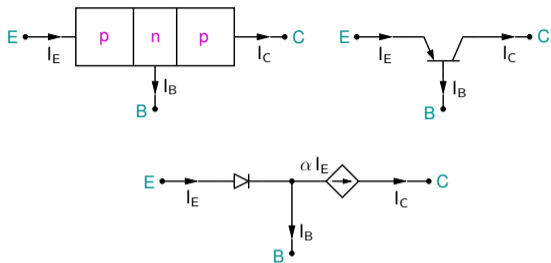
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$$\beta = \frac{I_C}{I_B} = \frac{\alpha}{1 - \alpha}.$$

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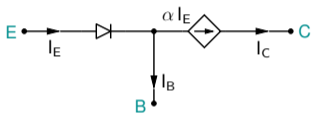
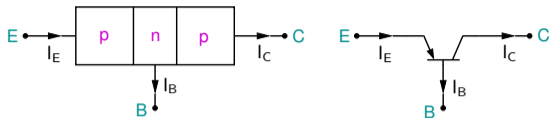


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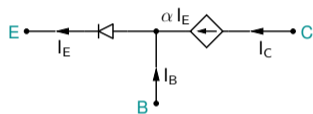
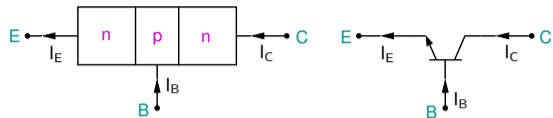
$$\beta = \frac{I_C}{I_B} = \frac{\alpha}{1 - \alpha}.$$

- * β is a function of I_C and temperature. However, we will generally treat it as a constant, a useful approximation to simplify things and still get a good insight.

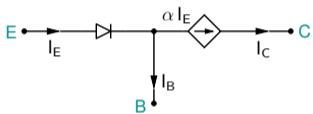
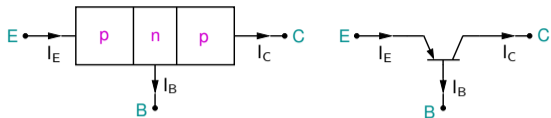
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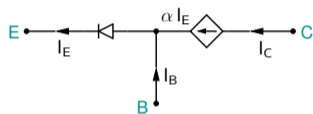
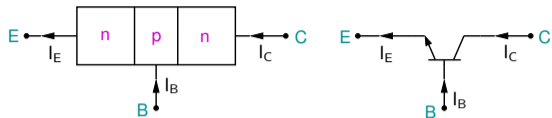


BJT in active mode

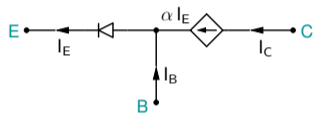
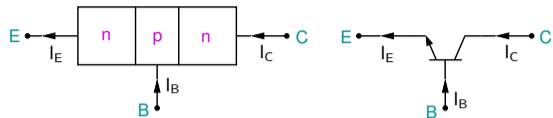
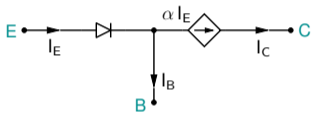
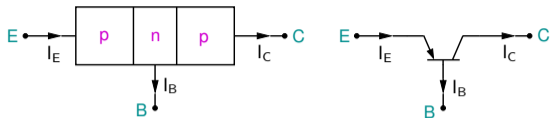


$$\beta = \frac{I_C}{I_B} = \frac{\alpha}{1 - \alpha}$$

α	β
0.9	9
0.95	19
0.99	99
0.995	199



BJT in active mode

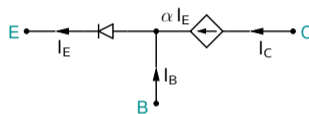
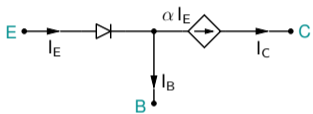
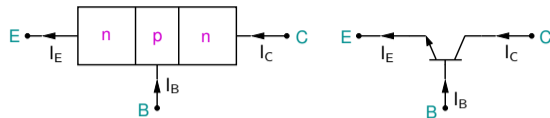
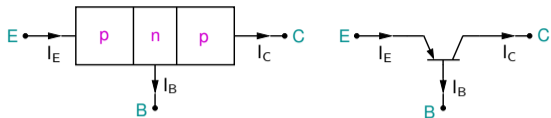


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* β increases substantially as $\alpha \rightarrow 1$.

BJT in active mode

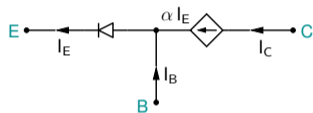
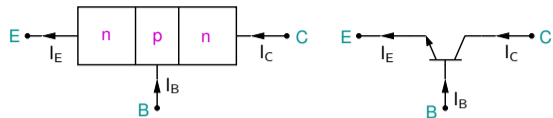
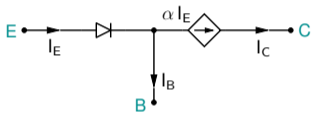
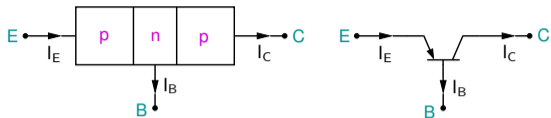


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- * β increases substantially as $\alpha \rightarrow 1$.
- * Transistors are generally designed to get a high value of β (typically 100 to 250, but can be as high as 2000 for "super- β " transistors).

BJT in active mode

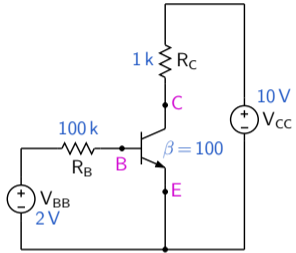


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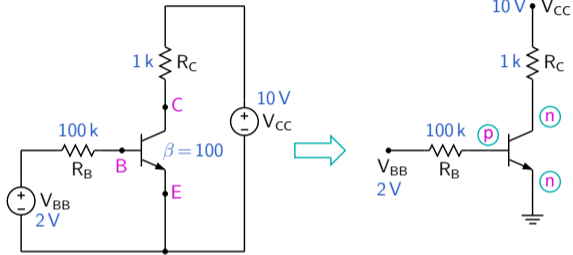
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- * β increases substantially as $\alpha \rightarrow 1$.
- * Transistors are generally designed to get a high value of β (typically 100 to 250, but can be as high as 2000 for "super- β " transistors).
- * A large $\beta \Rightarrow I_B \ll I_C$ or I_E when the transistor is in the active mode.

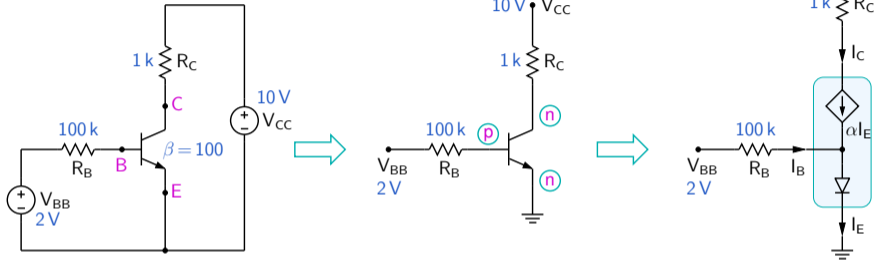
A simple BJT circuit



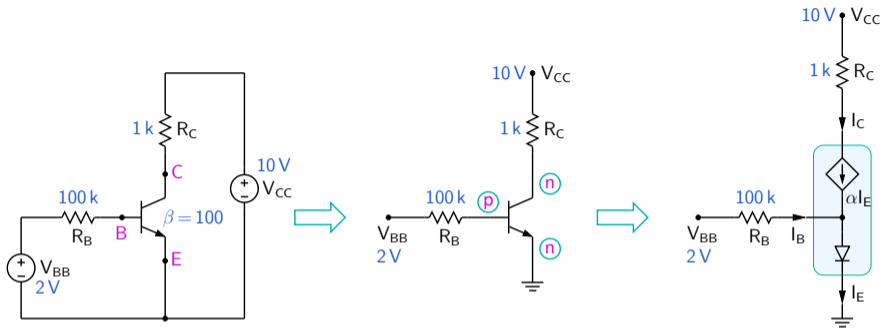
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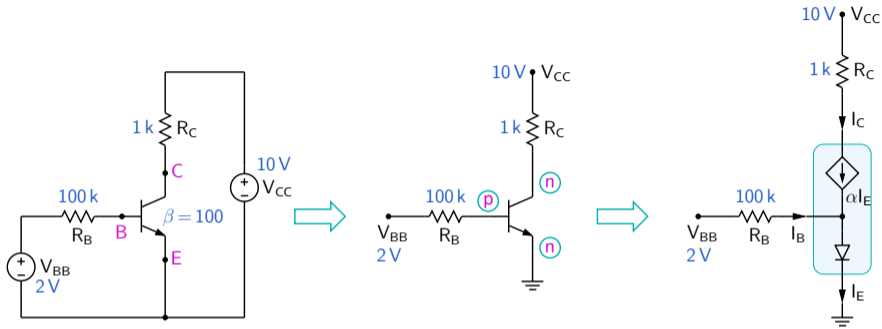


A simple BJT circuit



Assume the BJT to be in the active mode $\Rightarrow V_{BE} = 0.7V$ and $I_C = \alpha I_E = \beta I_B$.

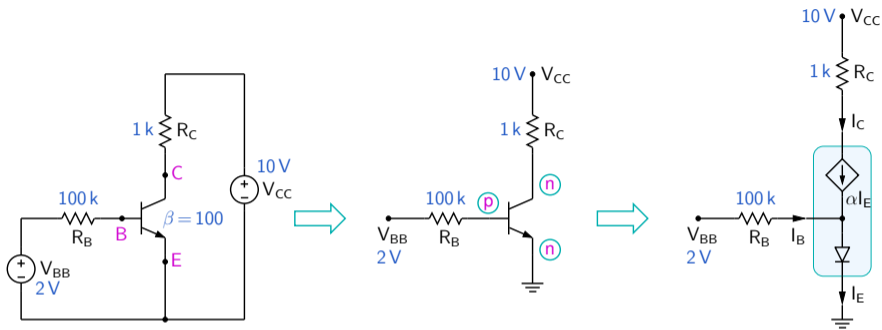
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$$I_B = \frac{V_{BB} - V_{BE}}{R_B} = \frac{2 \text{ V} - 0.7 \text{ V}}{100 \text{ k}} = 13 \mu\text{A}.$$

A simple BJT circuit

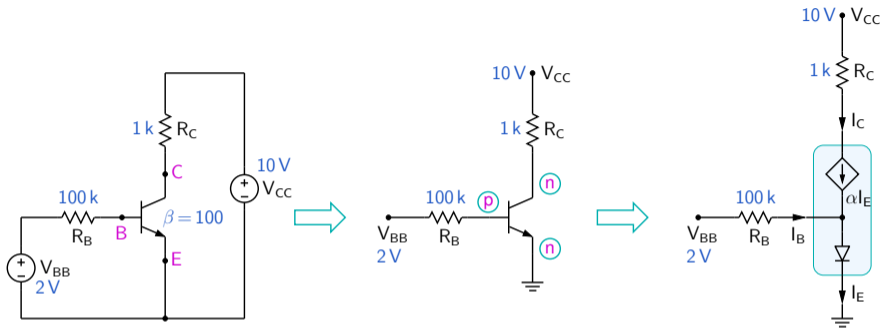


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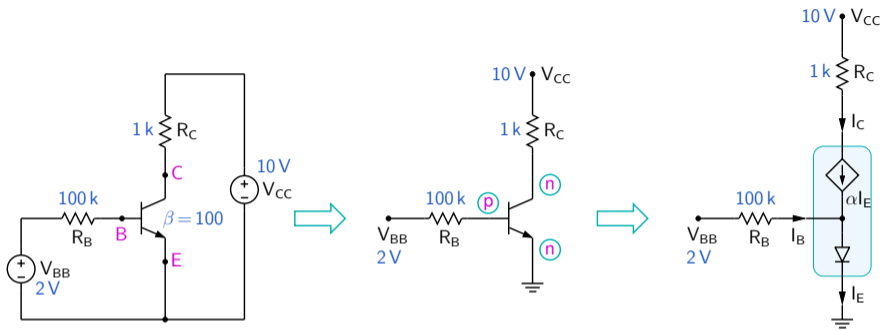
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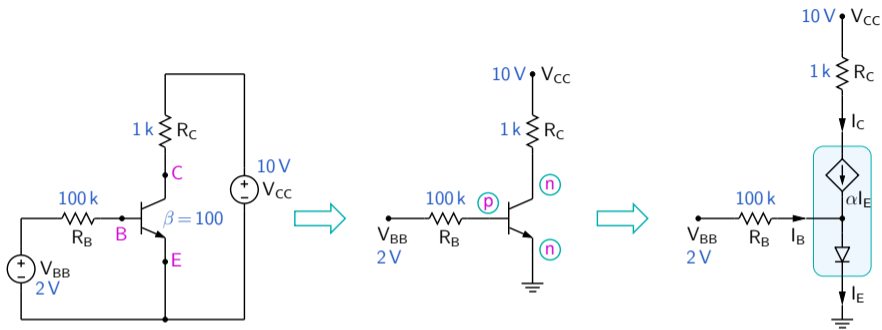
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Let us check whether our assumption of active mode is correct. We need to check whether the B-C junction is under reverse bias.

A simple BJT circuit



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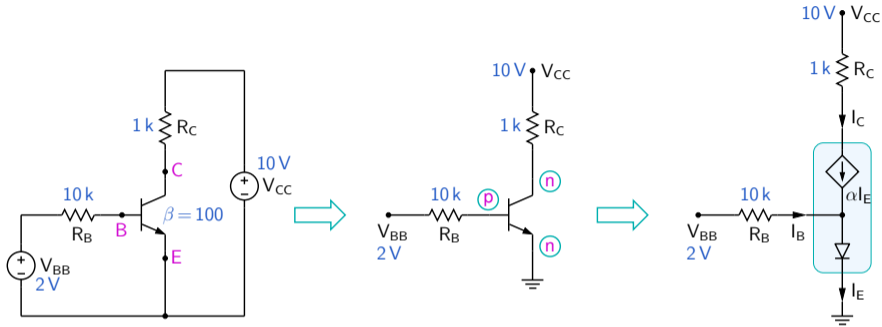
$$V_C = V_{CC} - I_C R_C = 10 \text{ V} - 1.3 \text{ mA} \times 1 \text{ k} = 8.7 \text{ V}.$$

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$$V_{BC} = V_B - V_C = 0.7 \text{ V} - 8.7 \text{ V} = -8.0 \text{ V},$$

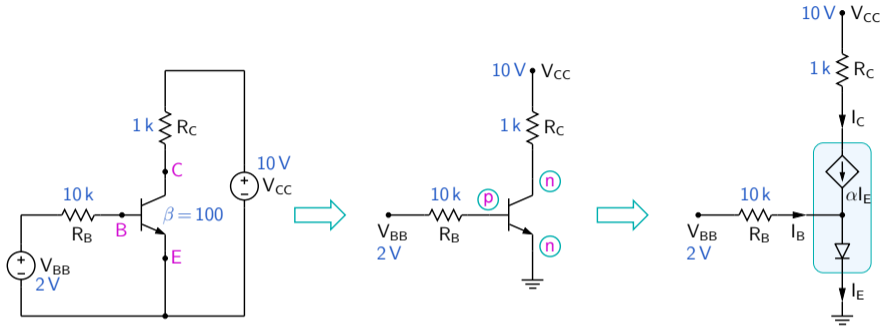
i.e., the B-C junction is indeed under reverse bias.

A simple BJT circuit: continued



What happens if R_B is changed from 100 k to 10 k?

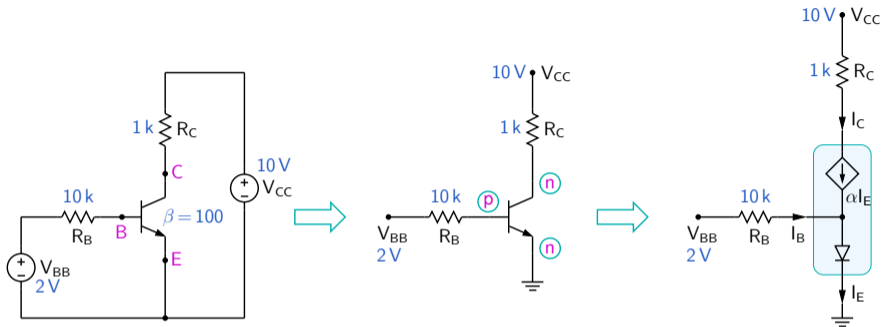
A simple BJT circuit: continued



What happens if R_B is changed from $100k$ to $10k$?

Assuming the BJT to be in the active mode again, we have $V_{BE} \approx 0.7V$, and $I_C = \beta I_B$.

A simple BJT circuit: continued

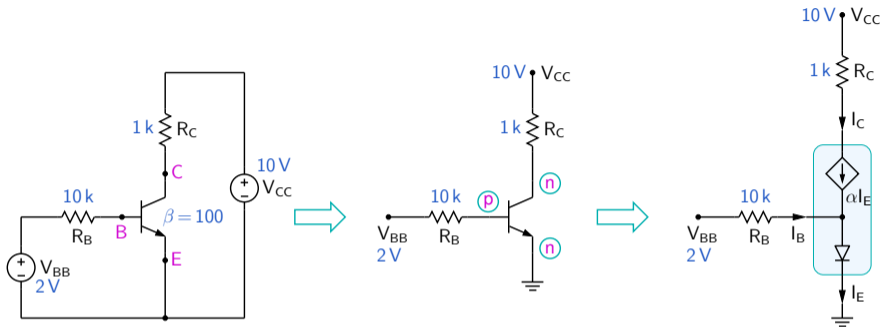


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$$I_B = \frac{V_{BB} - V_{BE}}{R_B} = \frac{2 \text{ V} - 0.7 \text{ V}}{10 \text{ k}} = 130 \mu\text{A}$$

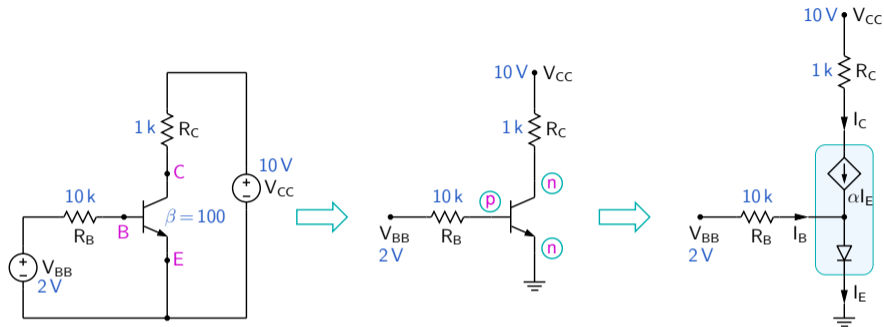
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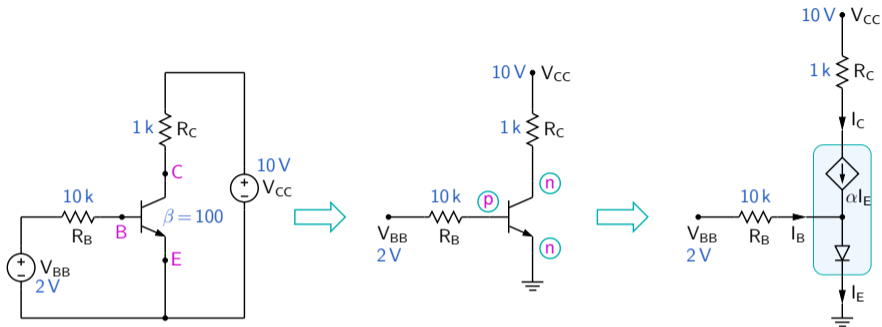


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$$V_C = V_{CC} - I_C R_C = 10\text{ V} - 13\text{ mA} \times 1\text{ k} = -3\text{ V}$$



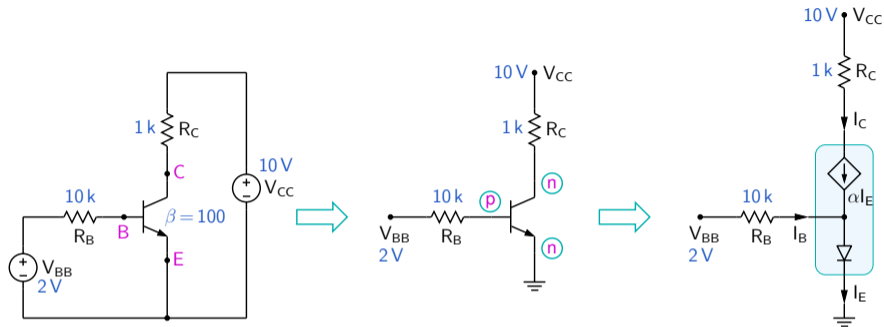
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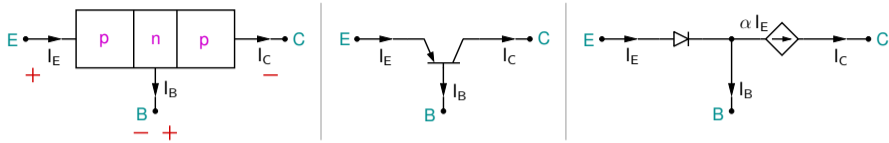
$$\rightarrow V_{BC} = V_B - V_C = 0.7 \text{ V} - (-3) \text{ V} = 3.7 \text{ V}.$$

V_{BC} is not only positive, it is *huge*!

\rightarrow The BJT cannot be in the active mode, and we need to take another look at the circuit.

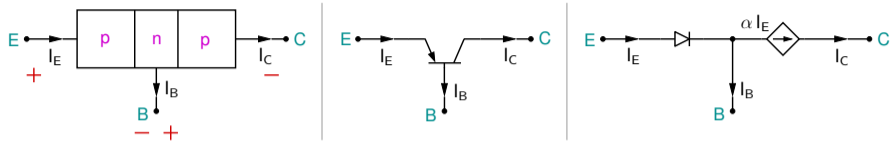
Ebers-Moll model for a *pn*p transistor

Active mode ("forward" active mode): B-E in f.b. B-C in r.b.

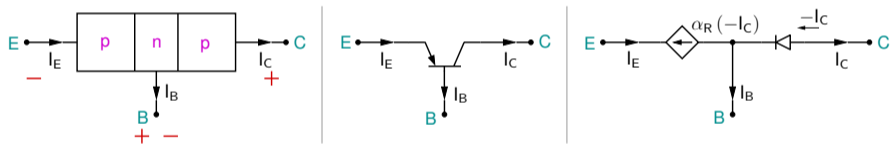


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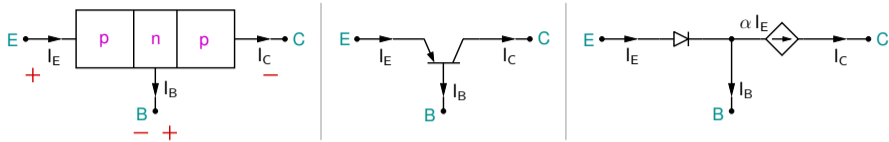


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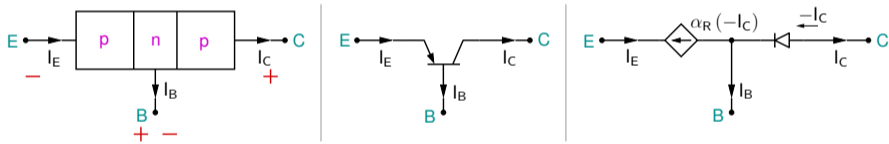


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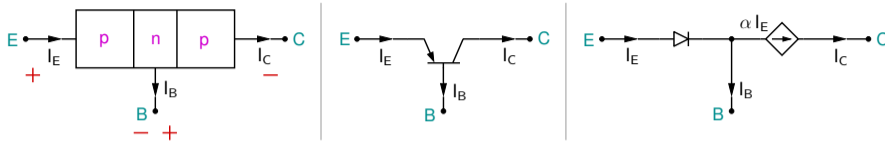
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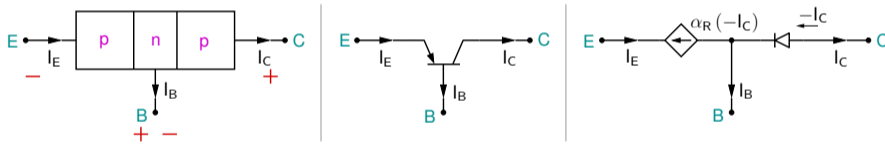
In the reverse active mode, emitter \leftrightarrow collector. (However, we continue to refer to the terminals with their original names.)

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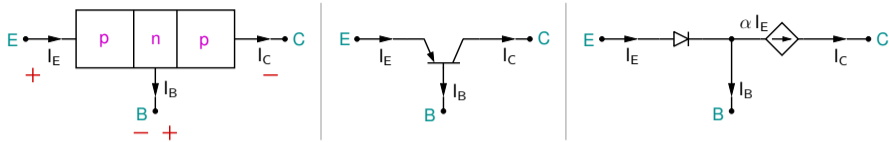


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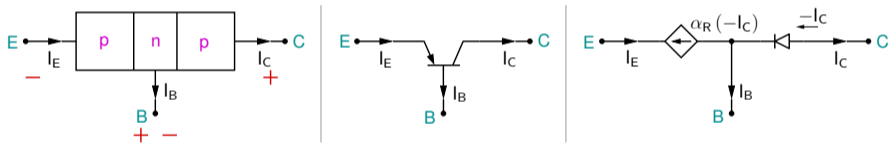
The two α 's, α_F (forward α) and α_R (reverse α) are generally quite different.

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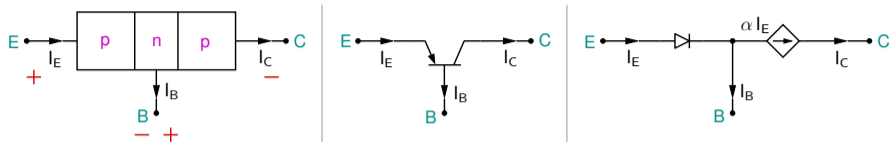
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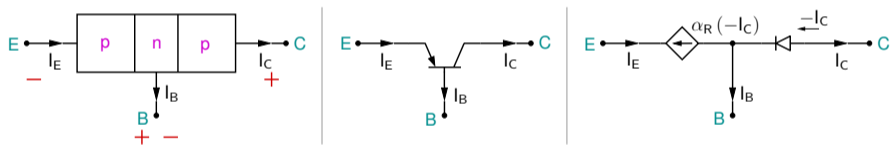
Typically, $\alpha_F > 0.98$, and α_R is in the range from 0.02 to 0.5.

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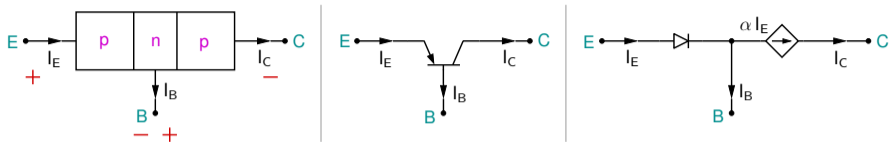
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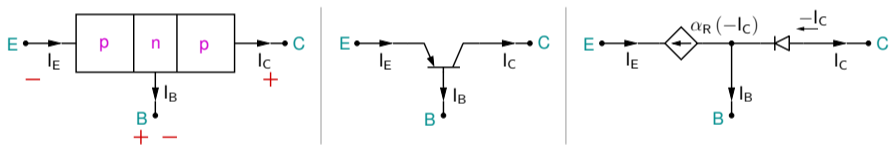
The corresponding current gains (β_F and β_R) differ significantly, since $\beta = \alpha/(1 - \alpha)$.

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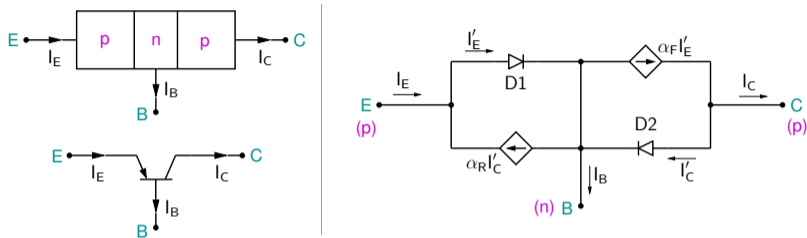
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In amplifiers, the BJT is biased in the forward active mode (simply called the "active mode") in order to make use of the higher value of β in that mode.

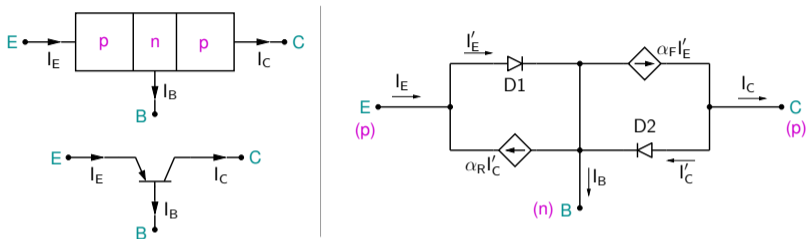
Ebers-Moll model for a *pnp* transistor

The Ebers-Moll model combines the forward and reverse operations of a BJT in a single comprehensive model.



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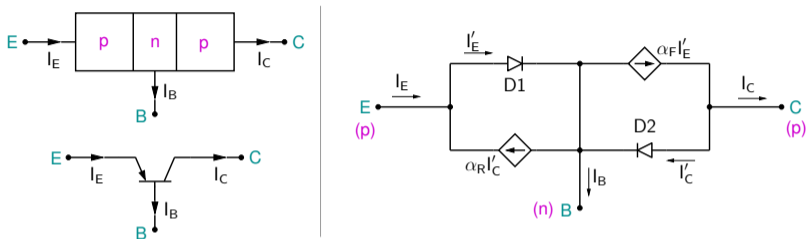


The currents I'_E and I'_C are given by the Shockley diode equation:

$$I'_E = I_{ES} \left[\exp\left(\frac{V_{EB}}{V_T}\right) - 1 \right], \quad I'_C = I_{CS} \left[\exp\left(\frac{V_{CB}}{V_T}\right) - 1 \right].$$

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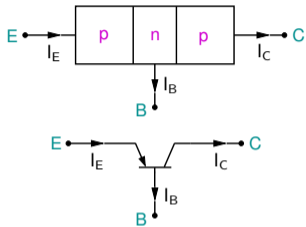


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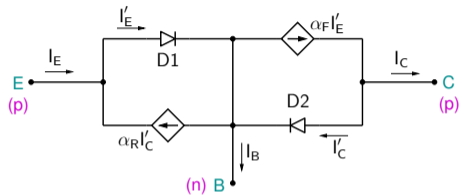
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Mode	B-E	B-C	
Forward active	forward	reverse	$I'_E \gg I'_C$
Reverse active	reverse	forward	$I'_C \gg I'_E$
Saturation	forward	forward	I'_E and I'_C are comparable.
Cut-off	reverse	reverse	I'_E and I'_C are negligblbe.

Ebers-Moll model

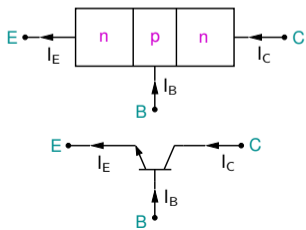


pnp transistor

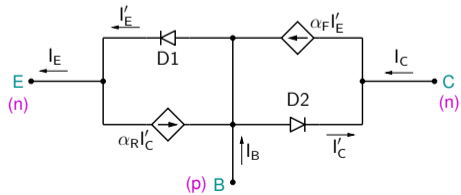


$$I'_E = I_{ES} [\exp(V_{EB}/V_T) - 1]$$

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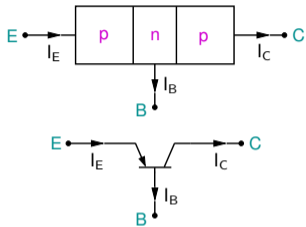


npn transistor

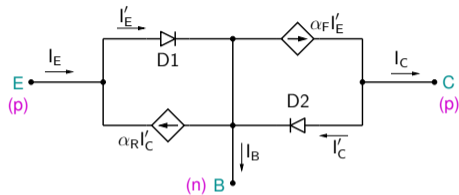


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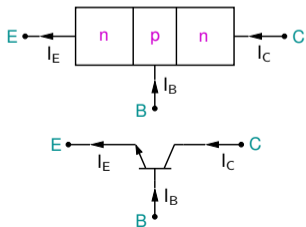


pnp transistor

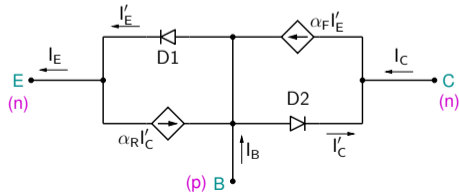


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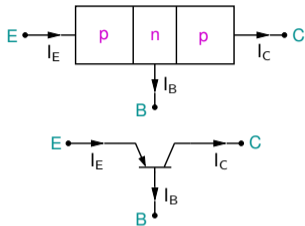
npn transistor



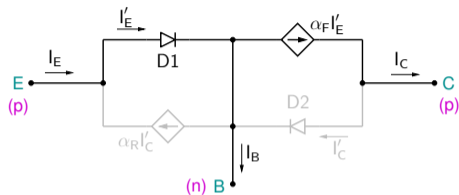
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Ebers-Moll model in active mode



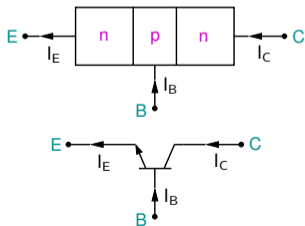
pnp transistor



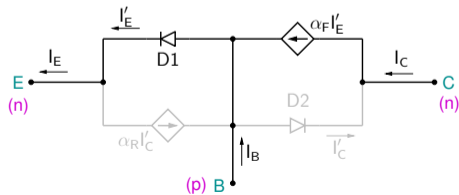
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$$I_C = \alpha_F I_E = \beta_F I_B$$



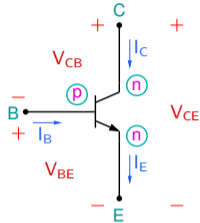
npn transistor

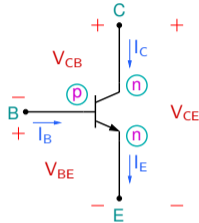


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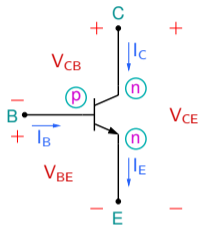
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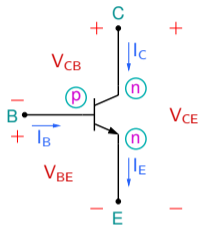




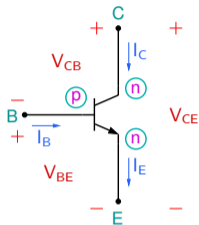
- * Since BJT is a three-terminal device, its behaviour can be described in many different ways, e.g.,



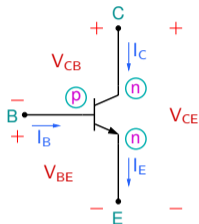
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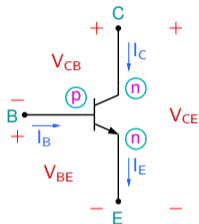
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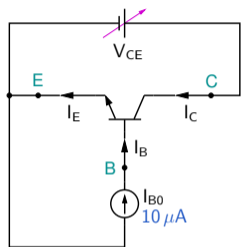


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- * The I - V relationship for a BJT is not a single curve but a “family” of curves or “characteristics.”
- * The I_C - V_{CE} characteristics for different I_B values are useful in understanding amplifier biasing.

BJT I - V characteristics



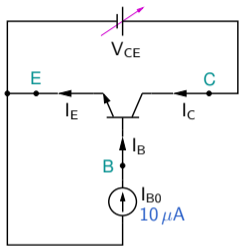
$$\alpha_F = 0.99 \rightarrow \beta_F = \frac{\alpha_F}{1 - \alpha_F} = 99$$

$$\alpha_R = 0.5 \rightarrow \beta_R = \frac{\alpha_R}{1 - \alpha_R} = 1$$

$$I_{ES} = 1 \times 10^{-14} \text{ A}$$

$$I_{CS} = 2 \times 10^{-14} \text{ A}$$

BJT I-V characteristics

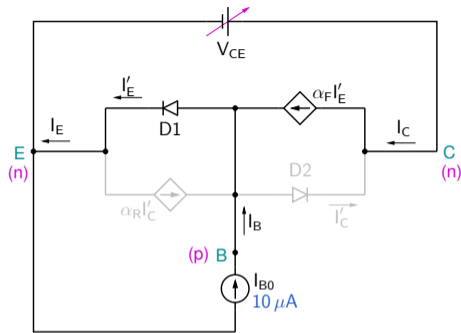


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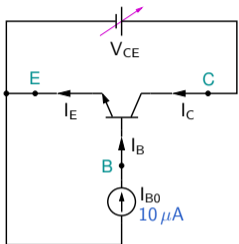


$$I'_E = I_{ES} [\exp(V_{BE}/V_T) - 1]$$

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$$I_C = \alpha_F I_E = \beta_F I_B \text{ in active mode}$$

BJT I - V characteristics

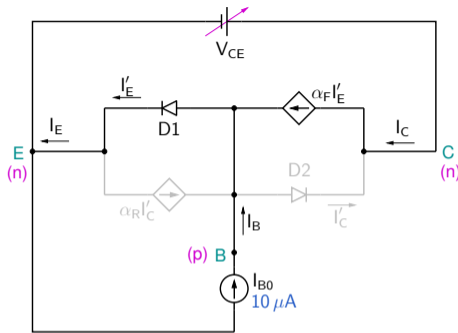


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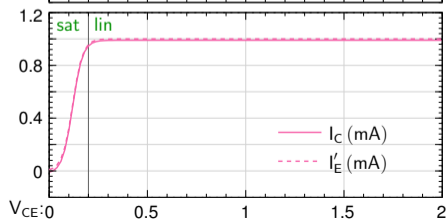
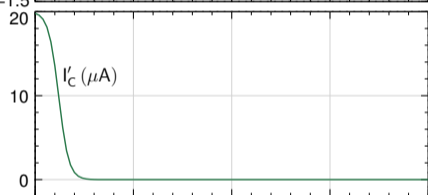
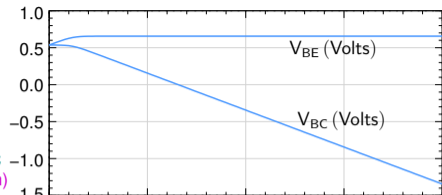
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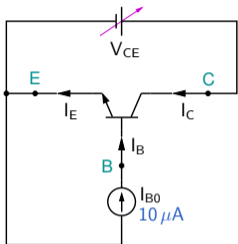
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BJT I-V characteristics

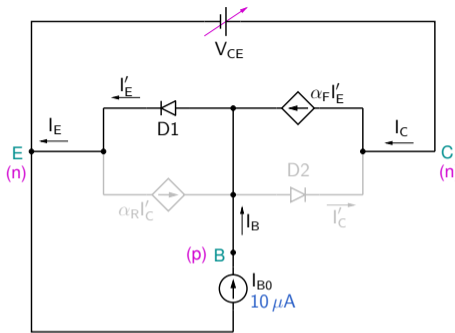


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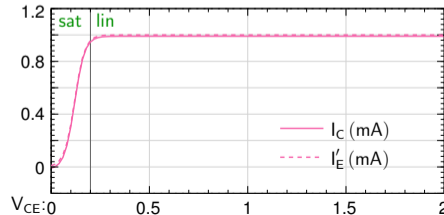
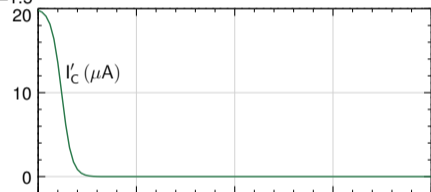
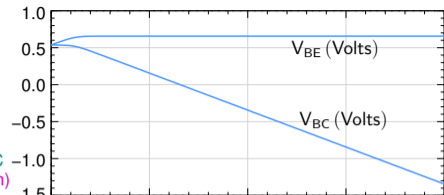
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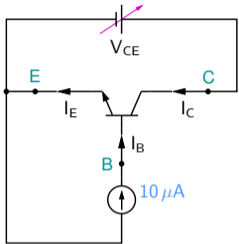
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- * linear region: B-E under forward bias, B-C under reverse bias, $I_C = \beta_F I_B$
- * saturation region: B-E under forward bias, B-C under forward bias, $I_C < \beta_F I_B$

BJT I - V characteristics

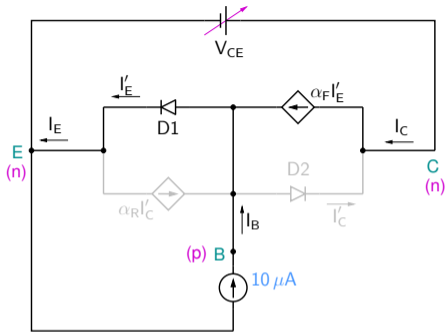


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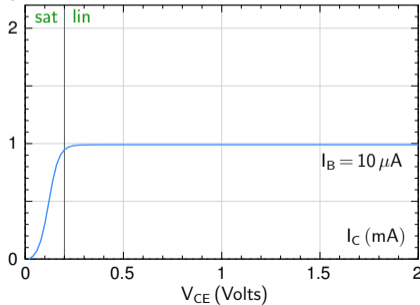
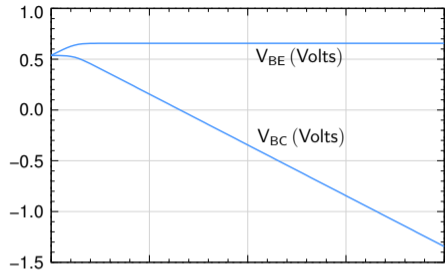
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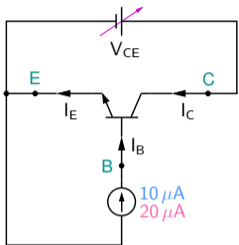
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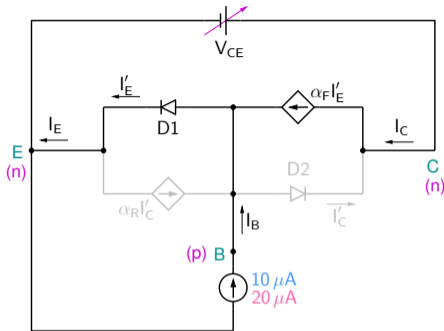


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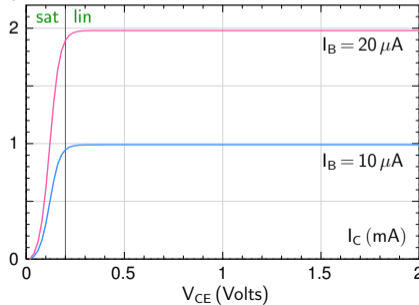
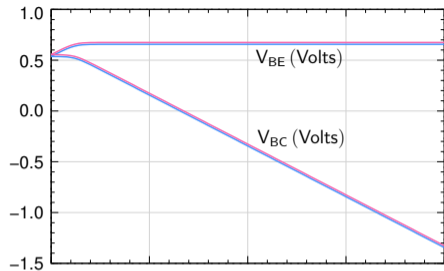
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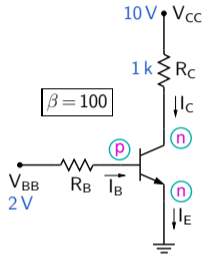
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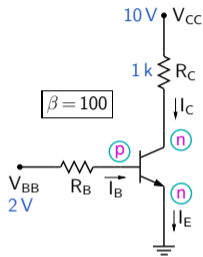
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A simple BJT circuit (revisited)



We are now in a position to explain what happens when R_B is decreased from 100 k to 10 k in the above circuit.

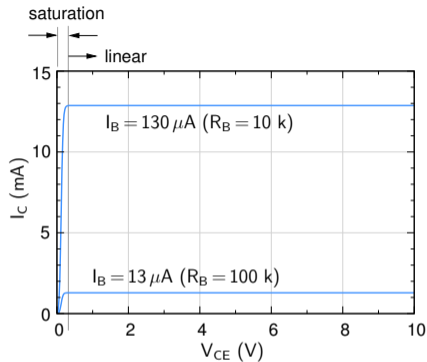
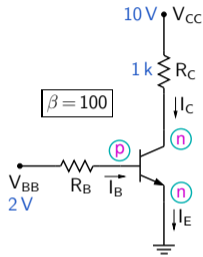
A simple BJT circuit (revisited)



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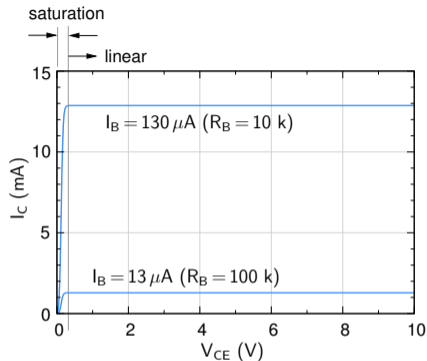
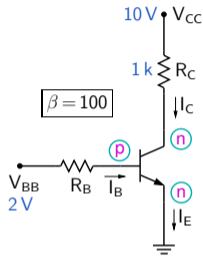
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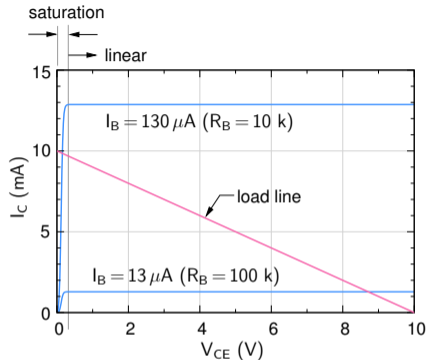
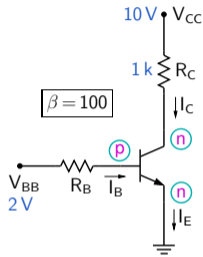


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In addition to the BJT $I_C - V_{CE}$ curve, the circuit variables must also satisfy the constraint, $V_{CC} = V_{CE} + I_C R_C$, a straight line in the $I_C - V_{CE}$ plane.

A simple BJT circuit (revisited)

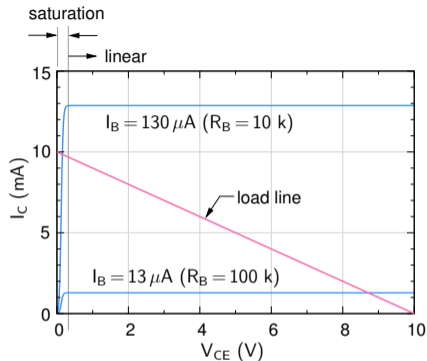
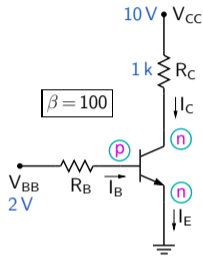


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A simple BJT circuit (revisited)



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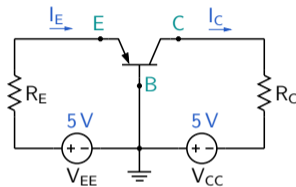
Let us plot $I_C - V_{CE}$ curves for $I_B \approx \frac{V_{BB} - 0.7 V}{R_B}$ for the two values of R_B .

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The intersection of the load line and the BJT characteristics gives the solution for the circuit. For $R_B = 10$ k, note that the BJT operates in the saturation region, leading to $V_{CE} \approx 0.2$ V, and $I_C = 9.8$ mA.

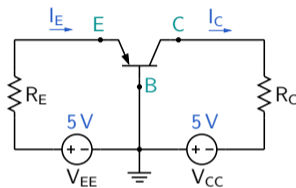
BJT circuit example

Assuming the transistor to be operating in the active region, find R_E and R_C to obtain $I_E = 2 \text{ mA}$, and $V_{BC} = 1 \text{ V}$ ($\alpha \approx 1$).



BJT circuit example

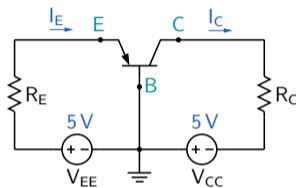
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$$V_{EB} - V_{EE} + I_E R_E = 0$$

BJT circuit example

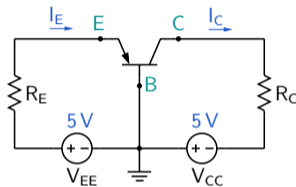
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$$V_{EB} - V_{EE} + I_E R_E = 0 \rightarrow I_E R_E = 5 - 0.7$$

BJT circuit example

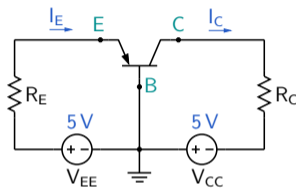
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$$V_{EB} - V_{EE} + I_E R_E = 0 \rightarrow I_E R_E = 5 - 0.7 \rightarrow R_E = \frac{4.3 \text{ V}}{2 \text{ mA}} = 2.15 \text{ k}.$$

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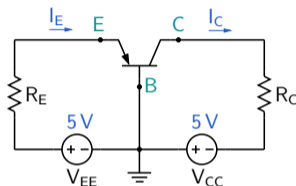


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$$V_{BC} + I_C R_C - V_{CC} = 0$$

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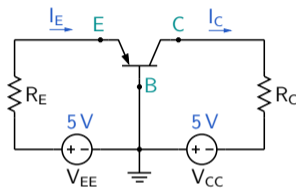


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$$V_{BC} + I_C R_C - V_{CC} = 0 \rightarrow I_C R_C = V_{CC} - V_{BC}.$$

BJT circuit example

Assuming the transistor to be operating in the active region, find R_E and R_C to obtain $I_E = 2 \text{ mA}$, and $V_{BC} = 1 \text{ V}$ ($\alpha \approx 1$).



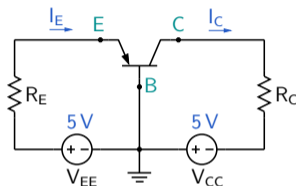
$$V_{EB} - V_{EE} + I_E R_E = 0 \rightarrow I_E R_E = 5 - 0.7 \rightarrow R_E = \frac{4.3 \text{ V}}{2 \text{ mA}} = 2.15 \text{ k}.$$

$$V_{BC} + I_C R_C - V_{CC} = 0 \rightarrow I_C R_C = V_{CC} - V_{BC}.$$

Since $\alpha \approx 1$, $I_C \approx I_E$

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$$\text{Since } \alpha \approx 1, I_C \approx I_E \rightarrow I_E R_C \approx 5 - 1 \rightarrow R_C = \frac{4 \text{ V}}{2 \text{ mA}} = 2 \text{ k}.$$