

Diode Circuits: Part 1

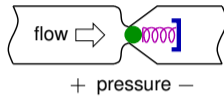
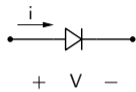


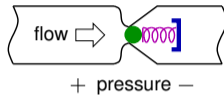
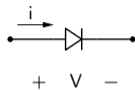
M. B. Patil

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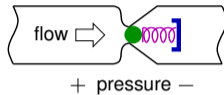
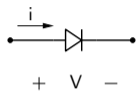
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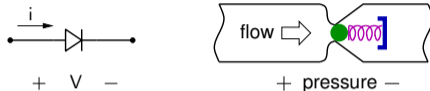




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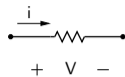
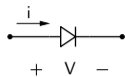


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- * Similarly, a diode presents a small resistance in the forward direction and a large resistance in the reverse direction.
- * Note: In a practical diode, the resistance $R_D = V/i$ is a nonlinear function of the applied voltage V . However, it is often a good approximation to treat it as a constant resistance which is small if V is positive and large if V is negative.

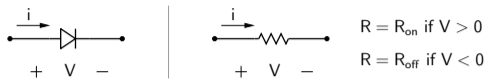
Simple models: $R_{\text{on}}/R_{\text{off}}$ model



$$R = R_{\text{on}} \text{ if } V > 0$$

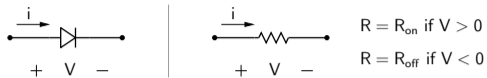
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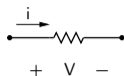
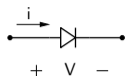
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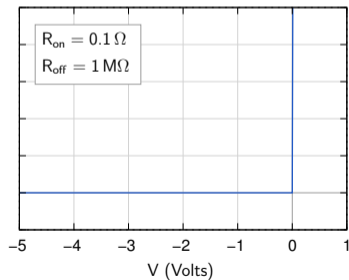
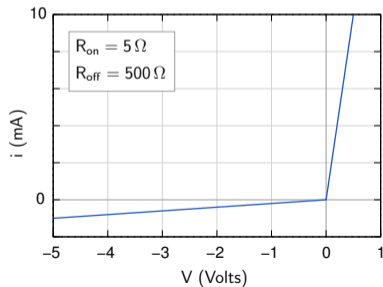
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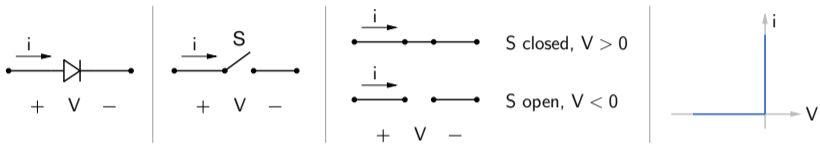
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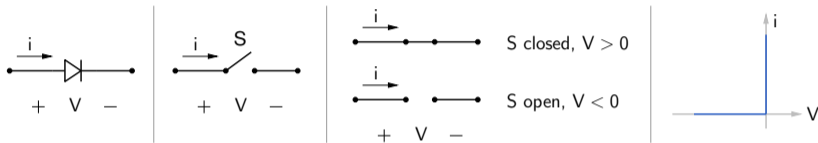
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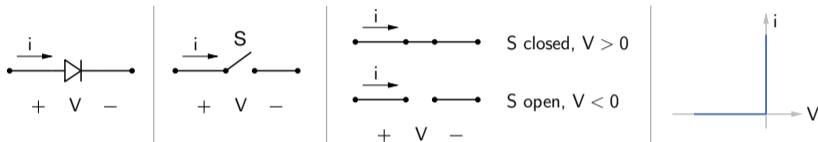


Simple models: ideal switch

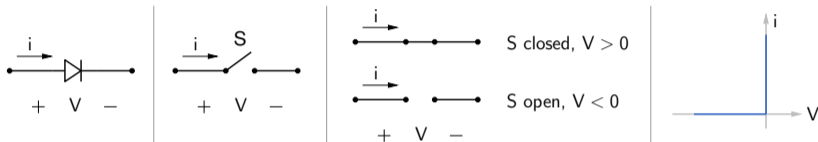




* Forward bias: $i > 0\text{ A}$, $V = 0\text{ V}$, \rightarrow S is closed (a perfect contact).

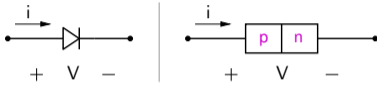


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- * The actual values of V and i for a diode in a circuit get determined by the i - V relationship of the diode *and* the constraints on V and i imposed by the circuit.

Shockley diode equation



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$$i = I_s \left[\exp \left(\frac{V}{V_T} \right) - 1 \right], \text{ where } V_T = k_B T / q.$$

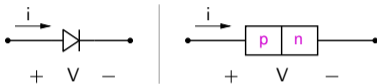
k_B = Boltzmann's constant = $1.38 \times 10^{-23} \text{ J/K}$.

q = electron charge = $1.602 \times 10^{-19} \text{ Coul}$.

T = temperature in $^{\circ}\text{K}$.

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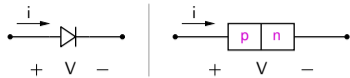
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- * The “turn-on” voltage (V_{on}) of a diode depends on the value of I_s . V_{on} may be defined as the voltage at which the diode starts carrying a substantial forward current (say, a few mA).
For a silicon diode, $V_{\text{on}} \approx 0.7$ V.
For LEDs, V_{on} varies from about 1.8 V (red) to 3.3 V (blue).

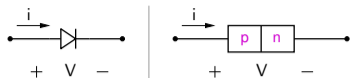
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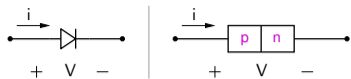


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0.2	7.74	0.229×10^4	0.229×10^{-9}
0.3	11.6	0.110×10^6	0.110×10^{-7}
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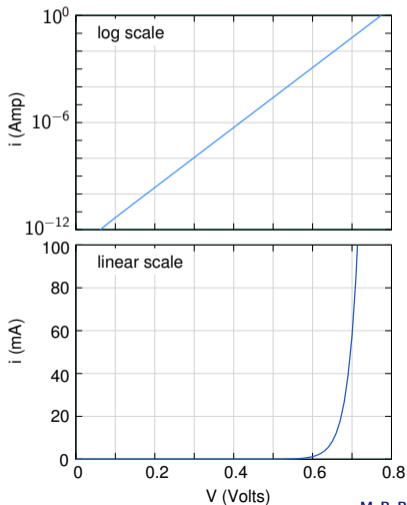
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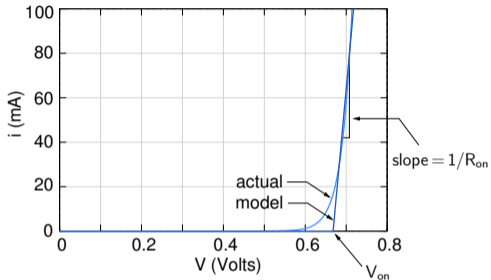
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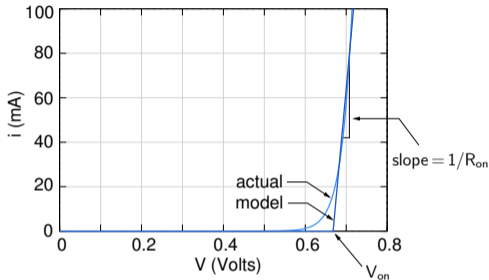


Diode circuit model



- * In many circuits, R_{on} can be neglected (assumed to be $0\ \Omega$) since it is much smaller than the other resistances in the circuit. In that case, the diode in forward conduction can be replaced with simply a battery.

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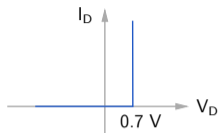
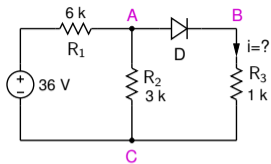
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- * Note that the “battery” shown in the above model is not a “source” of power! It can only absorb power (see the direction of the current), causing heat dissipation.

- * In DC situations, for each diode in the circuit, we need to establish whether it is on or off, replace it with the corresponding equivalent circuit, and then obtain the quantities of interest.

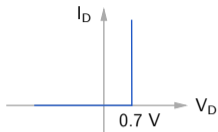
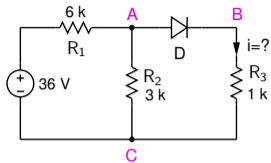
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- * In some diode circuits, the exponential nature of the diode I-V relationship (the Shockley model) is made use of. For these circuits, computation is usually difficult, and computer simulation may be required to solve the resulting non-linear equations.

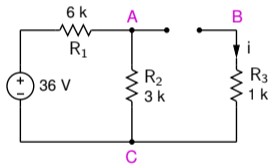
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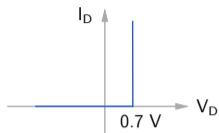
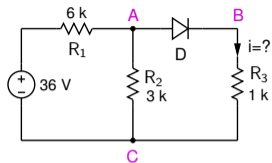
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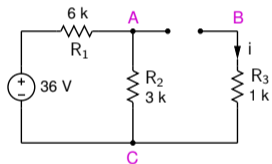
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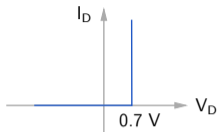
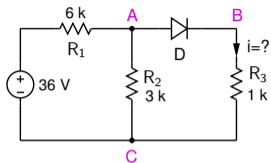
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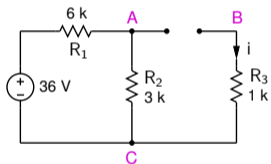
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which is not consistent with our assumption of D being off.

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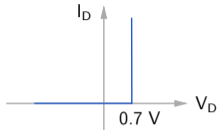
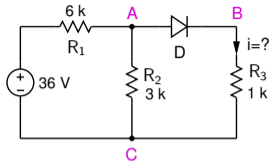


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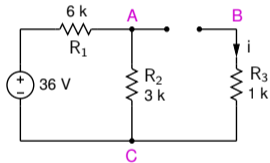
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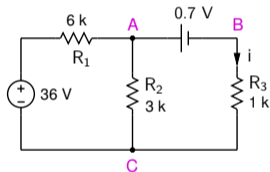


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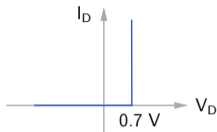
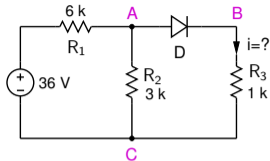
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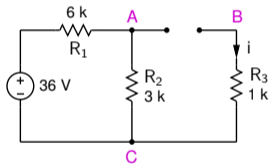
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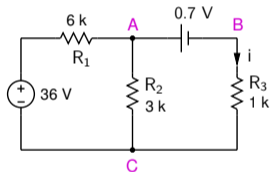


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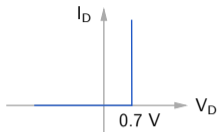
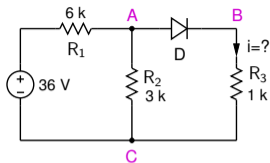


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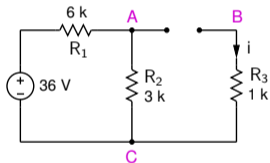
$$\frac{V_A - 36}{6 \text{ k}} + \frac{V_A}{3 \text{ k}} + \frac{V_A - 0.7}{1 \text{ k}} = 0,$$

→ $V_A = 4.47 \text{ V}$, $i = 3.77 \text{ mA}$.

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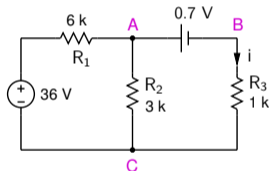


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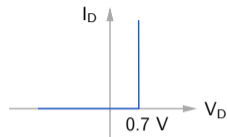
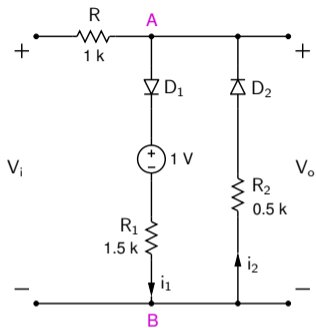
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$$\frac{V_A - 36}{6 \text{ k}} + \frac{V_A}{3 \text{ k}} + \frac{V_A - 0.7}{1 \text{ k}} = 0,$$

→ $V_A = 4.47 \text{ V}$, $i = 3.77 \text{ mA}$.

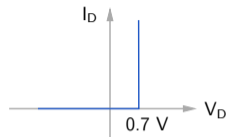
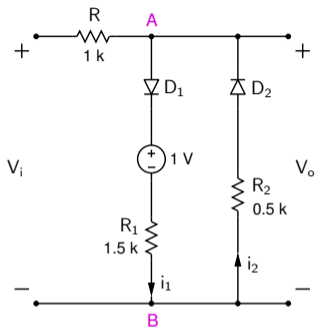
Remark: Often, we can figure out by inspection if a diode is on or off.

Diode circuit example



- (a) Plot V_o versus V_i for $-5 \text{ V} < V_i < 5 \text{ V}$.
- (b) Plot $V_o(t)$ for a triangular input:
 -5 V to $+5 \text{ V}$, 500 Hz .

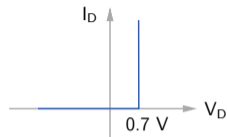
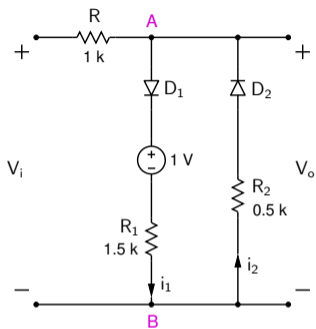
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First, let us show that D_1 on $\Rightarrow D_2$ off, and D_2 on $\Rightarrow D_1$ off.

Diode circuit example

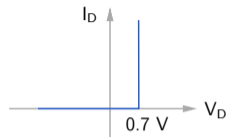
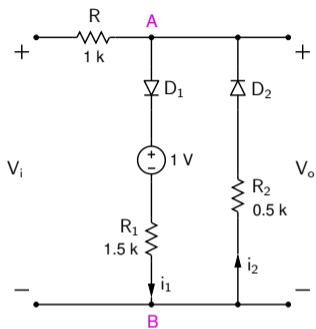


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Consider D_1 to be on $\rightarrow V_{AB} = 0.7 + 1 + i_1 R_1$.

Diode circuit example



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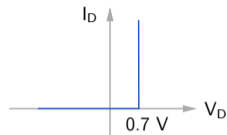
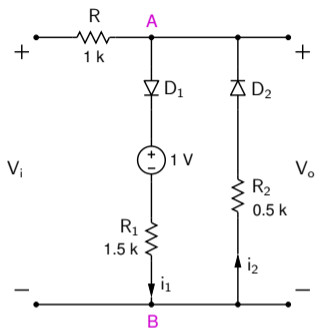
First, let us show that D_1 on $\Rightarrow D_2$ off, and D_2 on $\Rightarrow D_1$ off.

Consider D_1 to be on $\rightarrow V_{AB} = 0.7 + 1 + i_1 R_1$.

Note that $i_1 > 0$, since D_1 can only conduct in the forward direction.

$\Rightarrow V_{AB} > 1.7 \text{ V} \Rightarrow D_2$ cannot conduct.

Diode circuit example



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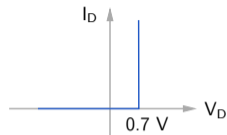
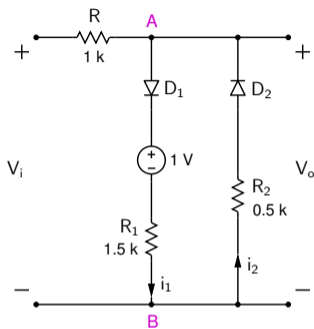
Consider D_1 to be on $\rightarrow V_{AB} = 0.7 + 1 + i_1 R_1$.

Note that $i_1 > 0$, since D_1 can only conduct in the forward direction.

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Similarly, if D_2 is on, $V_{BA} > 0.7 \text{ V}$, i.e., $V_{AB} < -0.7 \text{ V} \Rightarrow D_1$ cannot conduct.

Diode circuit example



- (a) Plot V_o versus V_i for $-5 \text{ V} < V_i < 5 \text{ V}$.
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First, let us show that D_1 on $\Rightarrow D_2$ off, and D_2 on $\Rightarrow D_1$ off.

Consider D_1 to be on $\rightarrow V_{AB} = 0.7 + 1 + i_1 R_1$.

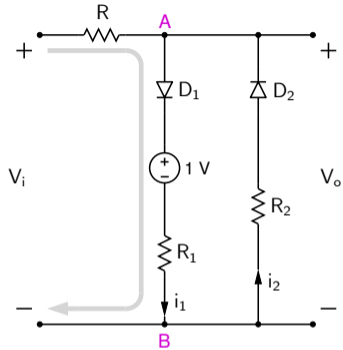
Note that $i_1 > 0$, since D_1 can only conduct in the forward direction.

$\Rightarrow V_{AB} > 1.7 \text{ V} \Rightarrow D_2$ cannot conduct.

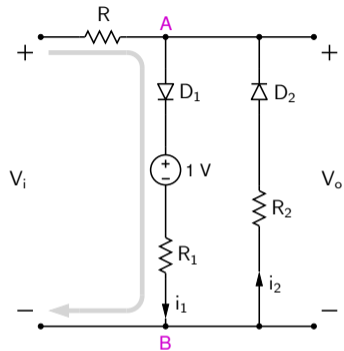
Similarly, if D_2 is on, $V_{BA} > 0.7 \text{ V}$, i.e., $V_{AB} < -0.7 \text{ V} \Rightarrow D_1$ cannot conduct.

Clearly, D_1 on $\Rightarrow D_2$ off, and D_2 on $\Rightarrow D_1$ off.

Diode circuit example



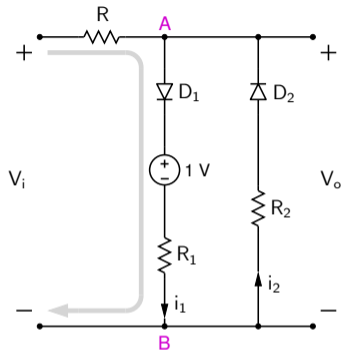
Diode circuit example



D_1 on:

$$V_i = i_1(R + R_1) + 1 + 0.7$$

Diode circuit example

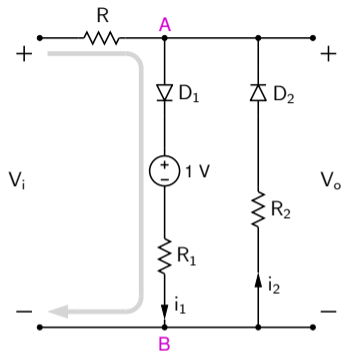


D_1 on:

$$V_i = i_1(R + R_1) + 1 + 0.7$$

Since $i_1 > 0$, $V_i > 1.7V$

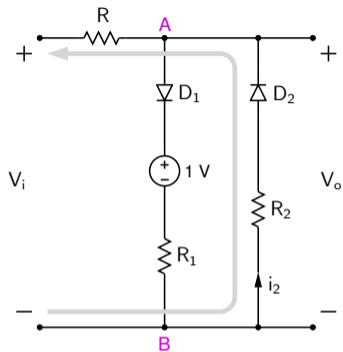
Diode circuit example



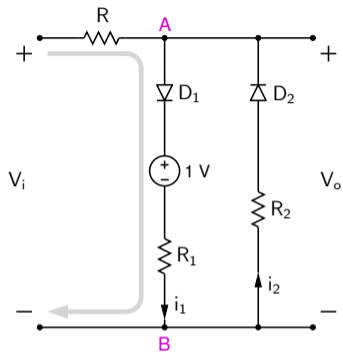
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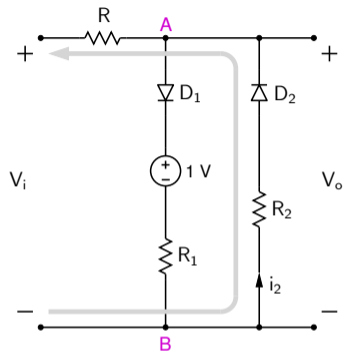
Diode circuit example



D_1 on:

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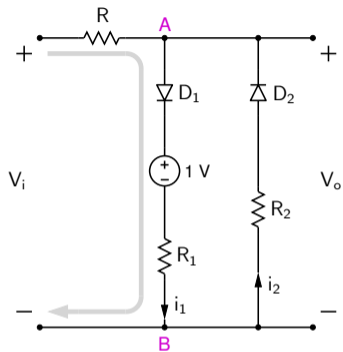
Since $i_1 > 0$, $V_i > 1.7V$



D_2 on:

$$i_2(R + R_2) + 0.7 + V_i = 0$$

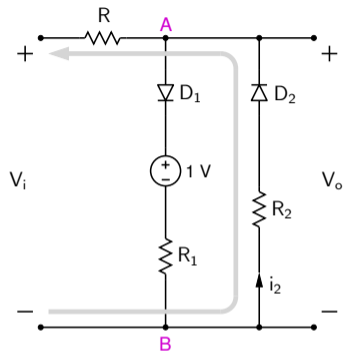
Diode circuit example



D_1 on:

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Since $i_1 > 0$, $V_i > 1.7V$

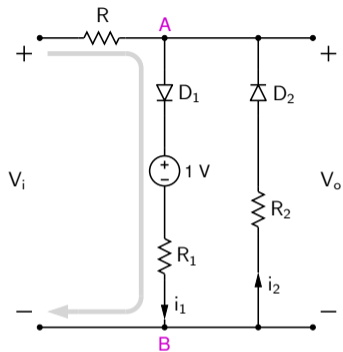


D_2 on:

$$i_2(R + R_2) + 0.7 + V_i = 0$$

$$V_i = -[0.7 + i_2(R + R_2)]$$

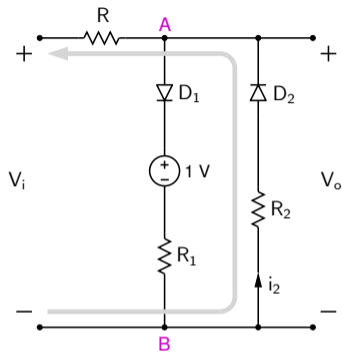
Diode circuit example



D_1 on:

$$V_i = i_1(R + R_1) + 1 + 0.7$$

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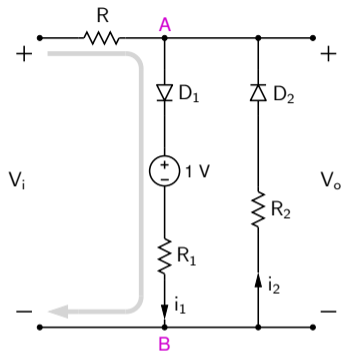
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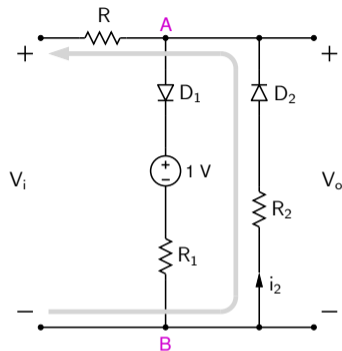
Diode circuit example



D_1 on:

$$V_i = i_1(R + R_1) + 1 + 0.7$$

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D_2 on:

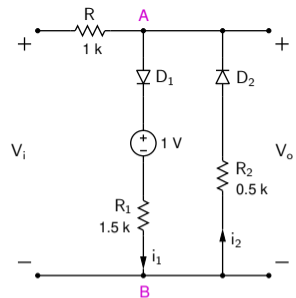
$$i_2(R + R_2) + 0.7 + V_i = 0$$

$$V_i = -[0.7 + i_2(R + R_2)]$$

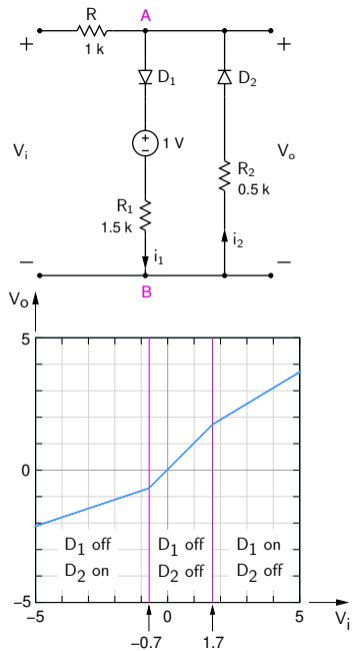
$$\text{Since } i_2 > 0, \boxed{V_i < -0.7\text{V}}$$

For $-0.7\text{V} < V_i < 1.7\text{V}$, neither D_1 nor D_2 can conduct.

- * For $-0.7 \text{ V} < V_i < 1.7 \text{ V}$, both D_1 and D_2 are off.
→ no drop across R , and $V_o = V_i$. (1)



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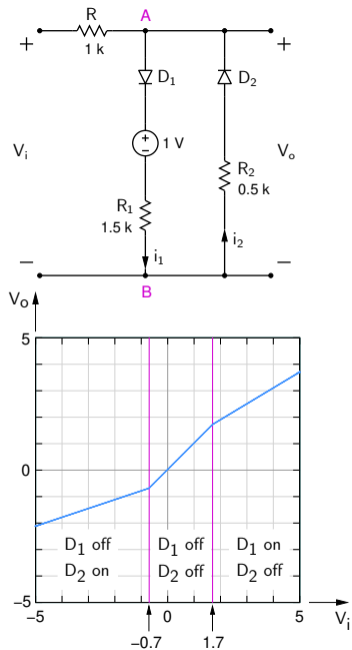
* For $-0.7 \text{ V} < V_i < 1.7 \text{ V}$, both D_1 and D_2 are off.
 \rightarrow no drop across R , and $V_o = V_i$. (1)

* For $V_i < -0.7 \text{ V}$, D_2 conducts. $\rightarrow V_o = -0.7 - i_2 R_2$.
 Use KVL to get i_2 : $V_i + i_2 R_2 + 0.7 + R i_2 = 0$.

$$\rightarrow i_2 = -\frac{V_i + 0.7}{R + R_2}, \text{ and}$$

$$V_o = -0.7 - R_2 i_2 = \frac{R_2}{R + R_2} V_i - 0.7 \frac{R}{R + R_2}. \quad (2)$$

$$\text{Slope } \frac{dV_o}{dV_i} = \frac{R_2}{R + R_2} = \frac{0.5 \text{ k}}{1 \text{ k} + 0.5 \text{ k}} = \frac{1}{3}.$$



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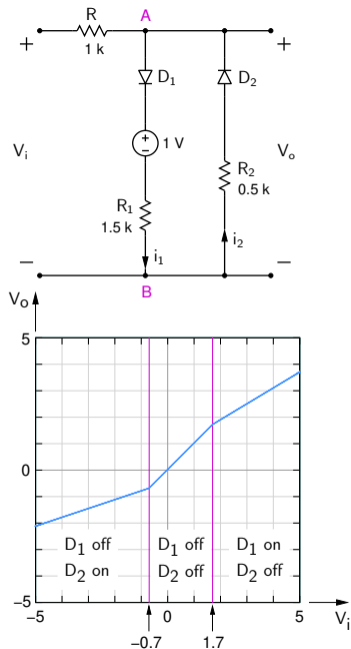
$$\text{Slope } \frac{dV_o}{dV_i} = \frac{R_2}{R + R_2} = \frac{0.5 \text{ k}}{1 \text{ k} + 0.5 \text{ k}} = \frac{1}{3}.$$

* For $V_i > 1.7 \text{ V}$, D_1 conducts. $\rightarrow V_o = 0.7 + 1 + i_1 R_1$.
 Use KVL to get i_1 : $-V_i + i_1 R + 0.7 + 1 + i_1 R_1 = 0$.

$$\rightarrow i_1 = \frac{V_i - 1.7}{R + R_1}, \text{ and}$$

$$V_o = 1.7 + R_1 i_1 = \frac{R_1}{R + R_1} V_i + 1.7 \frac{R}{R + R_1}. \quad (3)$$

$$\text{Slope } \frac{dV_o}{dV_i} = \frac{R_1}{R + R_1} = \frac{1.5 \text{ k}}{1 \text{ k} + 1.5 \text{ k}} = \frac{3}{5}.$$



* For $-0.7 \text{ V} < V_i < 1.7 \text{ V}$, both D_1 and D_2 are off.
 \rightarrow no drop across R , and $V_o = V_i$. (1)

* For $V_i < -0.7 \text{ V}$, D_2 conducts. $\rightarrow V_o = -0.7 - i_2 R_2$.
 Use KVL to get i_2 : $V_i + i_2 R_2 + 0.7 + R i_2 = 0$.

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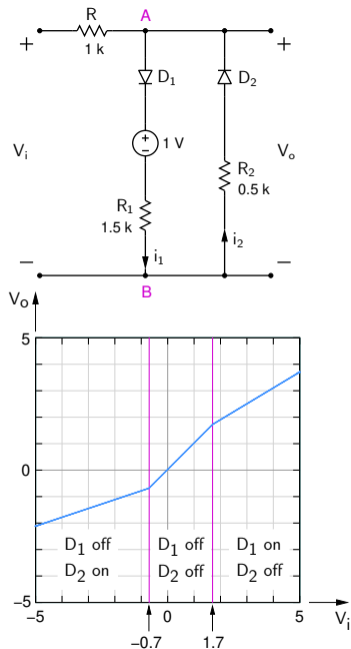
* For $V_i > 1.7 \text{ V}$, D_1 conducts. $\rightarrow V_o = 0.7 + 1 + i_1 R_1$.
 Use KVL to get i_1 : $-V_i + i_1 R + 0.7 + 1 + i_1 R_1 = 0$.

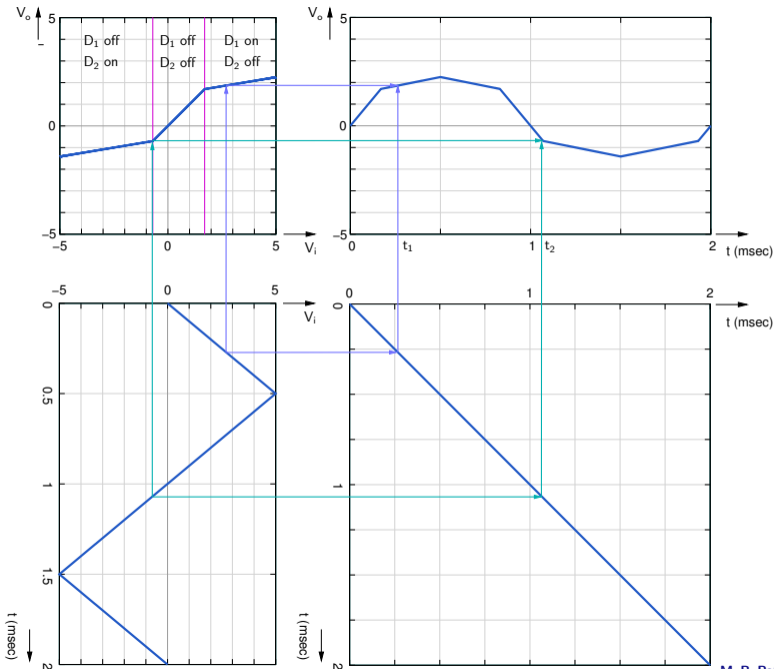
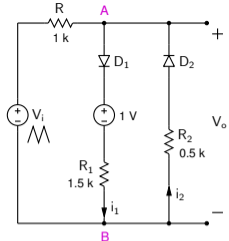
$$\rightarrow i_1 = \frac{V_i - 1.7}{R + R_1}, \text{ and}$$

$$V_o = 1.7 + R_1 i_1 = \frac{R_1}{R + R_1} V_i + 1.7 \frac{R}{R + R_1}. \quad (3)$$

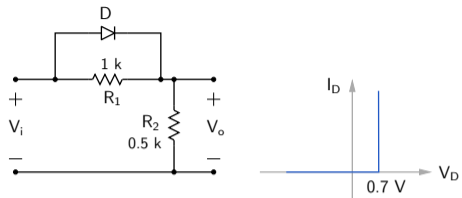
$$\text{Slope } \frac{dV_o}{dV_i} = \frac{R_1}{R + R_1} = \frac{1.5 \text{ k}}{1 \text{ k} + 1.5 \text{ k}} = \frac{3}{5}.$$

* Using Eqs. (1)-(3), we plot V_o versus V_i .
 (SEQUEL file: ee101_diode_circuit_1.sqproj)



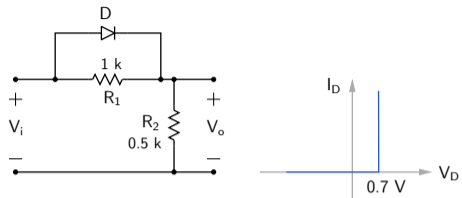


Diode circuit example

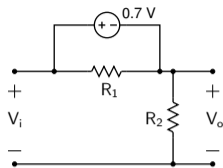


Plot V_o versus V_i for $-5 \text{ V} < V_i < 5 \text{ V}$.

Diode circuit example

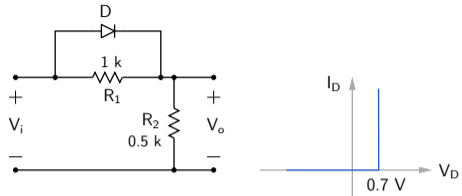


Plot V_o versus V_i for $-5 \text{ V} < V_i < 5 \text{ V}$.

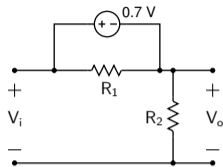


D on
 $V_o = V_i - 0.7$

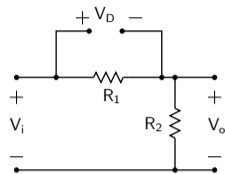
Diode circuit example



Plot V_o versus V_i for $-5 \text{ V} < V_i < 5 \text{ V}$.

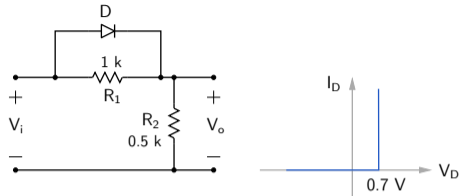


D on
 $V_o = V_i - 0.7$

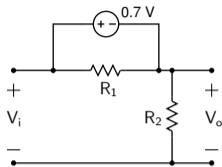


D off
 $V_o = \frac{R_2}{R_1 + R_2} V_i$

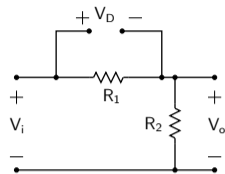
Diode circuit example



Plot V_o versus V_i for $-5\text{ V} < V_i < 5\text{ V}$.



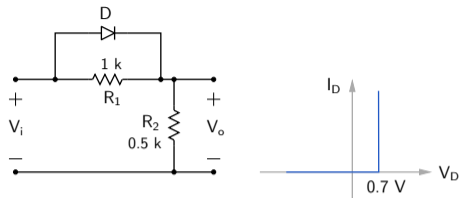
D on
 $V_o = V_i - 0.7$



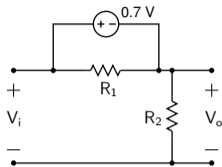
D off
 $V_o = \frac{R_2}{R_1 + R_2} V_i$

At what value of V_i will the diode turn on?

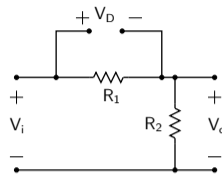
Diode circuit example



Plot V_o versus V_i for $-5\text{ V} < V_i < 5\text{ V}$.



D on
 $V_o = V_i - 0.7$

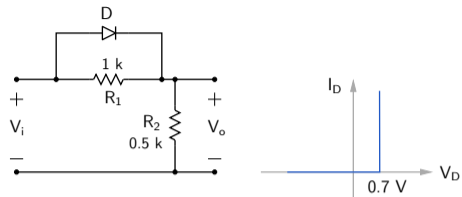


D off
 $V_o = \frac{R_2}{R_1 + R_2} V_i$

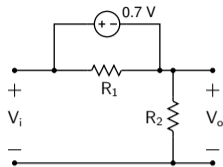
At what value of V_i will the diode turn on?

In the off state, $V_D = \frac{R_1}{R_1 + R_2} V_i$.

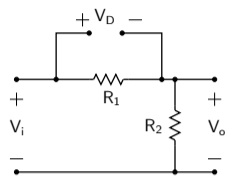
Diode circuit example



Plot V_o versus V_i for $-5\text{ V} < V_i < 5\text{ V}$.



D on
 $V_o = V_i - 0.7$



D off
 $V_o = \frac{R_2}{R_1 + R_2} V_i$

At what value of V_i will the diode turn on?

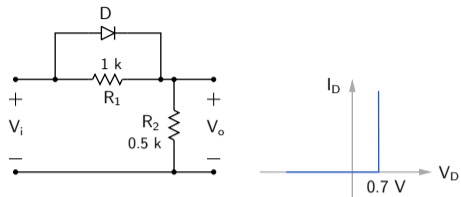
In the off state, $V_D = \frac{R_1}{R_1 + R_2} V_i$.

As V_i increases, V_D increases.

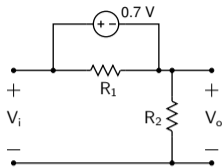
For D to turn on, we need $V_D = 0.7\text{ V}$.

i.e., $V_i = \frac{R_1 + R_2}{R_1} \times 0.7 = 1.05\text{ V}$.

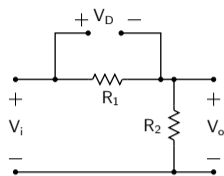
Diode circuit example



Plot V_o versus V_i for $-5\text{ V} < V_i < 5\text{ V}$.



D on
 $V_o = V_i - 0.7$



D off
 $V_o = \frac{R_2}{R_1 + R_2} V_i$

At what value of V_i will the diode turn on?

In the off state, $V_D = \frac{R_1}{R_1 + R_2} V_i$.

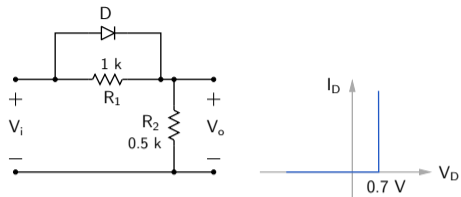
As V_i increases, V_D increases.

For D to turn on, we need $V_D = 0.7\text{ V}$.

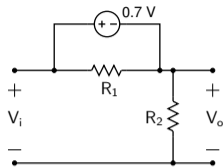
i.e., $V_i = \frac{R_1 + R_2}{R_1} \times 0.7 = 1.05\text{ V}$.

(SEQUEL file: ee101_diode_circuit_2.sqproj)

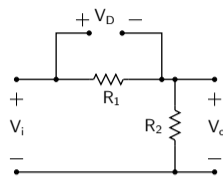
Diode circuit example



Plot V_o versus V_i for $-5 \text{ V} < V_i < 5 \text{ V}$.



D on
 $V_o = V_i - 0.7$



D off
 $V_o = \frac{R_2}{R_1 + R_2} V_i$

At what value of V_i will the diode turn on?

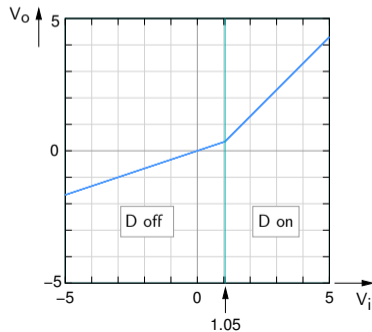
In the off state, $V_D = \frac{R_1}{R_1 + R_2} V_i$.

As V_i increases, V_D increases.

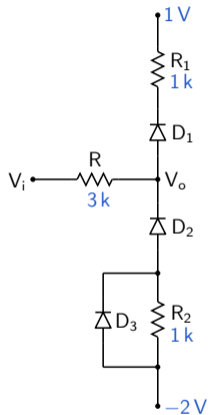
For D to turn on, we need $V_D = 0.7 \text{ V}$.

i.e., $V_i = \frac{R_1 + R_2}{R_1} \times 0.7 = 1.05 \text{ V}$.

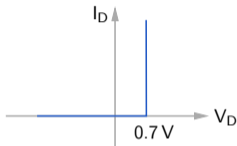
(SEQUEL file: ee101_diode_circuit_2.sqproj)



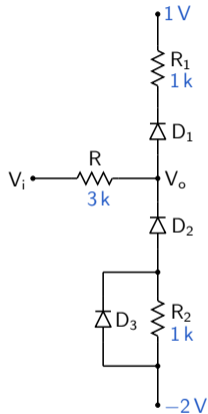
Diode circuit example



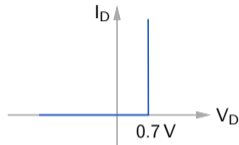
Plot V_o versus V_i (Ref: Sedra/Smith).



Diode circuit example

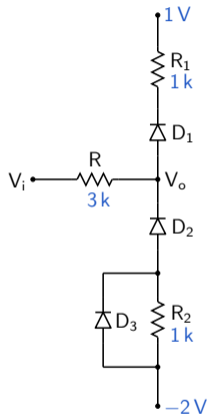


Plot V_o versus V_i (Ref: Sedra/Smith).

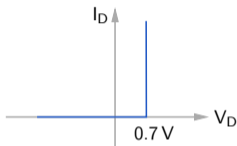


It is easier to find the status (on/off) of each diode w. r. t. V_o .

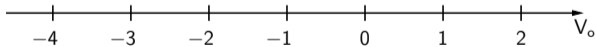
Diode circuit example



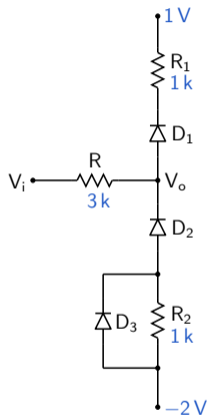
Plot V_o versus V_i (Ref: Sedra/Smith).



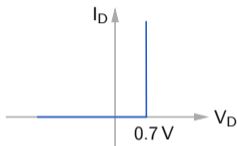
It is easier to find the status (on/off) of each diode w. r. t. V_o .



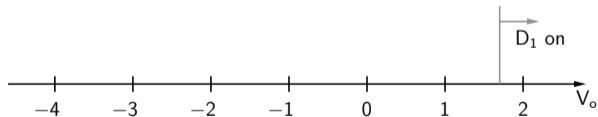
Diode circuit example



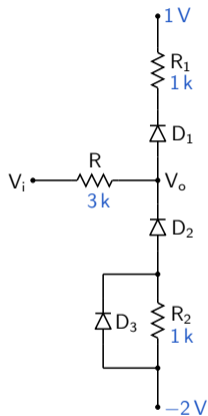
Plot V_o versus V_i (Ref: Sedra/Smith).



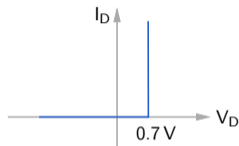
It is easier to find the status (on/off) of each diode w. r. t. V_o .



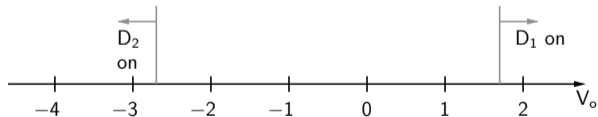
Diode circuit example



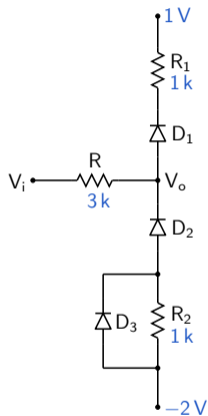
Plot V_o versus V_i (Ref: Sedra/Smith).



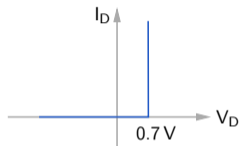
It is easier to find the status (on/off) of each diode w. r. t. V_o .



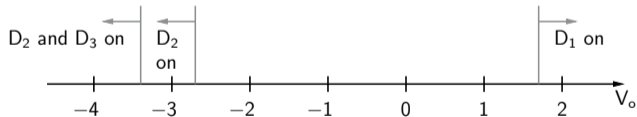
Diode circuit example

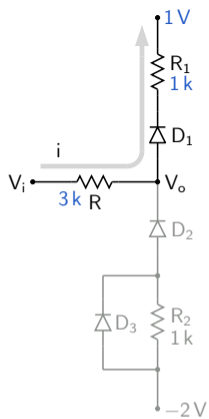


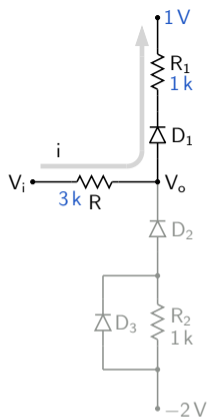
Plot V_o versus V_i (Ref: Sedra/Smith).



It is easier to find the status (on/off) of each diode w. r. t. V_o .

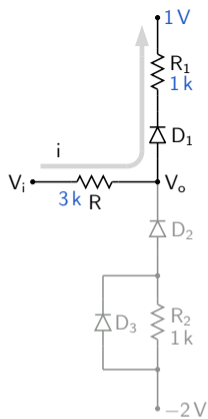






When D_1 just starts conducting,

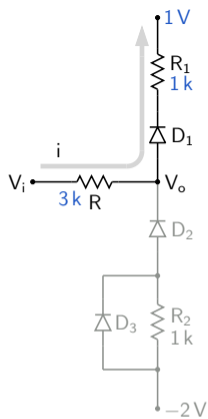
$$V_o = 1.7V, i \approx 0 \rightarrow V_i = 1.7V$$



When D_1 just starts conducting,

$$V_o = 1.7\text{V}, i \approx 0 \rightarrow V_i = 1.7\text{V}$$

$$\text{For } V_i > 1.7\text{V}, V_o = 1.7 + \left(\frac{V_i - 1.7}{R + R_1} \right) R_1$$

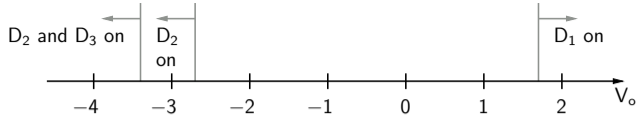
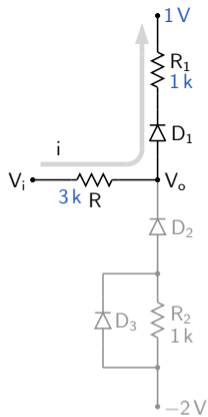


When D_1 just starts conducting,

$$V_o = 1.7\text{V}, i \approx 0 \rightarrow V_i = 1.7\text{V}$$

$$\text{For } V_i > 1.7\text{V}, V_o = 1.7 + \left(\frac{V_i - 1.7}{R + R_1} \right) R_1$$

$$\text{Slope } \frac{dV_o}{dV_i} = \frac{R_1}{R + R_1} = \frac{1}{4}$$

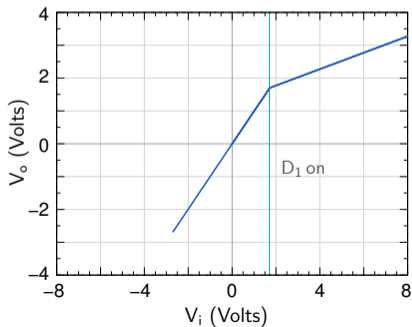


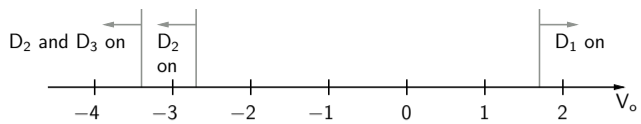
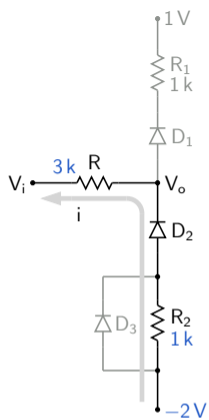
When D_1 just starts conducting,

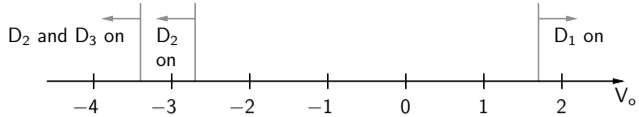
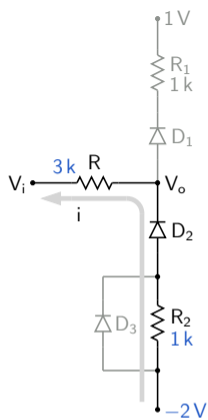
$$V_o = 1.7\text{V}, i \approx 0 \rightarrow V_i = 1.7\text{V}$$

$$\text{For } V_i > 1.7\text{V}, V_o = 1.7 + \left(\frac{V_i - 1.7}{R + R_1} \right) R_1$$

$$\text{Slope } \frac{dV_o}{dV_i} = \frac{R_1}{R + R_1} = \frac{1}{4}$$

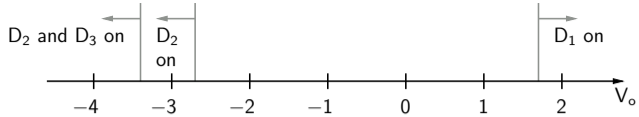
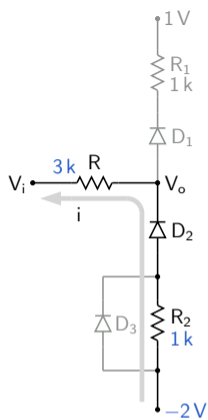






When D_2 just starts conducting,

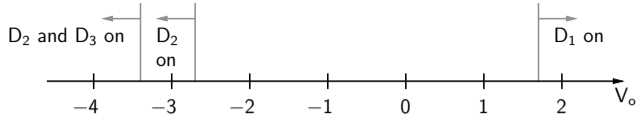
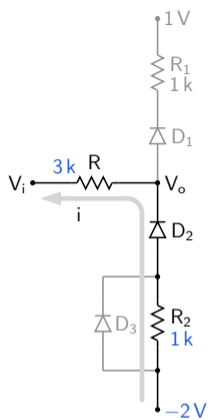
$$V_o = -2.7V, i \approx 0 \rightarrow V_i = -2.7V$$



When D_2 just starts conducting,

$$V_o = -2.7V, i \approx 0 \rightarrow V_i = -2.7V$$

$$\text{For } V_i < -2.7V, V_o = V_i + \left(\frac{-2.7 - V_i}{R + R_2} \right) R$$

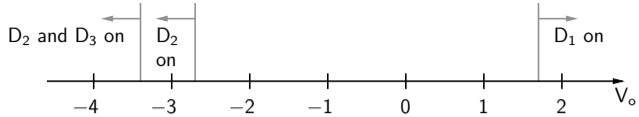
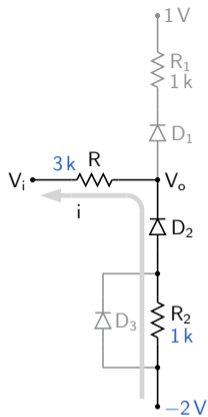


When D_2 just starts conducting,

$$V_o = -2.7\text{V}, i \approx 0 \rightarrow V_i = -2.7\text{V}$$

$$\text{For } V_i < -2.7\text{V}, V_o = V_i + \left(\frac{-2.7 - V_i}{R + R_2} \right) R$$

$$\text{Slope } \frac{dV_o}{dV_i} = 1 - \frac{R}{R + R_2} = \frac{R_2}{R + R_2} = \frac{1}{4}$$

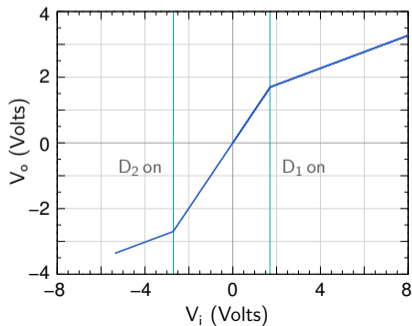


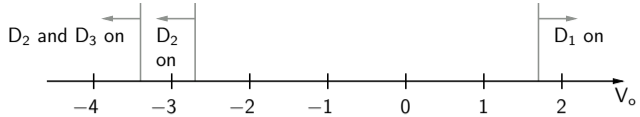
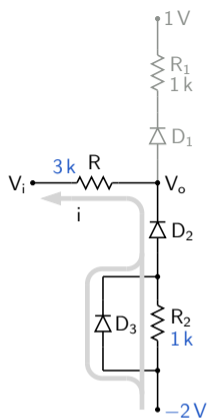
When D_2 just starts conducting,

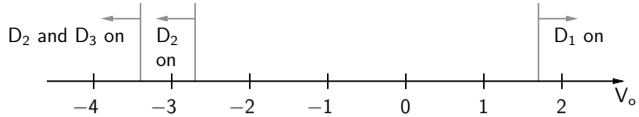
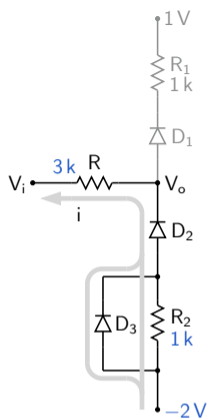
$$V_o = -2.7\text{V}, i \approx 0 \rightarrow V_i = -2.7\text{V}$$

$$\text{For } V_i < -2.7\text{V}, V_o = V_i + \left(\frac{-2.7 - V_i}{R + R_2} \right) R$$

$$\text{Slope } \frac{dV_o}{dV_i} = 1 - \frac{R}{R + R_2} = \frac{R_2}{R + R_2} = \frac{1}{4}$$

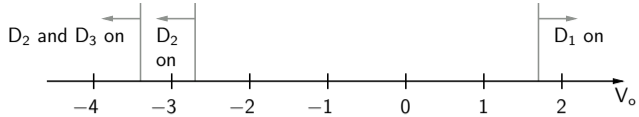
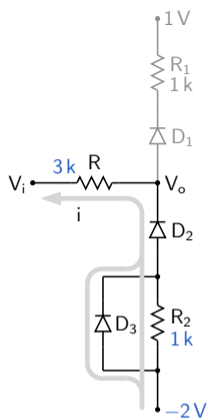






When D_3 just starts conducting,

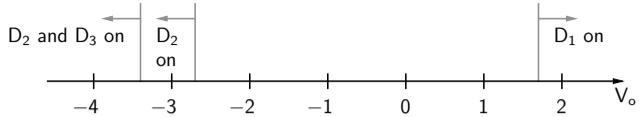
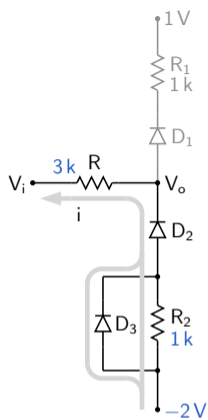
$$R_2 \frac{(-2.7 - V_i)}{R + R_2} = 0.7 \text{ V} \rightarrow V_i = -5.5 \text{ V}$$



When D_3 just starts conducting,

$$R_2 \frac{(-2.7 - V_i)}{R + R_2} = 0.7 \text{ V} \rightarrow V_i = -5.5 \text{ V}$$

$$V_o = -2 - 0.7 - 0.7 = -3.4 \text{ V}$$

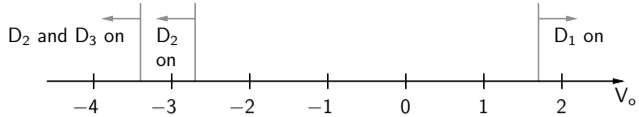
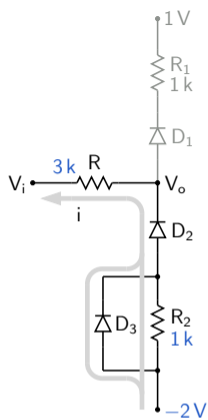


When D_3 just starts conducting,

$$R_2 \frac{(-2.7 - V_i)}{R + R_2} = 0.7 \text{ V} \rightarrow V_i = -5.5 \text{ V}$$

$$V_o = -2 - 0.7 - 0.7 = -3.4 \text{ V}$$

For $V_i < -5.5 \text{ V}$, $V_o = -3.4 \text{ V}$ (constant)

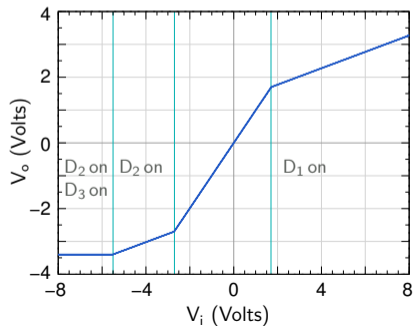


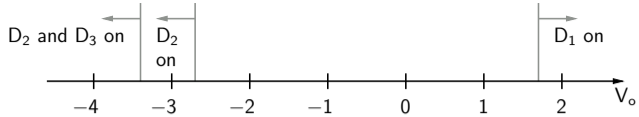
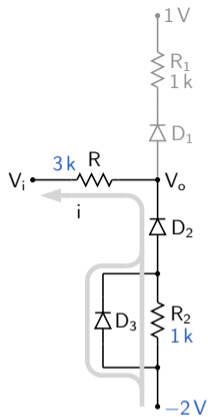
When D_3 just starts conducting,

$$R_2 \frac{(-2.7 - V_i)}{R + R_2} = 0.7 \text{ V} \rightarrow V_i = -5.5 \text{ V}$$

$$V_o = -2 - 0.7 - 0.7 = -3.4 \text{ V}$$

For $V_i < -5.5 \text{ V}$, $V_o = -3.4 \text{ V}$ (constant)



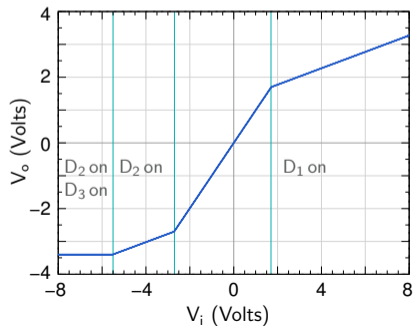


When D_3 just starts conducting,

$$R_2 \frac{(-2.7 - V_i)}{R + R_2} = 0.7 \text{ V} \rightarrow V_i = -5.5 \text{ V}$$

$$V_o = -2 - 0.7 - 0.7 = -3.4 \text{ V}$$

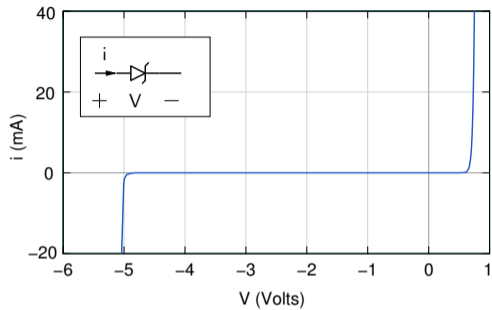
For $V_i < -5.5 \text{ V}$, $V_o = -3.4 \text{ V}$ (constant)

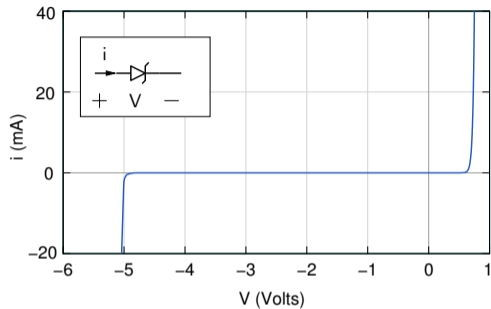


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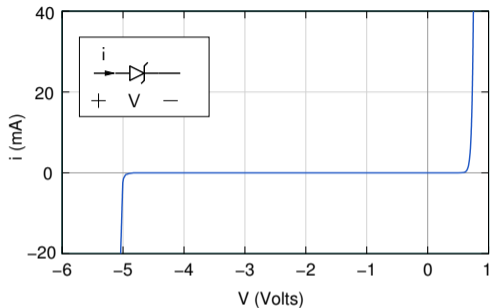
ee101_diode_circuit.12.sqproj

Reverse breakdown

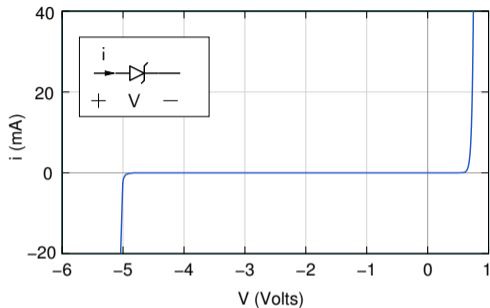




* In the reverse direction, an ideal diode presents a large resistance for *any* applied voltage.

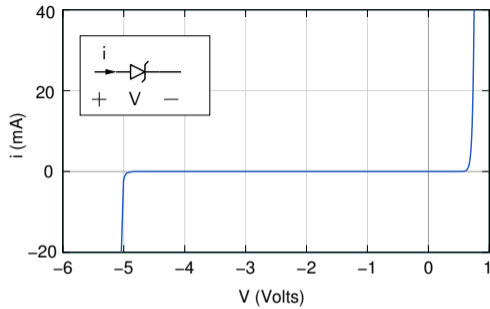


- * In the reverse direction, an ideal diode presents a large resistance for *any* applied voltage.
- * A real diode cannot withstand indefinitely large reverse voltages and “breaks down” at a certain voltage called the “breakdown voltage” (V_{BR}).



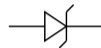
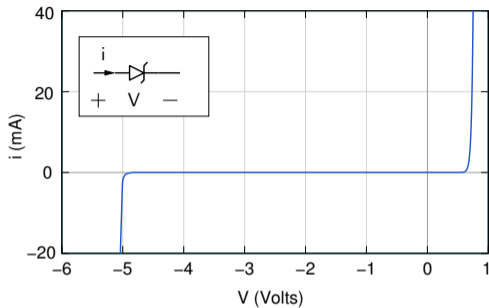
- * In the reverse direction, an ideal diode presents a large resistance for *any* applied voltage.
- * A real diode cannot withstand indefinitely large reverse voltages and “breaks down” at a certain voltage called the “breakdown voltage” (V_{BR}).
- * When the reverse bias $V_R > V_{BR}$ (i.e., $V < -V_{BR}$), the diode allows a large amount of current. If the current is not constrained by the external circuit, the diode would get damaged.

Reverse breakdown



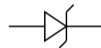
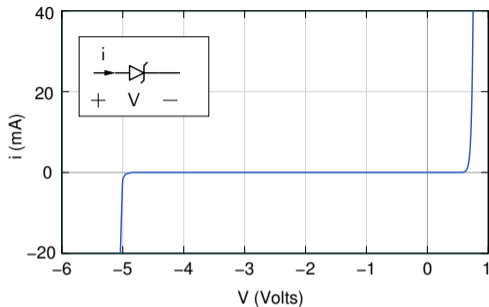
Symbol for a Zener diode

Reverse breakdown



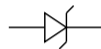
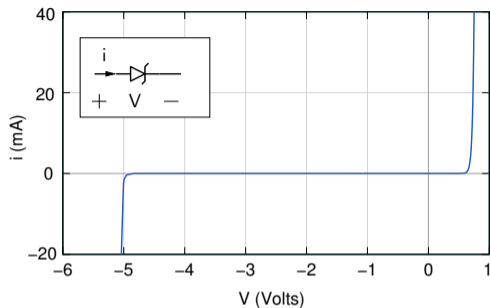
Symbol for a Zener diode

- * A wide variety of diodes is available, with V_{BR} ranging from a few Volts to a few thousand Volts! Generally, higher the breakdown voltage, higher is the cost.



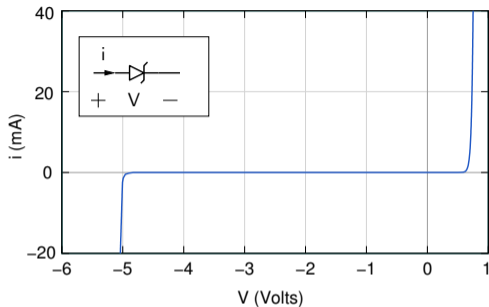
Symbol for a Zener diode

- * A wide variety of diodes is available, with V_{BR} ranging from a few Volts to a few thousand Volts! Generally, higher the breakdown voltage, higher is the cost.
- * Diodes with high V_{BR} are generally used in power electronics applications and are therefore also designed to carry a large forward current (tens or hundreds of Amps).



Symbol for a Zener diode

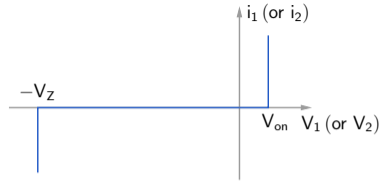
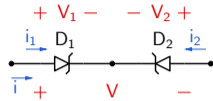
- * A wide variety of diodes is available, with V_{BR} ranging from a few Volts to a few thousand Volts! Generally, higher the breakdown voltage, higher is the cost.
- * Diodes with high V_{BR} are generally used in power electronics applications and are therefore also designed to carry a large forward current (tens or hundreds of Amps).
- * Typically, circuits are designed so that the reverse bias across any diode is less than the V_{BR} rating for that diode.



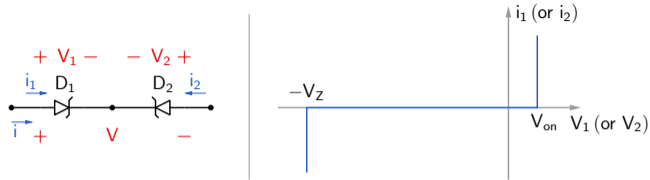
Symbol for a Zener diode

- * A wide variety of diodes is available, with V_{BR} ranging from a few Volts to a few thousand Volts! Generally, higher the breakdown voltage, higher is the cost.
- * Diodes with high V_{BR} are generally used in power electronics applications and are therefore also designed to carry a large forward current (tens or hundreds of Amps).
- * Typically, circuits are designed so that the reverse bias across any diode is less than the V_{BR} rating for that diode.
- * “Zener” diodes typically have V_{BR} of a few Volts, which is denoted by V_Z . They are often used to limit the voltage swing in electronic circuits.

Two Zener diodes connected "back-to-back"

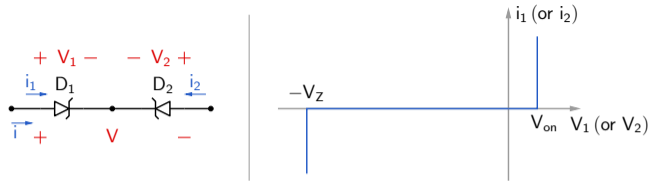


Two Zener diodes connected "back-to-back"



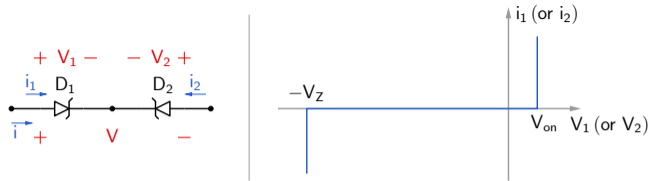
* $i > 0 \rightarrow D_1$ in forward conduction, D_2 in reverse conduction

Two Zener diodes connected "back-to-back"



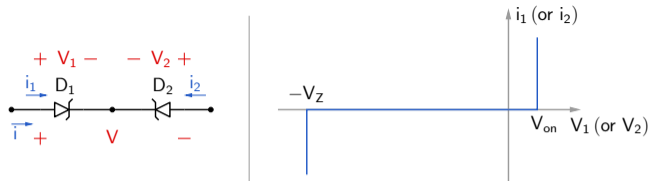
- * $i > 0 \rightarrow D_1$ in forward conduction, D_2 in reverse conduction
 $\rightarrow V_1 = V_{on}, V_2 = -V_Z$.

Two Zener diodes connected "back-to-back"



- * $i > 0 \rightarrow D_1$ in forward conduction, D_2 in reverse conduction
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Total voltage drop $V = V_1 - V_2 = V_{on} + V_Z$.

Two Zener diodes connected "back-to-back"



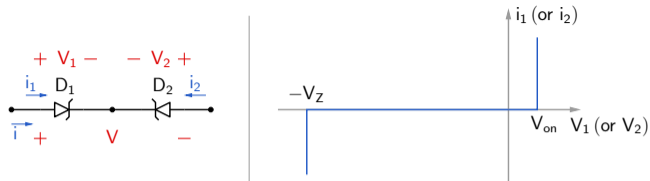
* $i > 0 \rightarrow D_1$ in forward conduction, D_2 in reverse conduction

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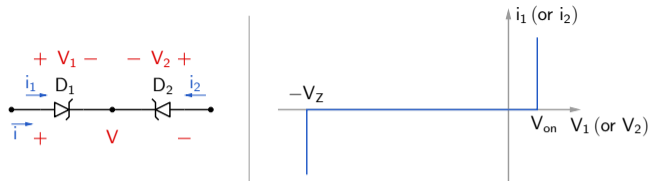
Example: $V_{on} = 0.7\text{ V}, V_Z = 5\text{ V} \rightarrow V = 5.7\text{ V}.$

Two Zener diodes connected “back-to-back”



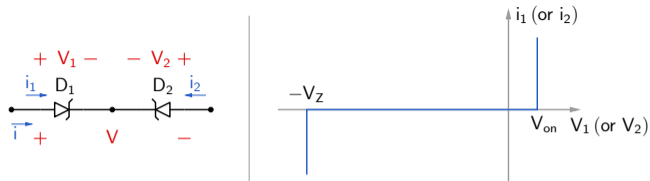
- * $i > 0 \rightarrow D_1$ in forward conduction, D_2 in reverse conduction
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Two Zener diodes connected “back-to-back”



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- * $i < 0 \rightarrow D_1$ in reverse conduction, D_2 in forward conduction
 $\rightarrow V_1 = -V_Z, V_2 = V_{on}$.

Two Zener diodes connected "back-to-back"



* $i > 0 \rightarrow D_1$ in forward conduction, D_2 in reverse conduction

$$\rightarrow V_1 = V_{on}, V_2 = -V_Z.$$

$$\text{Total voltage drop } V = V_1 - V_2 = V_{on} + V_Z.$$

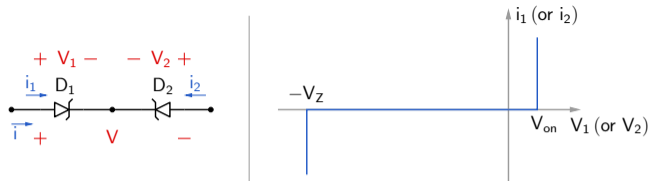
$$\text{Example: } V_{on} = 0.7 \text{ V}, V_Z = 5 \text{ V} \rightarrow V = 5.7 \text{ V}.$$

* $i < 0 \rightarrow D_1$ in reverse conduction, D_2 in forward conduction

$$\rightarrow V_1 = -V_Z, V_2 = V_{on}.$$

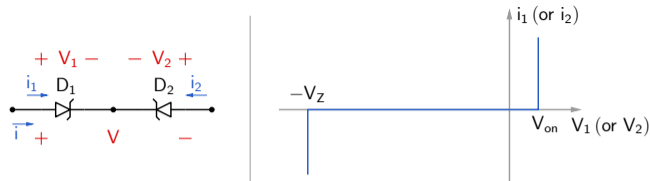
$$\text{Total voltage drop } V = V_1 - V_2 = -V_Z - V_{on} = -(V_Z + V_{on}) = -5.7 \text{ V}.$$

Two Zener diodes connected "back-to-back"

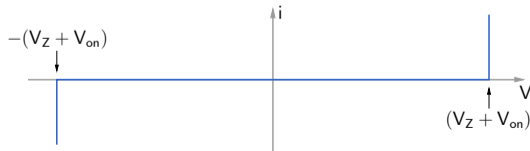


- * $i > 0 \rightarrow D_1$ in forward conduction, D_2 in reverse conduction
 $\rightarrow V_1 = V_{on}, V_2 = -V_Z$.
Total voltage drop $V = V_1 - V_2 = V_{on} + V_Z$.
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- * For $-(V_Z + V_{on}) < V < (V_Z + V_{on})$, conduction is not possible $\rightarrow i = 0$.

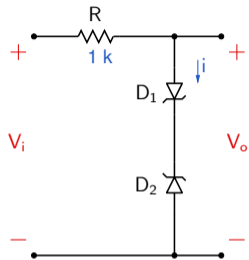
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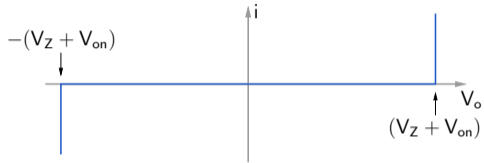
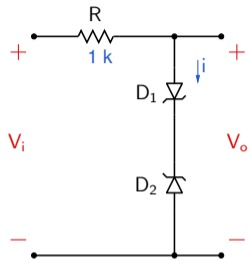
Diode circuit example (voltage limiter)



$$V_{\text{on}} = 0.7\text{ V}, V_Z = 5\text{ V}.$$

Plot V_o versus V_i .

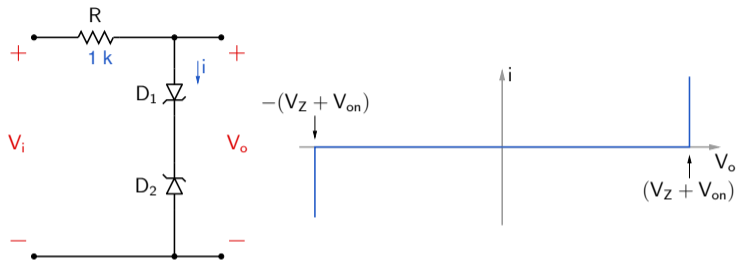
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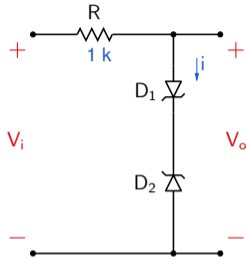


$$V_{on} = 0.7\text{ V}, V_Z = 5\text{ V}.$$

Plot V_o versus V_i .

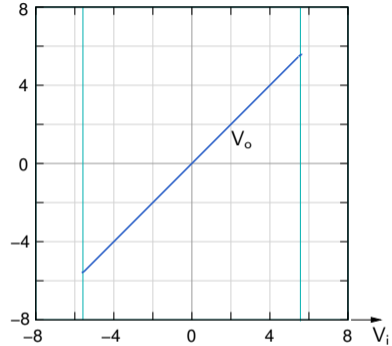
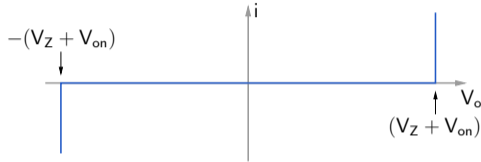
* For $-5.7\text{ V} < V_i < 5.7\text{ V}$, no conduction is possible $\rightarrow V_o = V_i$.

Diode circuit example (voltage limiter)



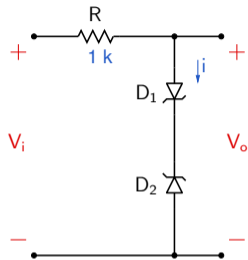
$$V_{\text{on}} = 0.7 \text{ V}, V_Z = 5 \text{ V}.$$

Plot V_o versus V_i .



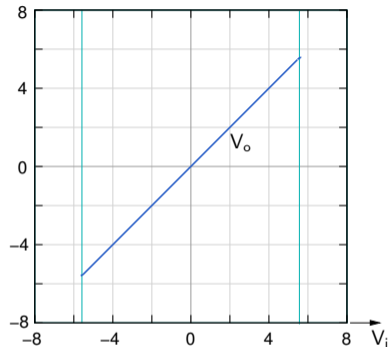
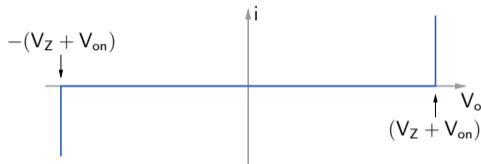
* For $-5.7 \text{ V} < V_i < 5.7 \text{ V}$, no conduction is possible $\rightarrow V_o = V_i$.

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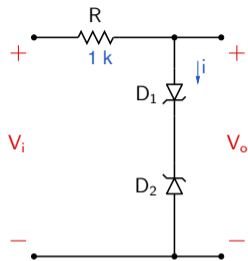
$$V_{\text{on}} = 0.7 \text{ V}, V_Z = 5 \text{ V}.$$

Plot V_o versus V_i .



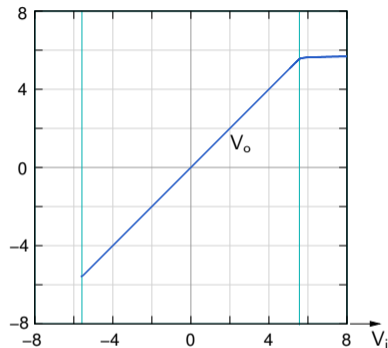
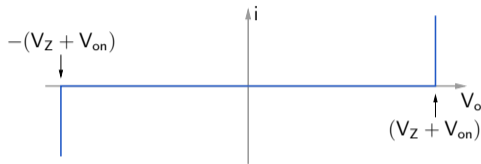
- * For $-5.7 \text{ V} < V_i < 5.7 \text{ V}$, no conduction is possible $\rightarrow V_o = V_i$.
- * For $V_i > 5.7 \text{ V}$, D_1 is forward-biased, D_2 is reverse-biased, and $V_o = (V_{\text{on}} + V_Z)$. The excess voltage $(V_i - (V_{\text{on}} + V_Z))$ drops across R .

Diode circuit example (voltage limiter)



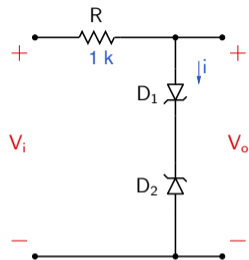
$$V_{\text{on}} = 0.7 \text{ V}, V_Z = 5 \text{ V}.$$

Plot V_o versus V_i .



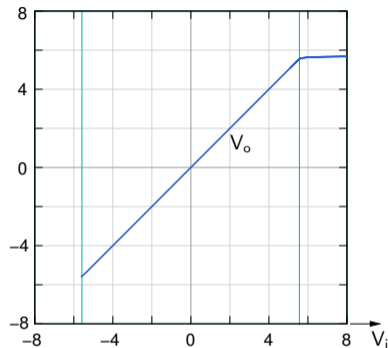
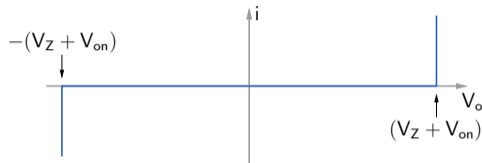
- * For $-5.7 \text{ V} < V_i < 5.7 \text{ V}$, no conduction is possible $\rightarrow V_o = V_i$.
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Diode circuit example (voltage limiter)



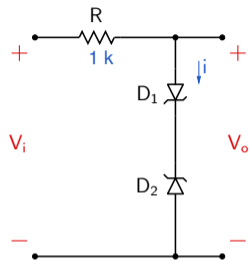
$$V_{\text{on}} = 0.7\text{ V}, V_Z = 5\text{ V}.$$

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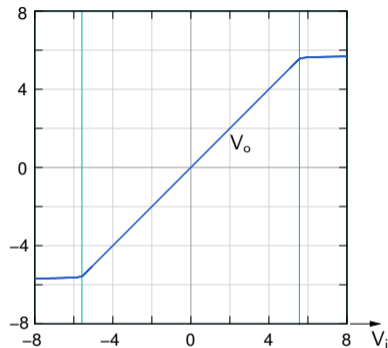
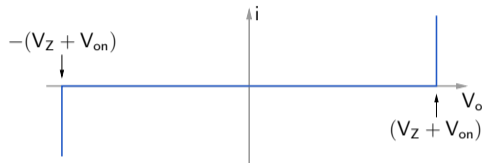
- * For $-5.7\text{ V} < V_i < 5.7\text{ V}$, no conduction is possible $\rightarrow V_o = V_i$.
- * For $V_i > 5.7\text{ V}$, D_1 is forward-biased, D_2 is reverse-biased, and $V_o = (V_{\text{on}} + V_Z)$. The excess voltage $(V_i - (V_{\text{on}} + V_Z))$ drops across R .
- * For $V_i < -5.7\text{ V}$, D_2 is forward-biased, D_1 is reverse-biased, and $V_o = -(V_{\text{on}} + V_Z)$. The excess voltage $(-V_i - (V_{\text{on}} + V_Z))$ drops across R .

Diode circuit example (voltage limiter)



$$V_{\text{on}} = 0.7 \text{ V}, V_Z = 5 \text{ V}.$$

Plot V_o versus V_i .



- * For $-5.7 \text{ V} < V_i < 5.7 \text{ V}$, no conduction is possible $\rightarrow V_o = V_i$.
- * For $V_i > 5.7 \text{ V}$, D_1 is forward-biased, D_2 is reverse-biased, and $V_o = (V_{\text{on}} + V_Z)$. The excess voltage $(V_i - (V_{\text{on}} + V_Z))$ drops across R .
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