

## Diode Circuits: Part 2

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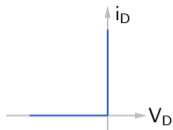
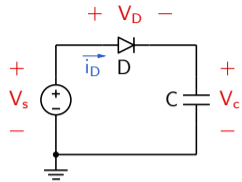
M. B. Patil

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[www.ee.iitb.ac.in/~sequel](http://www.ee.iitb.ac.in/~sequel)

Department of Electrical Engineering  
Indian Institute of Technology Bombay

# Peak detector (with $V_{on} = 0\text{ V}$ )

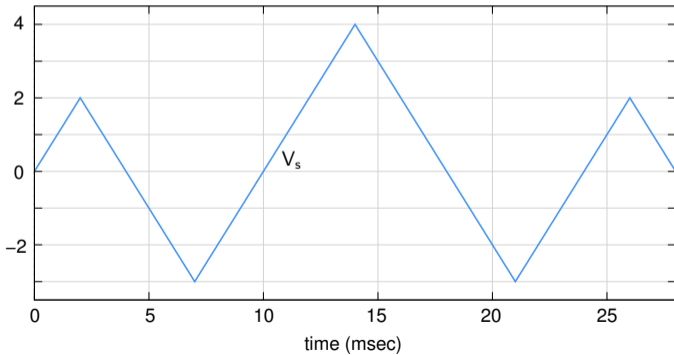


$$V_c(0) = 0\text{ V}$$

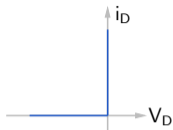
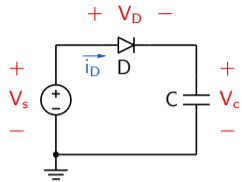
$$V_{on} = 0\text{ V}$$

$$R_{on} \rightarrow 0\ \Omega$$

$$R_{off} \rightarrow \infty\ \Omega$$



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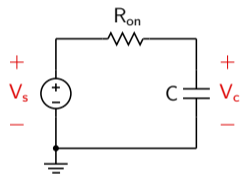


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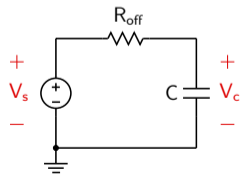
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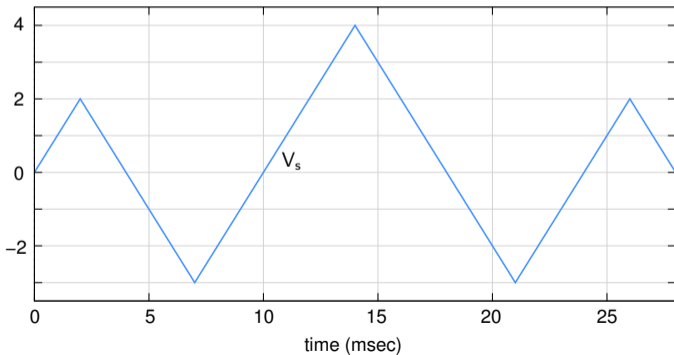
$$V_s > V_c$$

$$\tau = R_{on}C$$

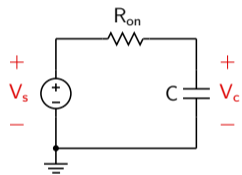
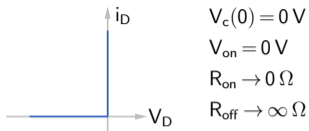
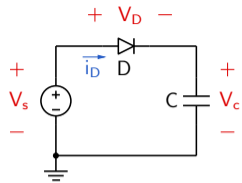


$$V_s < V_c$$

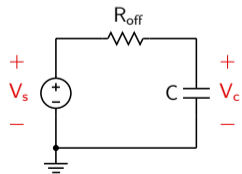
$$\tau = R_{off}C$$



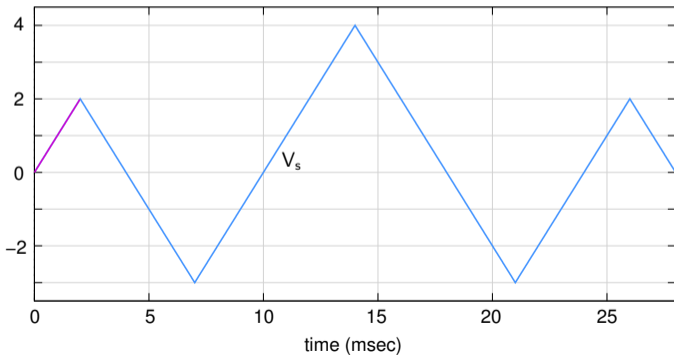
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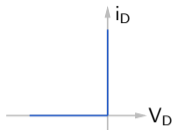
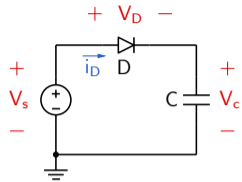
$$V_s > V_c$$
$$\tau = R_{on}C$$



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# Peak detector (with $V_{on} = 0\text{ V}$ )

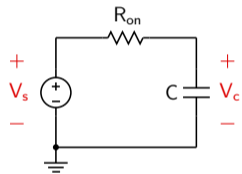


$$V_c(0) = 0\text{ V}$$

$$V_{on} = 0\text{ V}$$

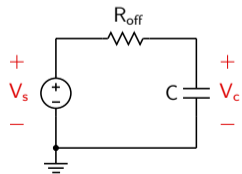
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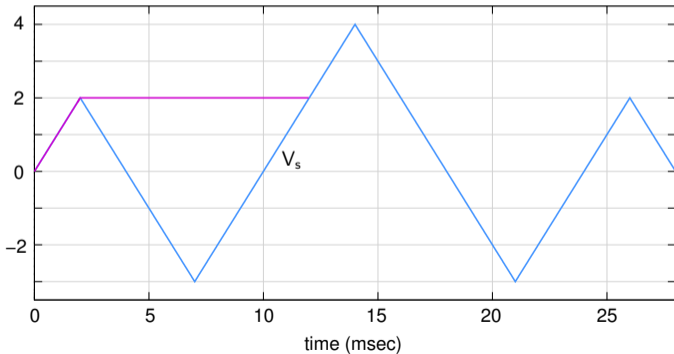
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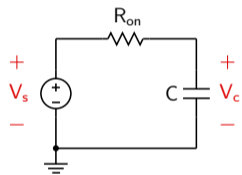
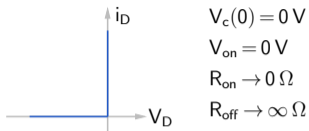
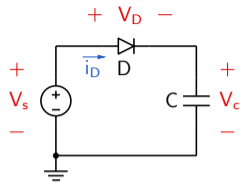


$$V_s < V_c$$

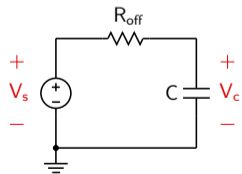
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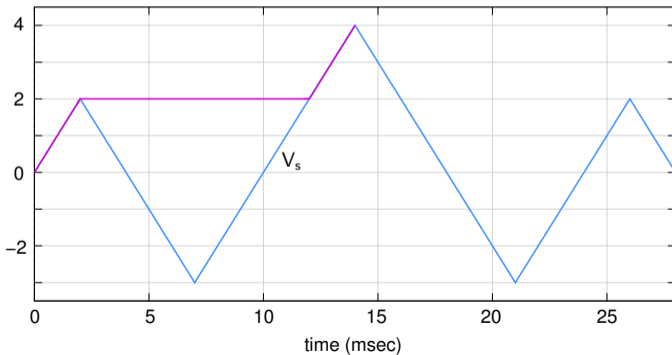
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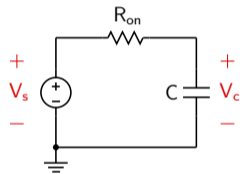
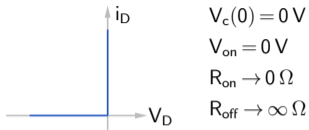
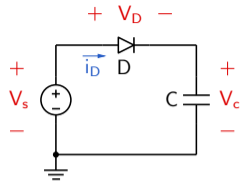
$V_s > V_c$   
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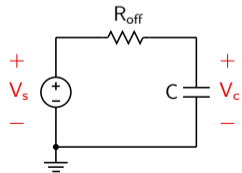
$V_s < V_c$   
 $\tau = R_{off}C$



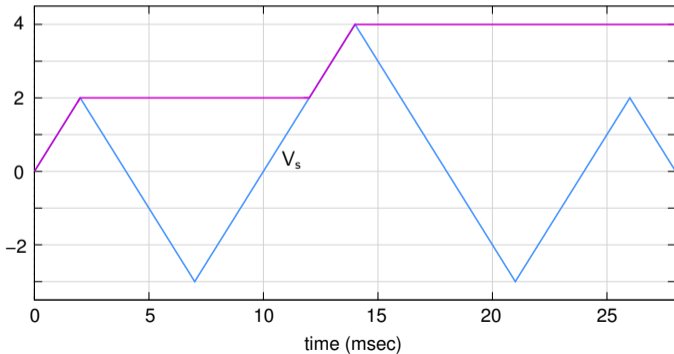
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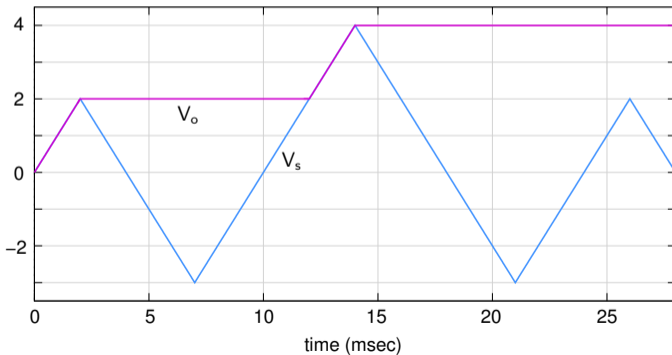
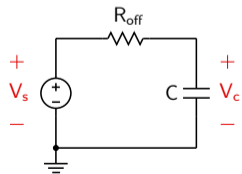
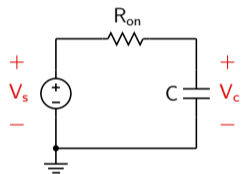
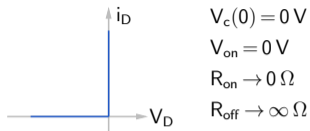
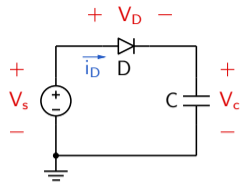
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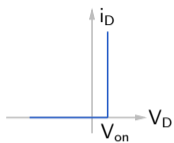
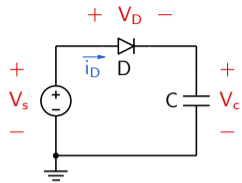


# Peak detector (with $V_{on} = 0V$ )





# Peak detector (with $V_{on} = 0.7\text{ V}$ )

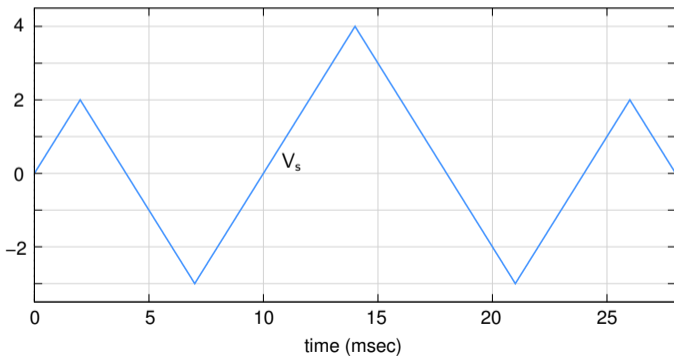


$$V_c(0) = 0\text{ V}$$

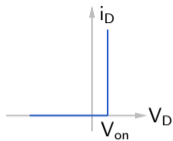
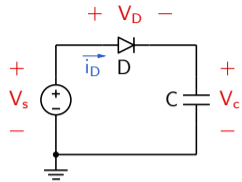
$$V_{on} = 0.7\text{ V}$$

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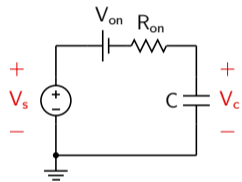


$$V_c(0) = 0\text{ V}$$

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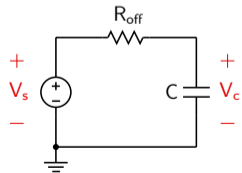
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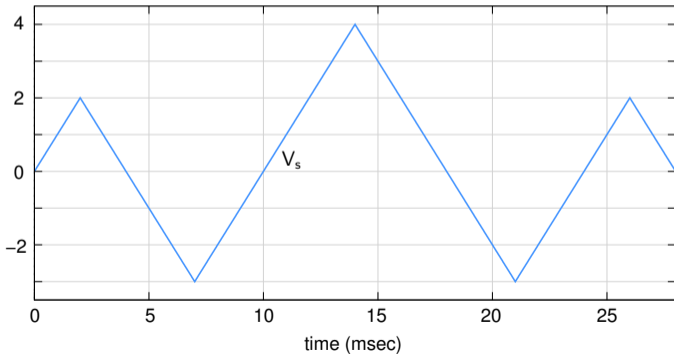
$$V_s > V_c + V_{on}$$

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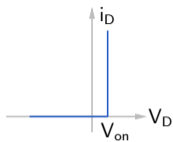
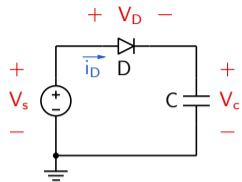


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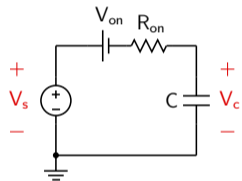


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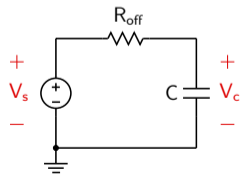
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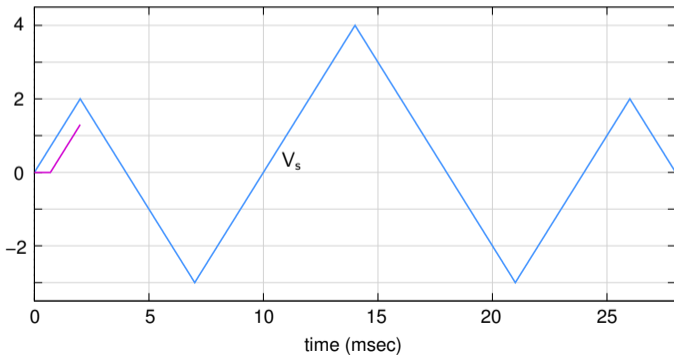
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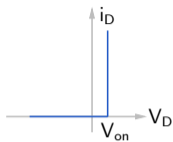
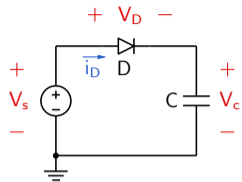


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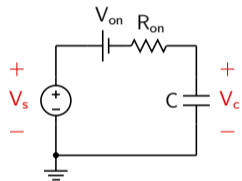


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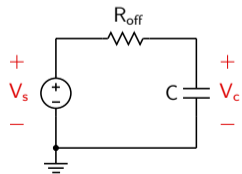
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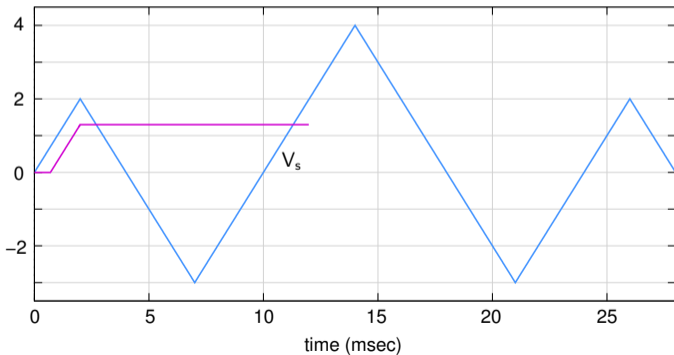
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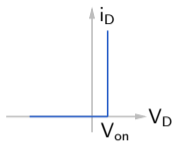
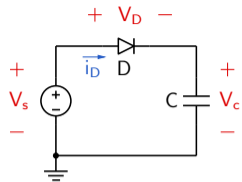


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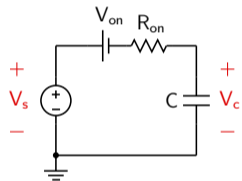


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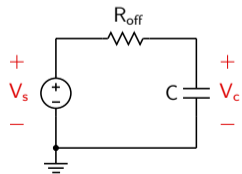
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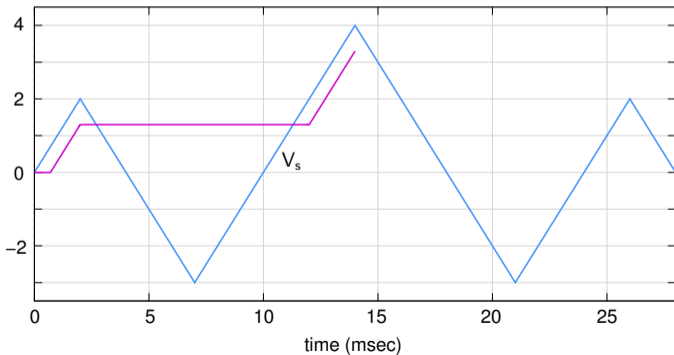
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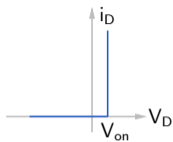
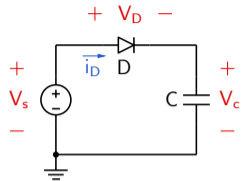


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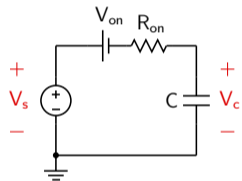


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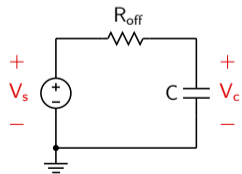
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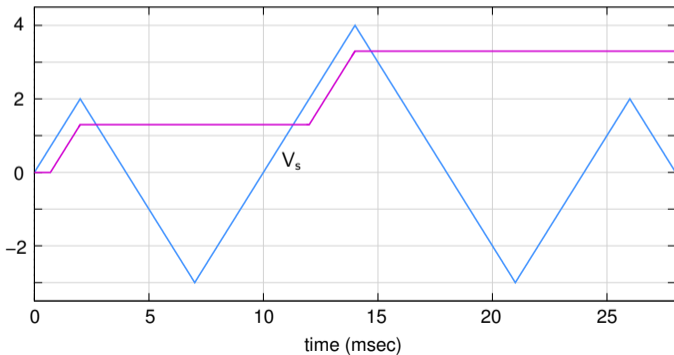
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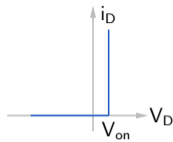
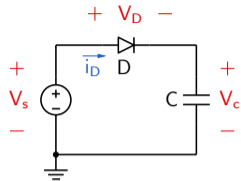


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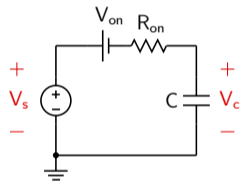


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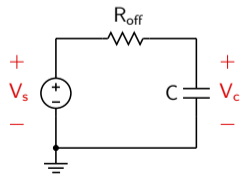
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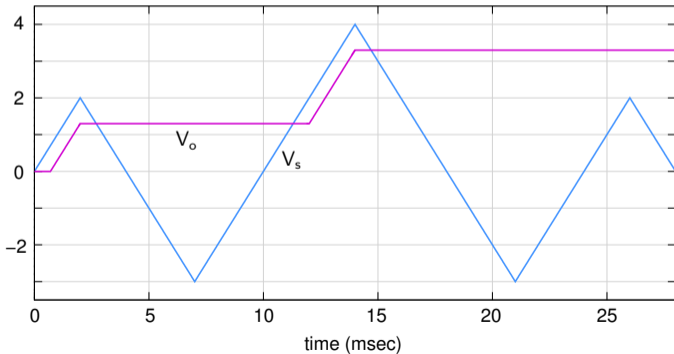
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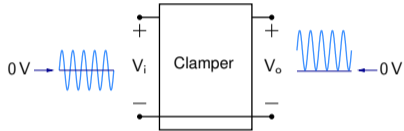


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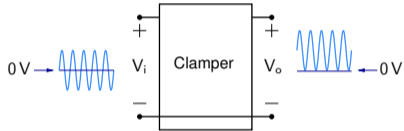
# Clamper circuits



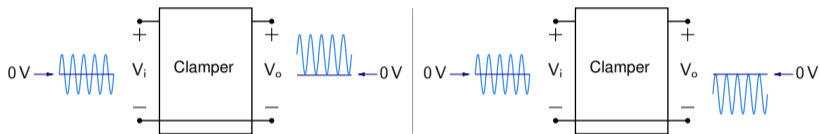
- \* A clamper circuit provides a "level shift." (The shape of the input signal is not altered.)



# Clamper circuits

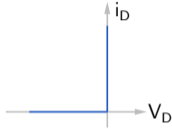
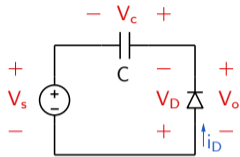


- \* A clamper circuit provides a “level shift.” (The shape of the input signal is not altered.)
- \* The shift could be positive or negative.



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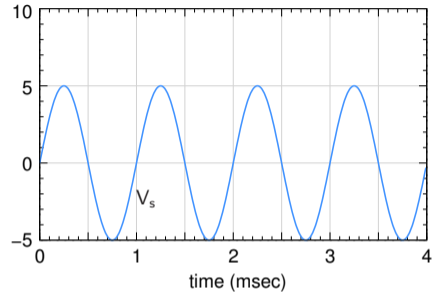
$$V_s(t) = V_m \sin \omega t$$

$$V_c(0) = 0 \text{ V}$$

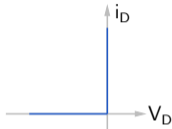
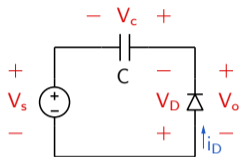
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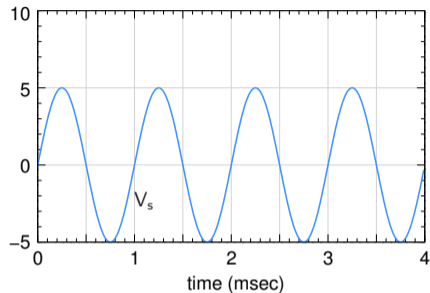
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$$V_c(0) = 0 \text{ V}$$

$$V_{on} = 0 \text{ V}$$

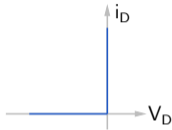
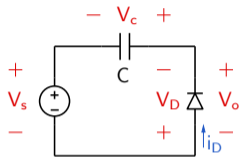
$$R_{on} \rightarrow 0 \Omega$$

$$R_{off} \rightarrow \infty \Omega$$



- \* When  $D$  conducts, the capacitor charges instantaneously since  $R_{on}$  is small. In this phase,  $V_D = 0 \rightarrow V_c + V_s = 0 \rightarrow V_c = -V_s$ .

# Clamper circuits



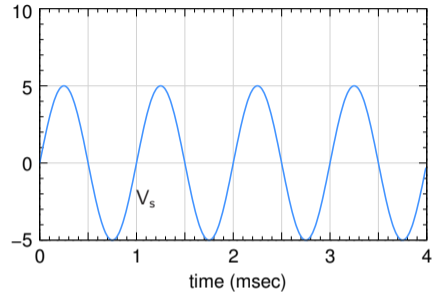
$$V_s(t) = V_m \sin \omega t$$

$$V_c(0) = 0 \text{ V}$$

$$V_{on} = 0 \text{ V}$$

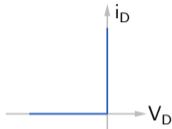
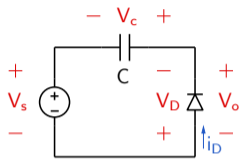
$$R_{on} \rightarrow 0 \Omega$$

$$R_{off} \rightarrow \infty \Omega$$



- \* When  $D$  conducts, the capacitor charges instantaneously since  $R_{on}$  is small. In this phase,  $V_D = 0 \rightarrow V_c + V_s = 0 \rightarrow V_c = -V_s$ .
- \*  $V_c$  can only increase since a decrease in  $V_c$  would require the diode to conduct in the reverse direction.

# Clamper circuits



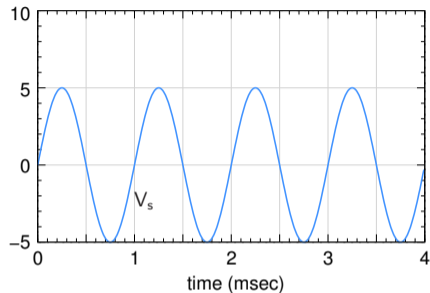
$$V_s(t) = V_m \sin \omega t$$

$$V_c(0) = 0 \text{ V}$$

$$V_{on} = 0 \text{ V}$$

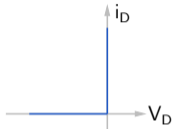
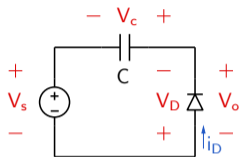
$$R_{on} \rightarrow 0 \Omega$$

$$R_{off} \rightarrow \infty \Omega$$



- \* When  $D$  conducts, the capacitor charges instantaneously since  $R_{on}$  is small. In this phase,  $V_D = 0 \rightarrow V_c + V_s = 0 \rightarrow V_c = -V_s$ .
- \*  $V_c$  can only increase since a decrease in  $V_c$  would require the diode to conduct in the reverse direction.
- \* After  $V_c$  reaches its maximum value ( $V_m$ ), it cannot change any more. We then have  $V_o(t) = V_s(t) + V_c(t) = V_s(t) + V_m$ , i.e., a positive level shift.

# Clamper circuits



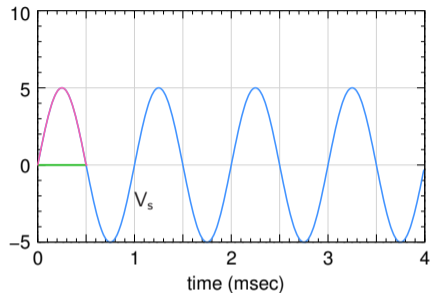
$$V_s(t) = V_m \sin \omega t$$

$$V_c(0) = 0 \text{ V}$$

$$V_{on} = 0 \text{ V}$$

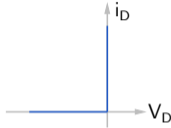
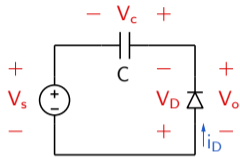
$$R_{on} \rightarrow 0 \Omega$$

$$R_{off} \rightarrow \infty \Omega$$



- \* When  $D$  conducts, the capacitor charges instantaneously since  $R_{on}$  is small. In this phase,  $V_D = 0 \rightarrow V_c + V_s = 0 \rightarrow V_c = -V_s$ .
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# Clamper circuits



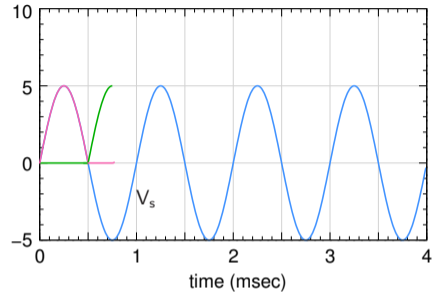
$$V_s(t) = V_m \sin \omega t$$

$$V_c(0) = 0 \text{ V}$$

$$V_{on} = 0 \text{ V}$$

$$R_{on} \rightarrow 0 \Omega$$

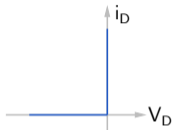
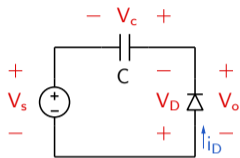
$$R_{off} \rightarrow \infty \Omega$$



- \* When  $D$  conducts, the capacitor charges instantaneously since  $R_{on}$  is small. In this phase,  $V_D = 0 \rightarrow V_c + V_s = 0 \rightarrow V_c = -V_s$ .
- \*  $V_c$  can only increase since a decrease in  $V_c$  would require the diode to conduct in the reverse direction.
- \* After  $V_c$  reaches its maximum value ( $V_m$ ), it cannot change any more. We then have  $V_o(t) = V_s(t) + V_c(t) = V_s(t) + V_m$ , i.e., a positive level shift.



# Clamper circuits



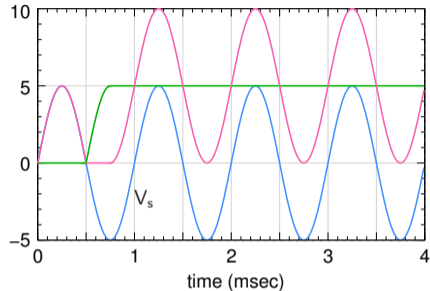
$$V_s(t) = V_m \sin \omega t$$

$$V_c(0) = 0 \text{ V}$$

$$V_{on} = 0 \text{ V}$$

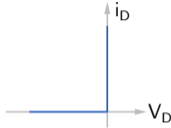
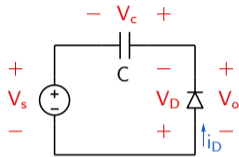
$$R_{on} \rightarrow 0 \Omega$$

$$R_{off} \rightarrow \infty \Omega$$



- \* When  $D$  conducts, the capacitor charges instantaneously since  $R_{on}$  is small. In this phase,  $V_D = 0 \rightarrow V_c + V_s = 0 \rightarrow V_c = -V_s$ .
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# Clamper circuits



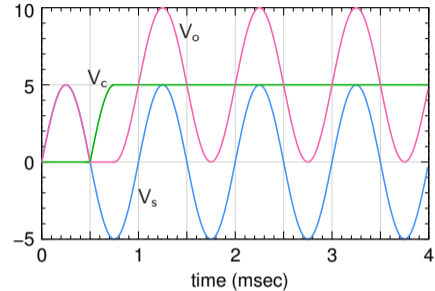
$$V_s(t) = V_m \sin \omega t$$

$$V_c(0) = 0 \text{ V}$$

$$V_{on} = 0 \text{ V}$$

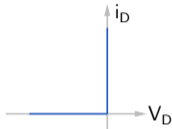
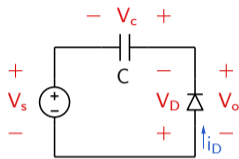
$$R_{on} \rightarrow 0 \Omega$$

$$R_{off} \rightarrow \infty \Omega$$



- \* When  $D$  conducts, the capacitor charges instantaneously since  $R_{on}$  is small. In this phase,  $V_D = 0 \rightarrow V_c + V_s = 0 \rightarrow V_c = -V_s$ .
- \*  $V_c$  can only increase since a decrease in  $V_c$  would require the diode to conduct in the reverse direction.
- \* After  $V_c$  reaches its maximum value ( $V_m$ ), it cannot change any more. We then have  $V_o(t) = V_s(t) + V_c(t) = V_s(t) + V_m$ , i.e., a positive level shift.

# Clamper circuits



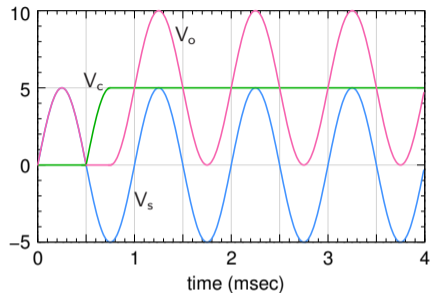
$$V_s(t) = V_m \sin \omega t$$

$$V_c(0) = 0 \text{ V}$$

$$V_{on} = 0 \text{ V}$$

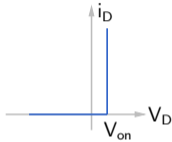
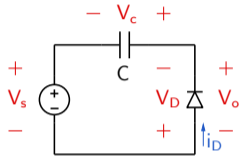
$$R_{on} \rightarrow 0 \Omega$$

$$R_{off} \rightarrow \infty \Omega$$



- \* When  $D$  conducts, the capacitor charges instantaneously since  $R_{on}$  is small. In this phase,  $V_D = 0 \rightarrow V_c + V_s = 0 \rightarrow V_c = -V_s$ .
- \*  $V_c$  can only increase since a decrease in  $V_c$  would require the diode to conduct in the reverse direction.
- \* After  $V_c$  reaches its maximum value ( $V_m$ ), it cannot change any more. We then have  $V_o(t) = V_s(t) + V_c(t) = V_s(t) + V_m$ , i.e., a positive level shift.
- \* Note that we are generally interested only in the steady-state behaviour and not in the transient at the beginning.

# Clamper circuits



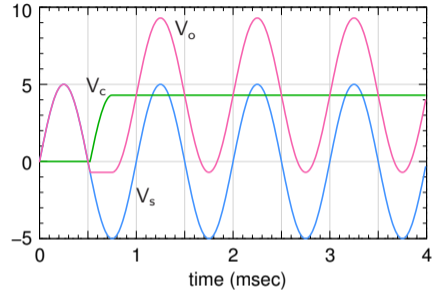
$$V_s(t) = V_m \sin \omega t$$

$$V_c(0) = 0 \text{ V}$$

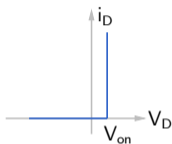
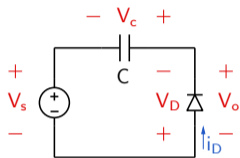
$$V_{on} = 0.7 \text{ V}$$

$$R_{on} \rightarrow 0 \Omega$$

$$R_{off} \rightarrow \infty \Omega$$



# Clamper circuits



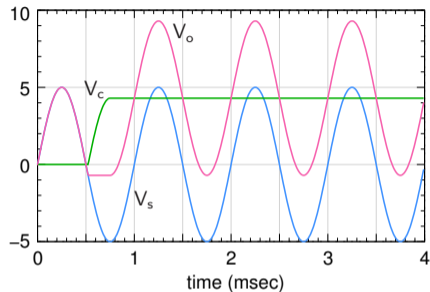
$$V_s(t) = V_m \sin \omega t$$

$$V_c(0) = 0 \text{ V}$$

$$V_{on} = 0.7 \text{ V}$$

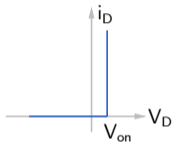
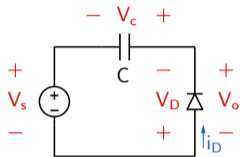
$$R_{on} \rightarrow 0 \Omega$$

$$R_{off} \rightarrow \infty \Omega$$



- \* When  $D$  conducts, the capacitor charges instantaneously since  $R_{on}$  is small (as in the last circuit).  
In this phase,  
 $V_c + V_s + V_{on} = 0 \rightarrow V_c = -V_s - V_{on}$ .

# Clamper circuits



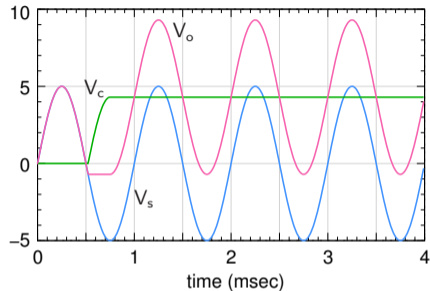
$$V_s(t) = V_m \sin \omega t$$

$$V_c(0) = 0 \text{ V}$$

$$V_{on} = 0.7 \text{ V}$$

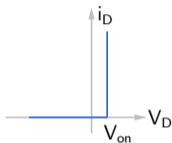
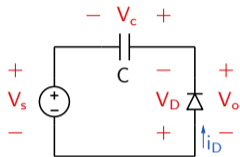
$$R_{on} \rightarrow 0 \Omega$$

$$R_{off} \rightarrow \infty \Omega$$



- \* When  $D$  conducts, the capacitor charges instantaneously since  $R_{on}$  is small (as in the last circuit). In this phase,  
 $V_c + V_s + V_{on} = 0 \rightarrow V_c = -V_s - V_{on}$ .
- \*  $V_c$  can only increase since a decrease in  $V_c$  would require the diode to conduct in the reverse direction.

# Clamper circuits



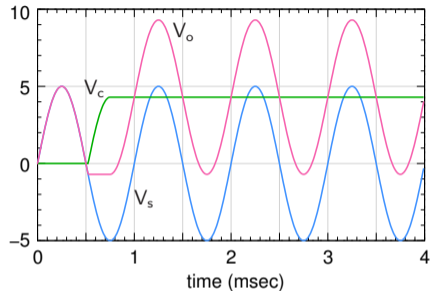
$$V_s(t) = V_m \sin \omega t$$

$$V_c(0) = 0 \text{ V}$$

$$V_{on} = 0.7 \text{ V}$$

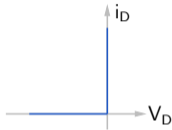
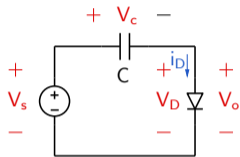
$$R_{on} \rightarrow 0 \Omega$$

$$R_{off} \rightarrow \infty \Omega$$



- \* When  $D$  conducts, the capacitor charges instantaneously since  $R_{on}$  is small (as in the last circuit). In this phase,  
 $V_c + V_s + V_{on} = 0 \rightarrow V_c = -V_s - V_{on}$ .
- \*  $V_c$  can only increase since a decrease in  $V_c$  would require the diode to conduct in the reverse direction.
- \* After  $V_c$  reaches its maximum value ( $V_m - V_{on}$ ), it cannot change any more. We then have  
 $V_o(t) = V_s(t) + V_c(t) = V_s(t) + V_m - V_{on}$ . In this case,  $V_o$  gets clamped at  $-0.7 \text{ V}$ .

# Clamper circuits



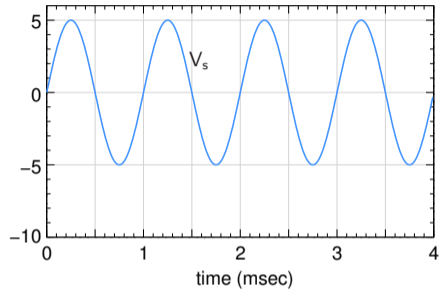
$$V_s(t) = V_m \sin \omega t$$

$$V_c(0) = 0 \text{ V}$$

$$V_{on} = 0 \text{ V}$$

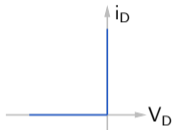
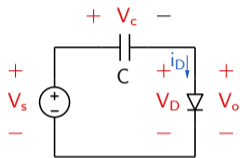
$$R_{on} \rightarrow 0 \Omega$$

$$R_{off} \rightarrow \infty \Omega$$





# Clamper circuits



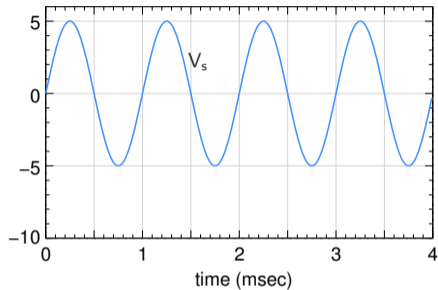
$$V_s(t) = V_m \sin \omega t$$

$$V_c(0) = 0 \text{ V}$$

$$V_{on} = 0 \text{ V}$$

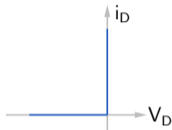
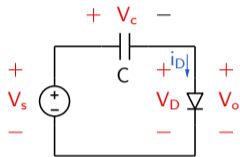
$$R_{on} \rightarrow 0 \Omega$$

$$R_{off} \rightarrow \infty \Omega$$



- \* When  $D$  conducts, the capacitor charges instantaneously since  $R_{on}$  is small. In this phase,  $V_D = 0 \rightarrow V_c - V_s = 0 \rightarrow V_c = V_s$ .

# Clamper circuits



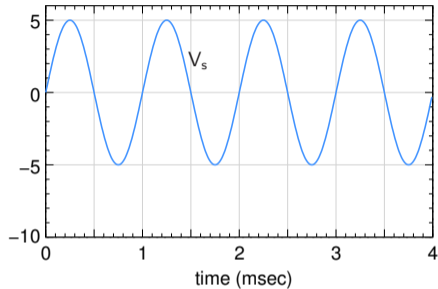
$$V_s(t) = V_m \sin \omega t$$

$$V_c(0) = 0 \text{ V}$$

$$V_{on} = 0 \text{ V}$$

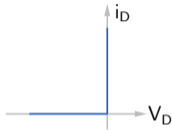
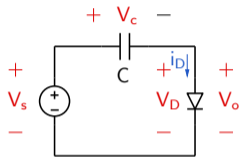
$$R_{on} \rightarrow 0 \Omega$$

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- \*  $V_c$  can only increase since a decrease in  $V_c$  would require the diode to conduct in the reverse direction.

# Clamper circuits



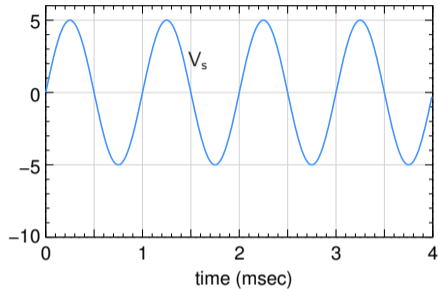
$$V_s(t) = V_m \sin \omega t$$

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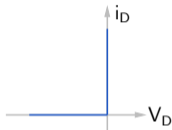
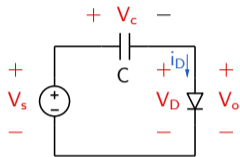
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- \* After  $V_c$  reaches its maximum value ( $V_m$ ), it cannot change any more. We then have  $V_o(t) = V_s(t) - V_c(t) = V_s(t) - V_m$ , i.e., a negative level shift.

# Clamper circuits



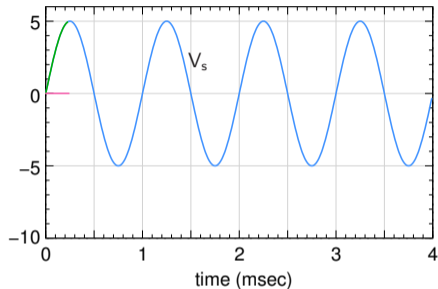
$$V_s(t) = V_m \sin \omega t$$

$$V_c(0) = 0 \text{ V}$$

$$V_{on} = 0 \text{ V}$$

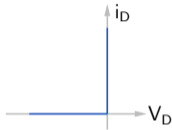
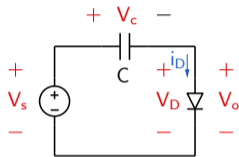
$$R_{on} \rightarrow 0 \Omega$$

$$R_{off} \rightarrow \infty \Omega$$



- \* When  $D$  conducts, the capacitor charges instantaneously since  $R_{on}$  is small. In this phase,  $V_D = 0 \rightarrow V_c - V_s = 0 \rightarrow V_c = V_s$ .
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# Clamper circuits



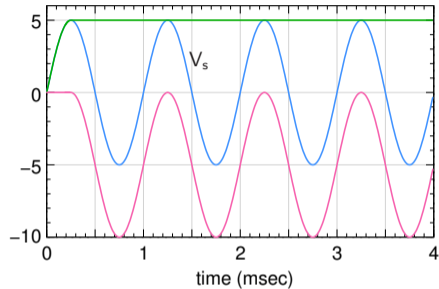
$$V_s(t) = V_m \sin \omega t$$

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$$V_{on} = 0 \text{ V}$$

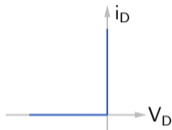
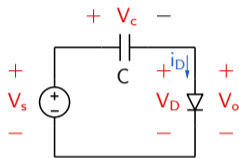
$$R_{on} \rightarrow 0 \Omega$$

$$R_{off} \rightarrow \infty \Omega$$



- \* When  $D$  conducts, the capacitor charges instantaneously since  $R_{on}$  is small. In this phase,  $V_D = 0 \rightarrow V_c - V_s = 0 \rightarrow V_c = V_s$ .
- \*  $V_c$  can only increase since a decrease in  $V_c$  would require the diode to conduct in the reverse direction.
- \* After  $V_c$  reaches its maximum value ( $V_m$ ), it cannot change any more. We then have  $V_o(t) = V_s(t) - V_c(t) = V_s(t) - V_m$ , i.e., a negative level shift.

# Clamper circuits



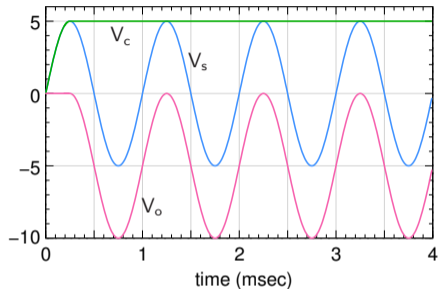
$$V_s(t) = V_m \sin \omega t$$

$$V_c(0) = 0 \text{ V}$$

$$V_{on} = 0 \text{ V}$$

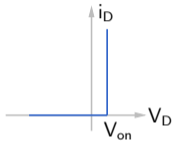
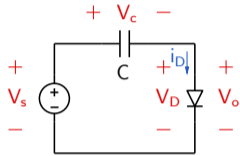
$$R_{on} \rightarrow 0 \Omega$$

$$R_{off} \rightarrow \infty \Omega$$



- \* When  $D$  conducts, the capacitor charges instantaneously since  $R_{on}$  is small. In this phase,  $V_D = 0 \rightarrow V_c - V_s = 0 \rightarrow V_c = V_s$ .
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# Clamper circuits



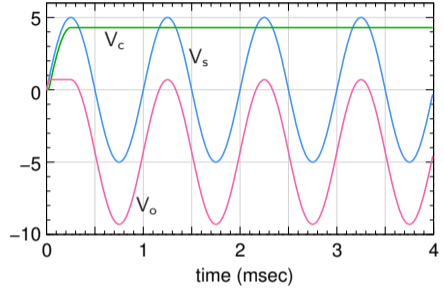
$$V_s(t) = V_m \sin \omega t$$

$$V_c(0) = 0 \text{ V}$$

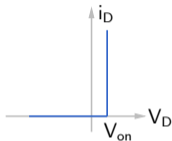
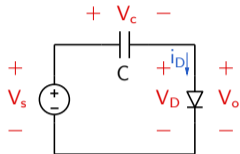
$$V_{on} = 0.7 \text{ V}$$

$$R_{on} \rightarrow 0 \Omega$$

$$R_{off} \rightarrow \infty \Omega$$



# Clamper circuits



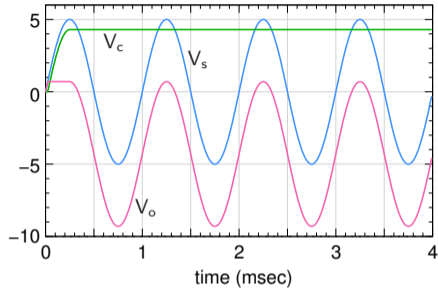
$$V_s(t) = V_m \sin \omega t$$

$$V_c(0) = 0 \text{ V}$$

$$V_{on} = 0.7 \text{ V}$$

$$R_{on} \rightarrow 0 \Omega$$

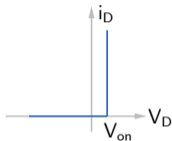
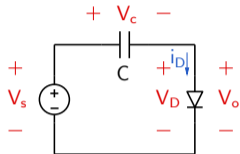
$$R_{off} \rightarrow \infty \Omega$$



- \* When  $D$  conducts, the capacitor charges instantaneously since  $R_{on}$  is small (as in the last circuit).  
In this phase,  
 $V_c + V_{on} - V_s = 0 \rightarrow V_c = V_s - V_{on}$ .



# Clamper circuits



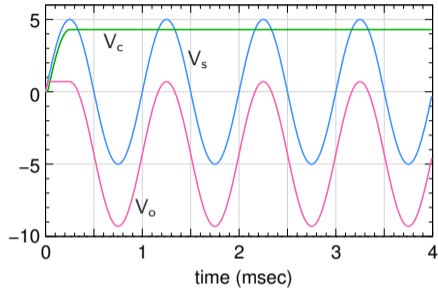
$$V_s(t) = V_m \sin \omega t$$

$$V_c(0) = 0 \text{ V}$$

$$V_{on} = 0.7 \text{ V}$$

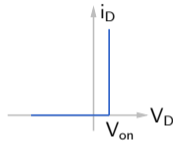
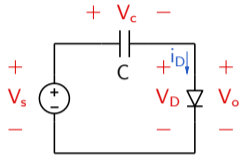
$$R_{on} \rightarrow 0 \Omega$$

$$R_{off} \rightarrow \infty \Omega$$

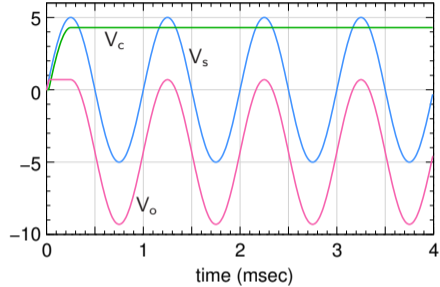


- \* When  $D$  conducts, the capacitor charges instantaneously since  $R_{on}$  is small (as in the last circuit). In this phase,  
 $V_c + V_{on} - V_s = 0 \rightarrow V_c = V_s - V_{on}$ .
- \*  $V_c$  can only increase since a decrease in  $V_c$  would require the diode to conduct in the reverse direction.

# Clamper circuits

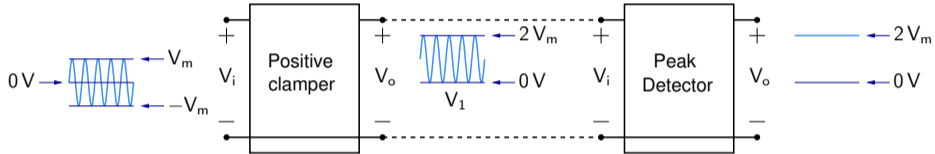


$$\begin{aligned}V_s(t) &= V_m \sin \omega t \\V_c(0) &= 0 \text{ V} \\V_{on} &= 0.7 \text{ V} \\R_{on} &\rightarrow 0 \Omega \\R_{off} &\rightarrow \infty \Omega\end{aligned}$$

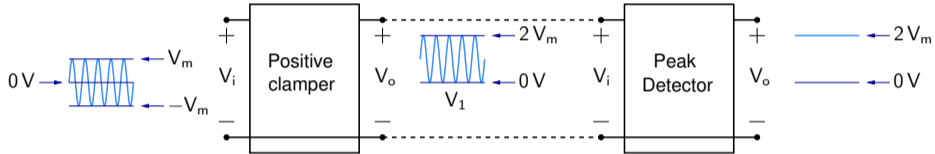


- \* When  $D$  conducts, the capacitor charges instantaneously since  $R_{on}$  is small (as in the last circuit). In this phase,  
 $V_c + V_{on} - V_s = 0 \rightarrow V_c = V_s - V_{on}$ .
- \*  $V_c$  can only increase since a decrease in  $V_c$  would require the diode to conduct in the reverse direction.
- \* After  $V_c$  reaches its maximum value ( $V_m - V_{on}$ ), it cannot change any more. We then have  $V_o(t) = V_s(t) - V_c(t) = V_s(t) - V_m + V_{on}$ . In this case,  $V_o$  gets clamped at 0.7 V.

# Voltage doubler (peak-to-peak detector)

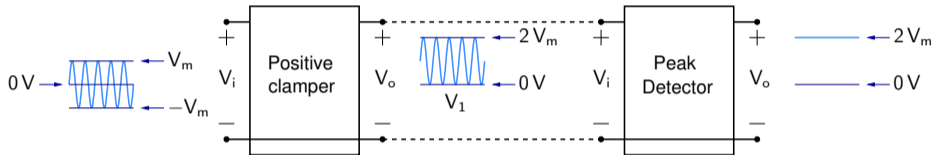


# Voltage doubler (peak-to-peak detector)



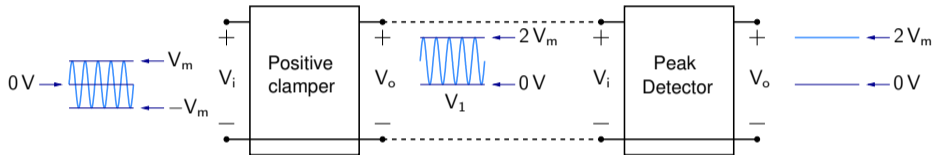
\* Input voltage:  $-V_m$  to  $V_m$

## Voltage doubler (peak-to-peak detector)



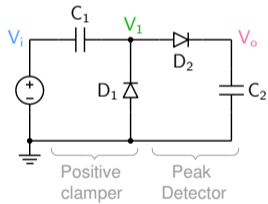
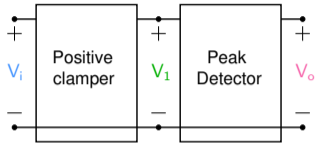
- \* Input voltage:  $-V_m$  to  $V_m$
- \* Output of positive clamper ( $V_1$ ):  $0$  to  $2V_m$

## Voltage doubler (peak-to-peak detector)

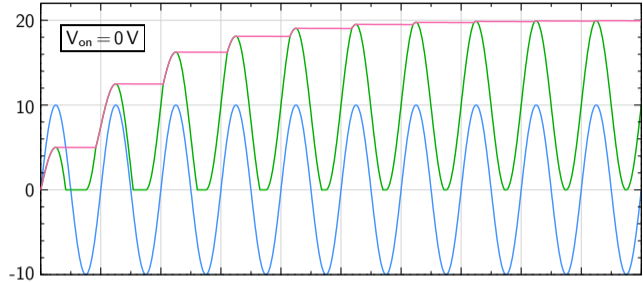
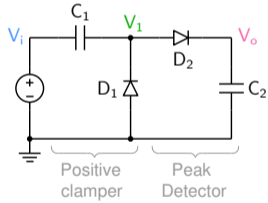
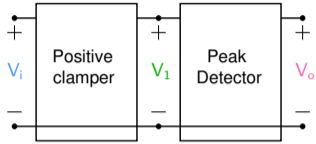


- \* Input voltage:  $-V_m$  to  $V_m$
- \* Output of positive clamper ( $V_1$ ):  $0$  to  $2V_m$
- \* The peak detector detects the peak of  $V_1(t)$ , i.e.,  $2V_m$  (dc).

# Voltage doubler (peak-to-peak detector)

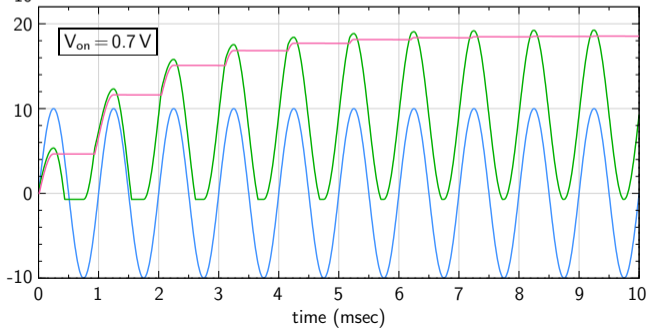
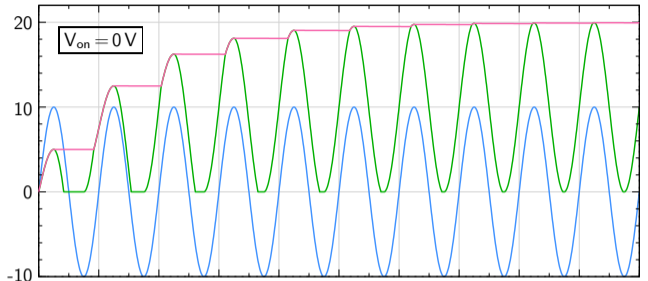
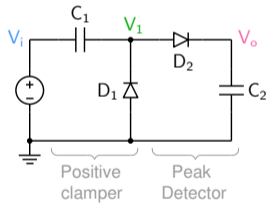
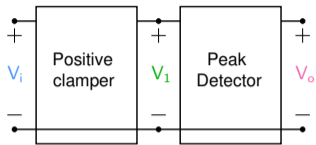


# Voltage doubler (peak-to-peak detector)

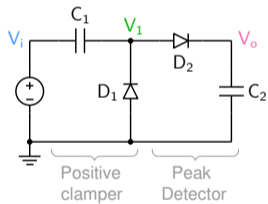
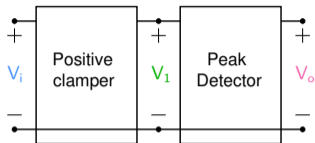




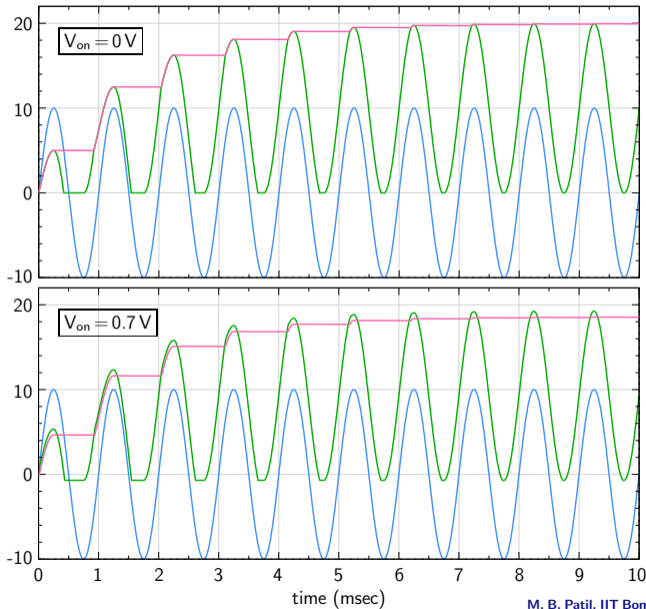
# Voltage doubler (peak-to-peak detector)



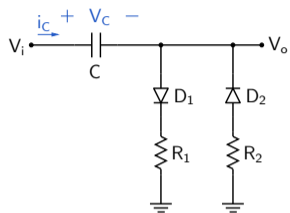
# Voltage doubler (peak-to-peak detector)



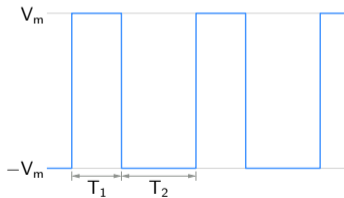
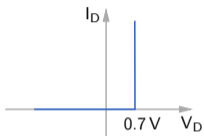
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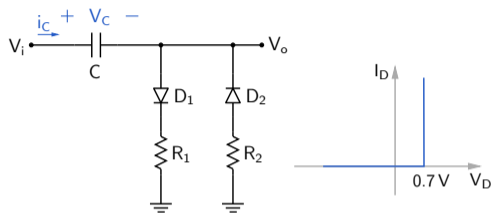
## Diode circuit example



Assuming  $R_1 C$  and  $R_2 C$  to be large compared to  $T$ , find  $V_o(t)$  in steady state.

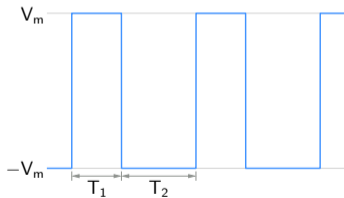


## Diode circuit example

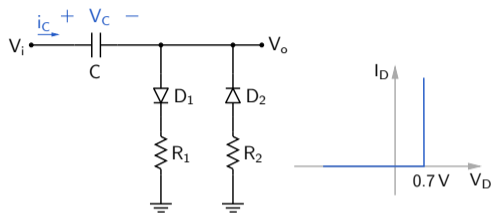


Assuming  $R_1 C$  and  $R_2 C$  to be large compared to  $T$ , find  $V_o(t)$  in steady state.

\* Charging time constant  $\tau_1 = R_1 C$ .

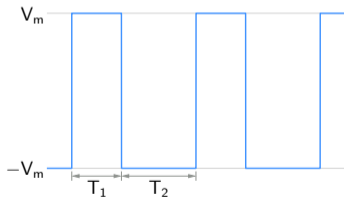


## Diode circuit example

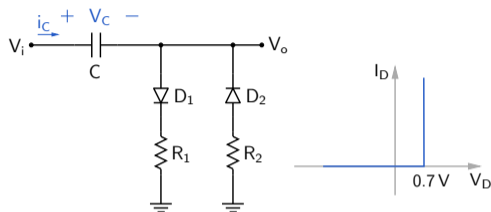


Assuming  $R_1 C$  and  $R_2 C$  to be large compared to  $T$ , find  $V_o(t)$  in steady state.

- \* Charging time constant  $\tau_1 = R_1 C$ .
- \* Discharging time constant  $\tau_2 = R_2 C$ .

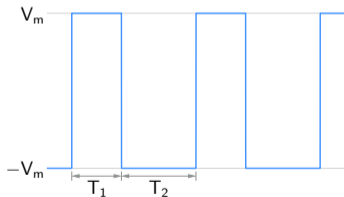


## Diode circuit example

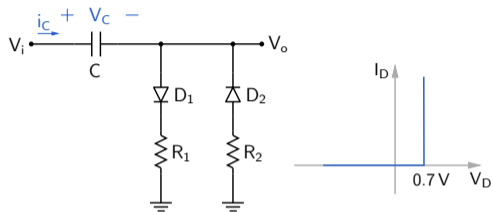


Assuming  $R_1 C$  and  $R_2 C$  to be large compared to  $T$ , find  $V_o(t)$  in steady state.

- \* Charging time constant  $\tau_1 = R_1 C$ .
- \* Discharging time constant  $\tau_2 = R_2 C$ .
- \* Since  $\tau_1 \gg T$  and  $\tau_2 \gg T$ , we expect  $V_C$  to be nearly constant in steady state, i.e.,  $V_C(t) \approx \text{constant} \equiv V_C^0$ .

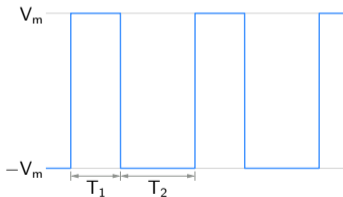


## Diode circuit example

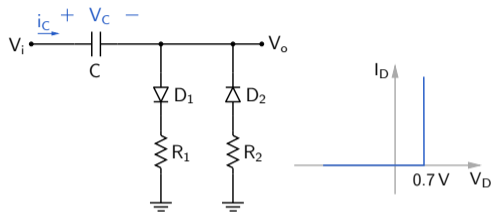


Assuming  $R_1 C$  and  $R_2 C$  to be large compared to  $T$ , find  $V_o(t)$  in steady state.

- \* Charging time constant  $\tau_1 = R_1 C$ .
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- \*  $V_o(t) = V_i(t) - V_C(t) \approx V_i(t) - V_C^0$ .



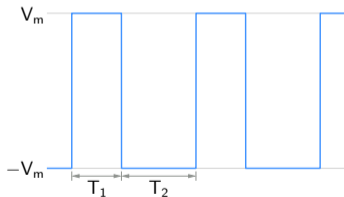
## Diode circuit example



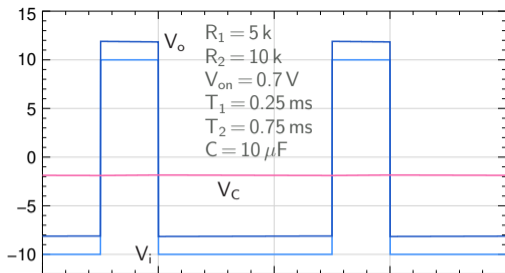
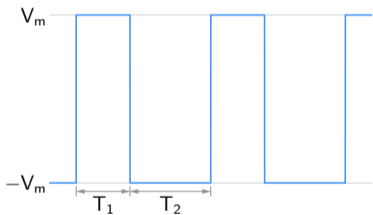
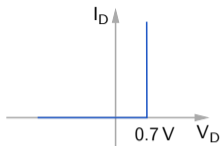
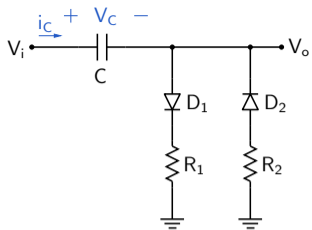
Assuming  $R_1 C$  and  $R_2 C$  to be large compared to  $T$ , find  $V_o(t)$  in steady state.

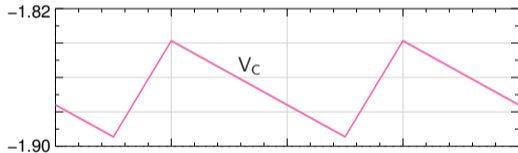
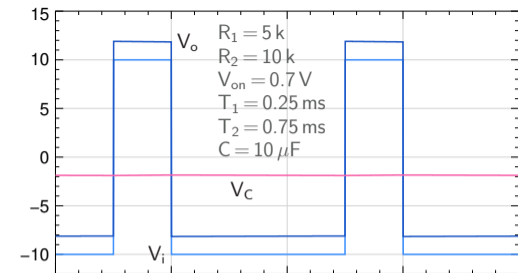
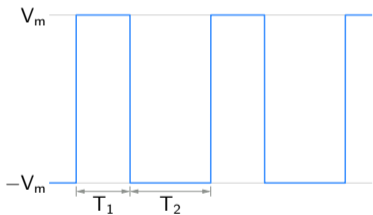
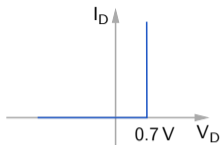
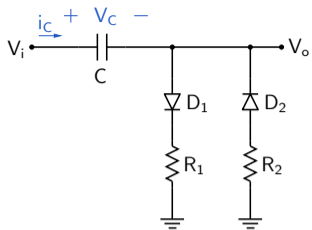
- \* Charging time constant  $\tau_1 = R_1 C$ .
- \* Discharging time constant  $\tau_2 = R_2 C$ .
- \* Since  $\tau_1 \gg T$  and  $\tau_2 \gg T$ , we expect  $V_C$  to be nearly constant in steady state, i.e.,  $V_C(t) \approx \text{constant} \equiv V_C^0$ .
- \*  $V_o(t) = V_i(t) - V_C(t) \approx V_i(t) - V_C^0$ .

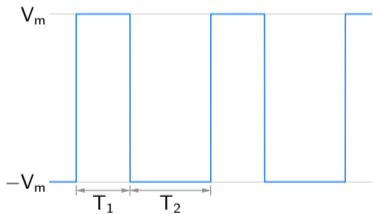
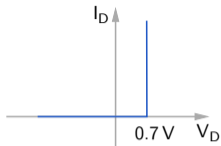
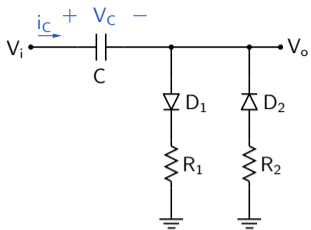
Let us look at an example.



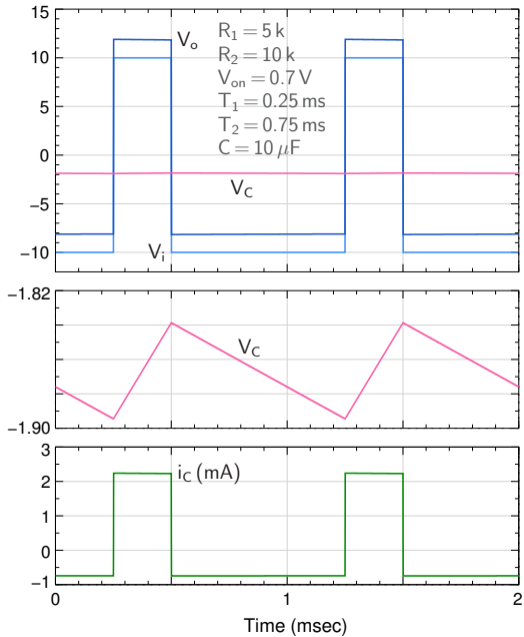


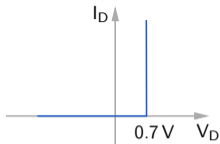
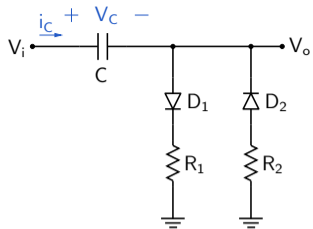




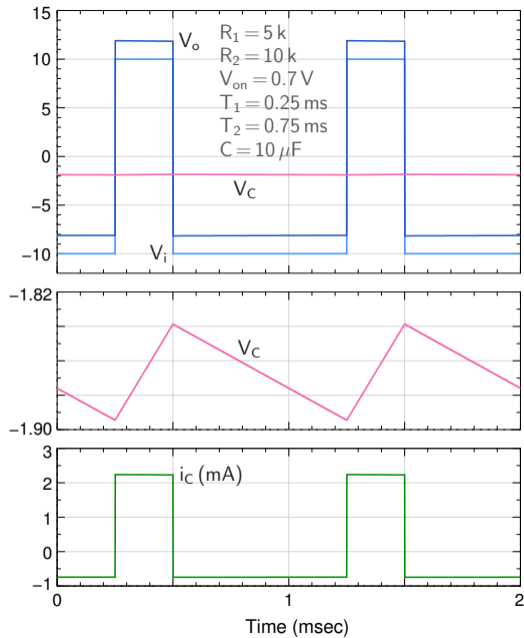


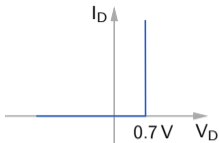
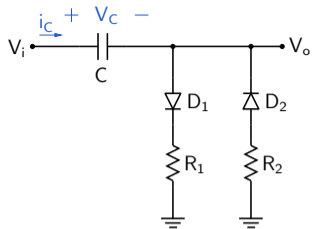
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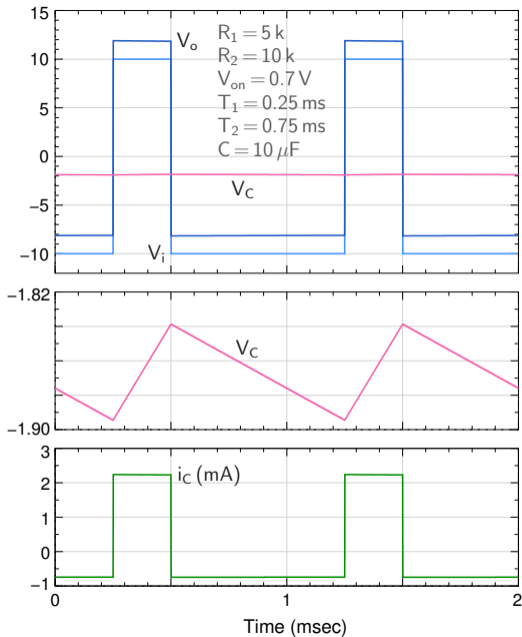
Charge conservation:

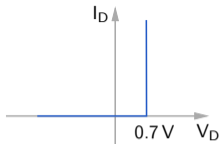
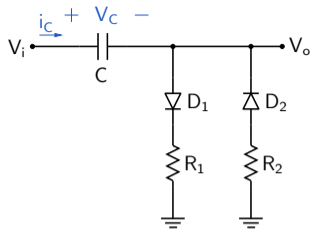




Charge conservation:

$$\Delta Q = \int_0^T i_c dt = \int_0^{T_1} i_c dt + \int_{T_1}^{T_1+T_2} i_c dt = 0.$$

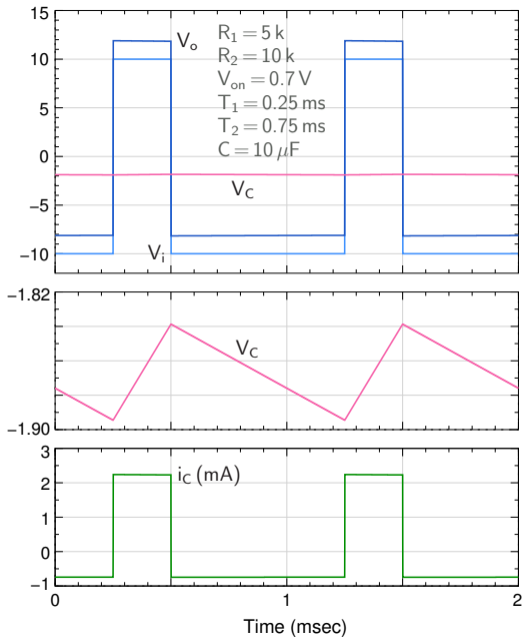


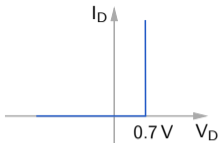
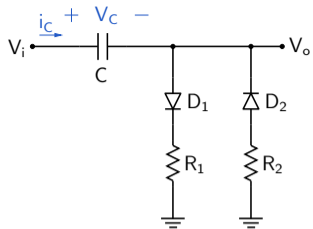


Charge conservation:

$$\Delta Q = \int_0^T i_C dt = \int_0^{T_1} i_C dt + \int_{T_1}^{T_1+T_2} i_C dt = 0.$$

$$T_1 \left( \frac{V_m - V_C - V_{on}}{R_1} \right) - T_2 \left( \frac{0 - (-V_m - V_C) - V_{on}}{R_2} \right) = 0.$$



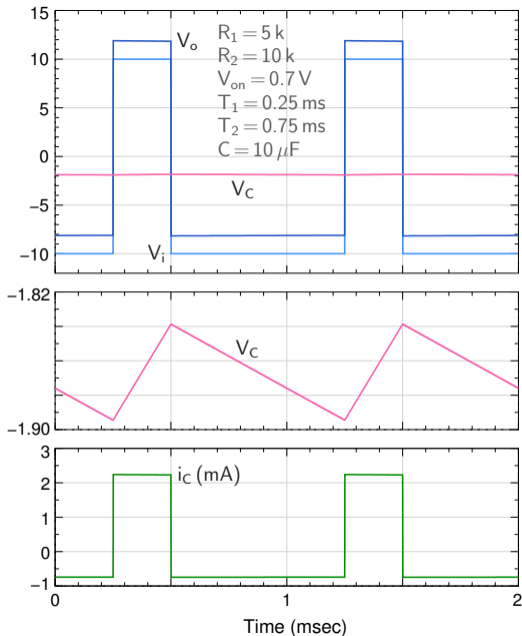


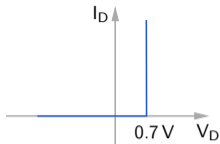
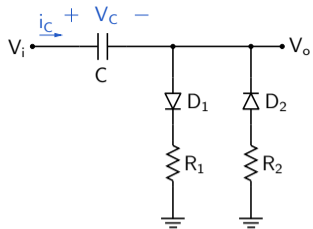
Charge conservation:

$$\Delta Q = \int_0^T i_C dt = \int_0^{T_1} i_C dt + \int_{T_1}^{T_1+T_2} i_C dt = 0.$$

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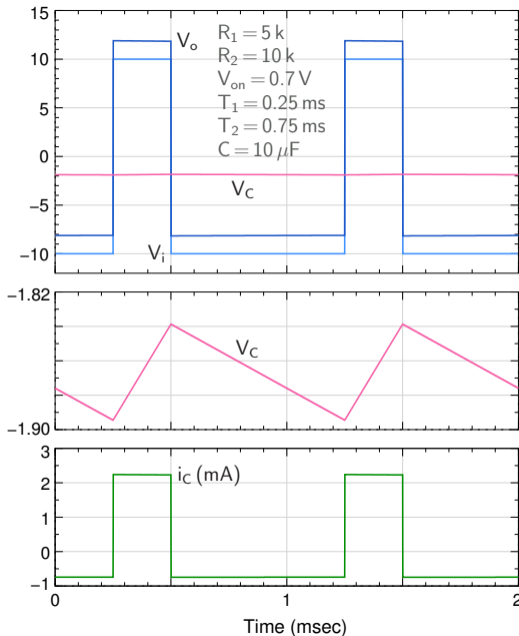
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$$\rightarrow V_C = \frac{\left( \frac{T_1}{R_1} - \frac{T_2}{R_2} \right)}{\left( \frac{T_1}{R_1} + \frac{T_2}{R_2} \right)} (V_m - V_{on}) = -1.86 \text{ V}.$$

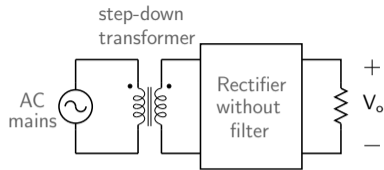




- \* A rectifier is used to convert an AC voltage to a DC voltage (typically 5 to 20 V), e.g., a mobile phone charger.

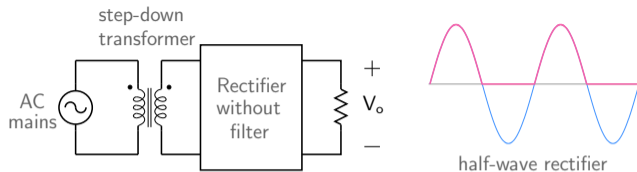
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# Rectifiers



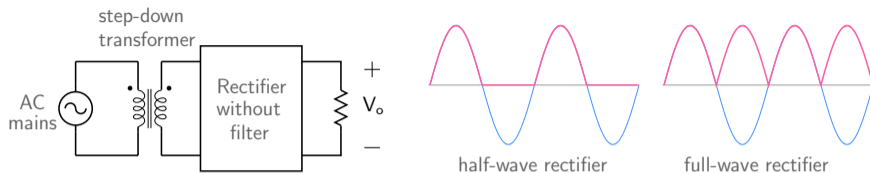
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# Rectifiers



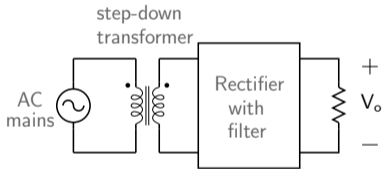
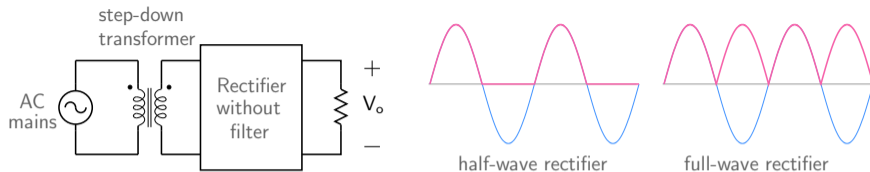
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# Rectifiers



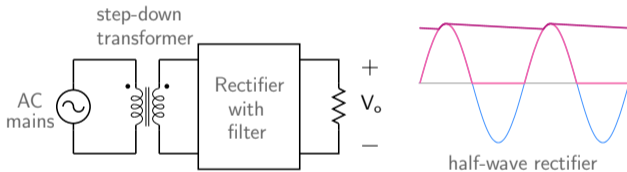
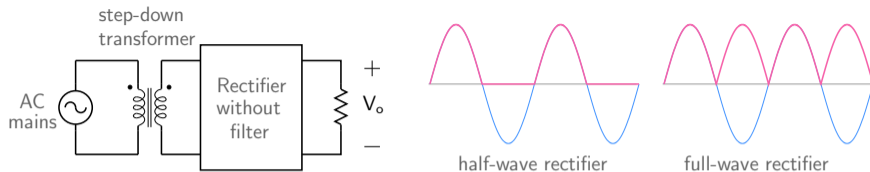
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# Rectifiers



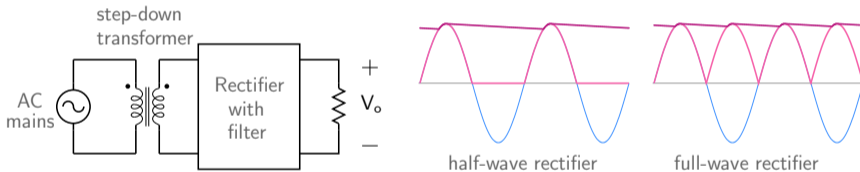
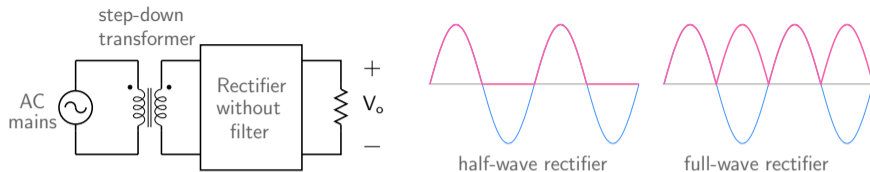
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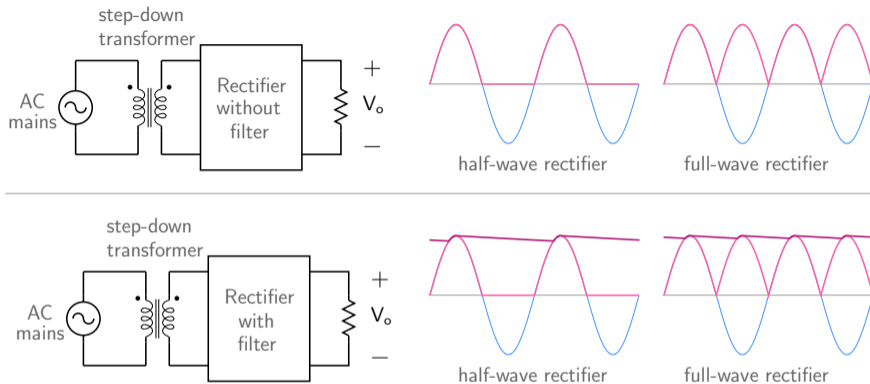
# Rectifiers



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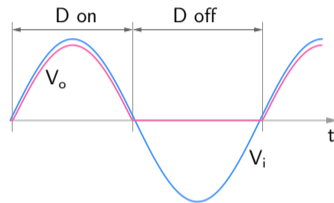
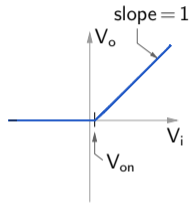
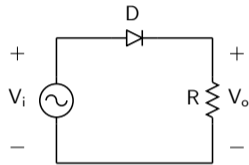


# Rectifiers

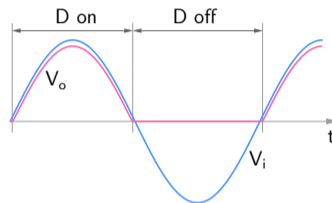
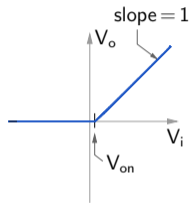
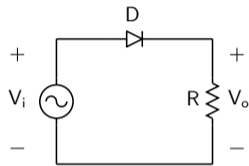


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- \* A voltage regulator would be typically used to remove the ripple riding on the DC output.

# Half-wave rectifier without filter

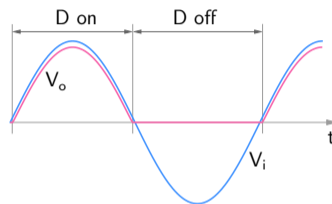
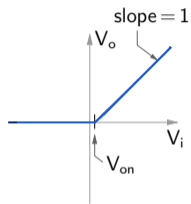
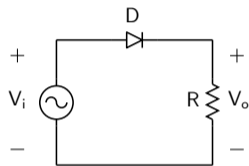


## Half-wave rectifier without filter



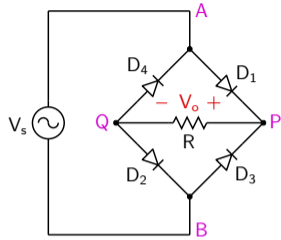
\*  $D$  conducts only if  $V_i > V_{on}$ , and in that case  $V_o = V_i - V_{on}$ , a straight line with slope = 1.

## Half-wave rectifier without filter

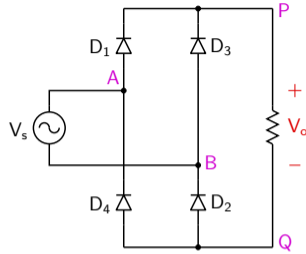
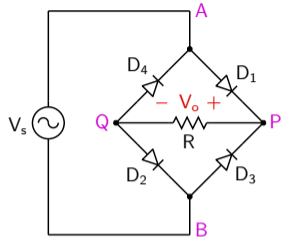


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- \* If  $V_i < V_{on}$ ,  $D$  does not conduct  $\rightarrow V_o = 0$ .

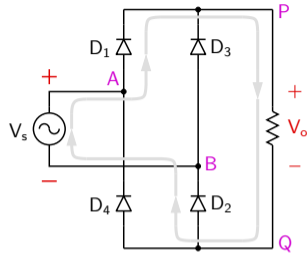
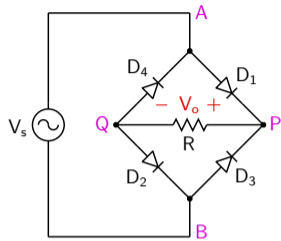
# Full-wave (bridge) rectifier without filter



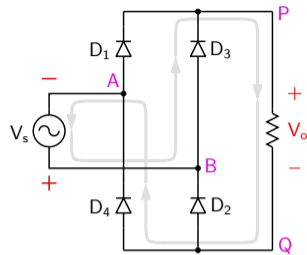
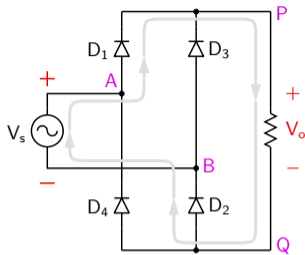
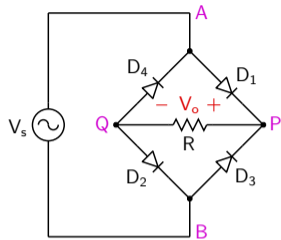
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# Full-wave (bridge) rectifier without filter

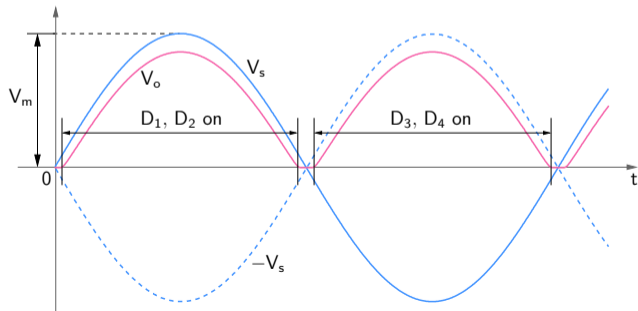
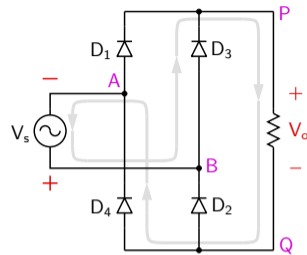
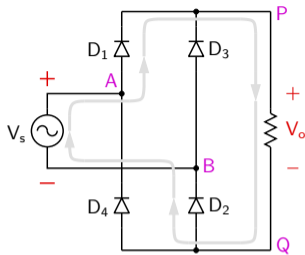
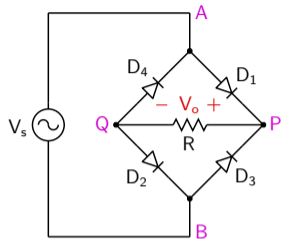


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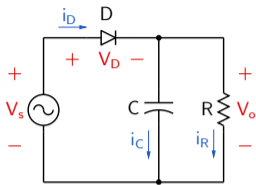




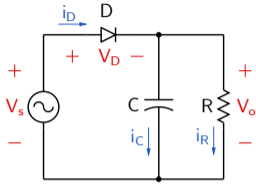
# Full-wave (bridge) rectifier without filter



## Half-wave rectifier with capacitor filter

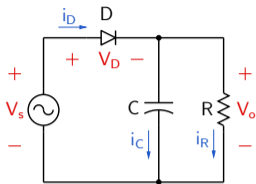


## Half-wave rectifier with capacitor filter

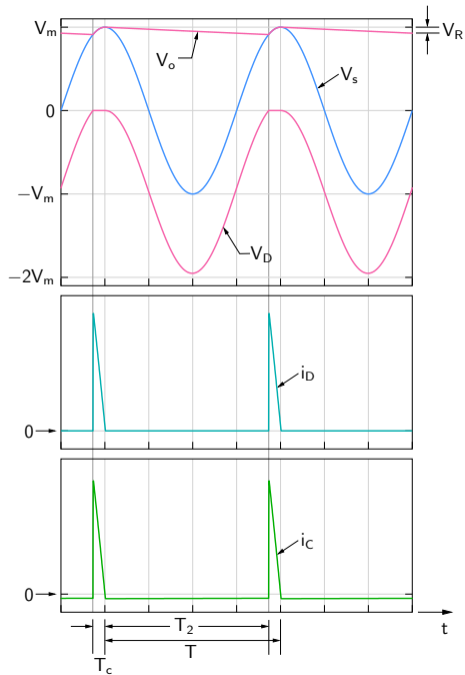


- \* Similar to the peak detector except that the load resistance provides a discharge path for the capacitor in this case.

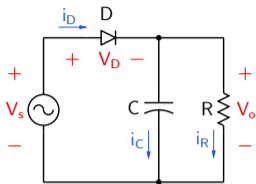
## Half-wave rectifier with capacitor filter



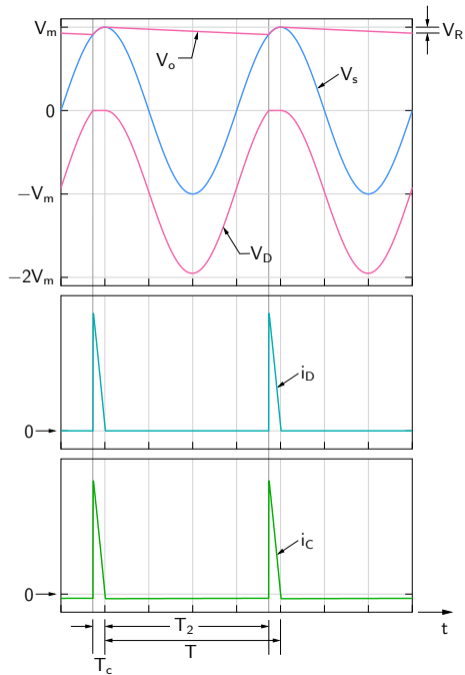
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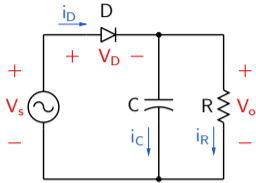
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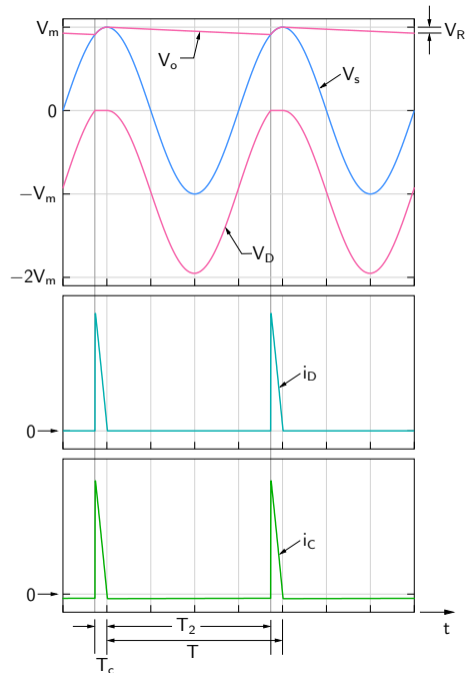
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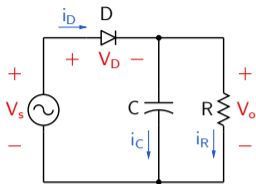
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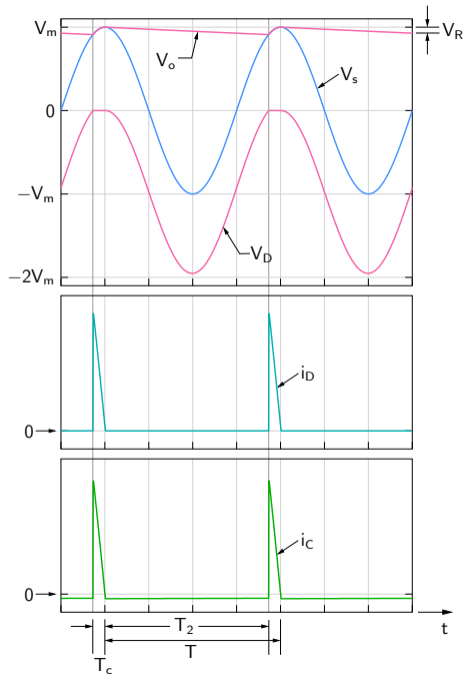
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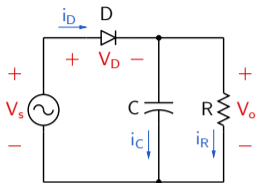
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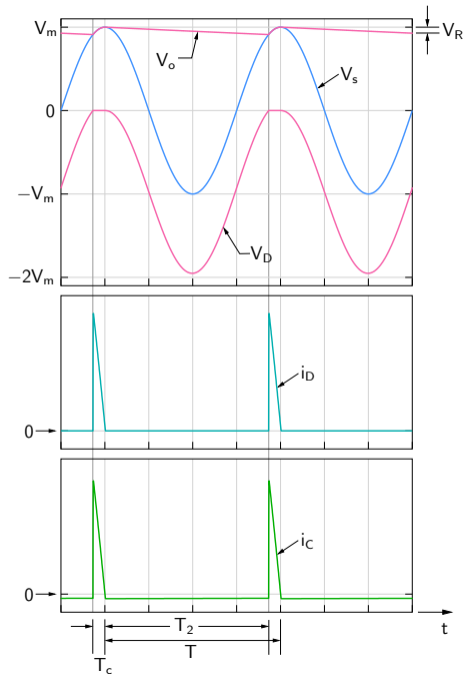
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 $\rightarrow$  The maximum reverse bias ("Peak Inverse Voltage" or PIV) across the diode is  $2V_m$ .



## Half-wave rectifier with capacitor filter

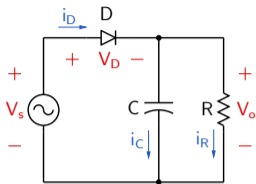


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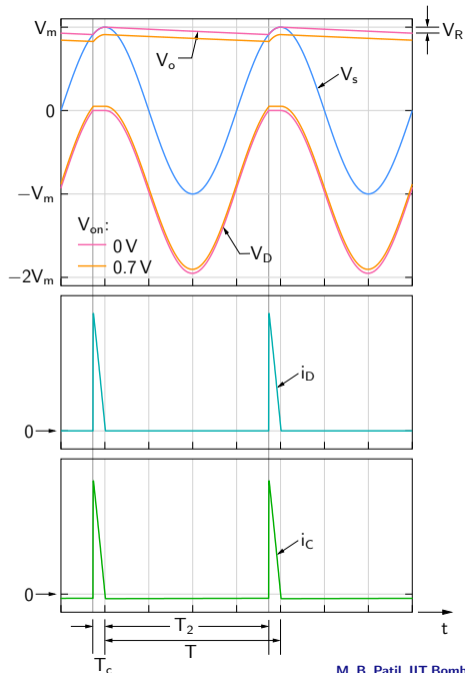




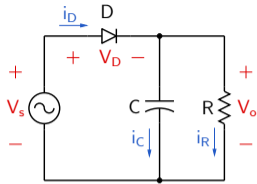
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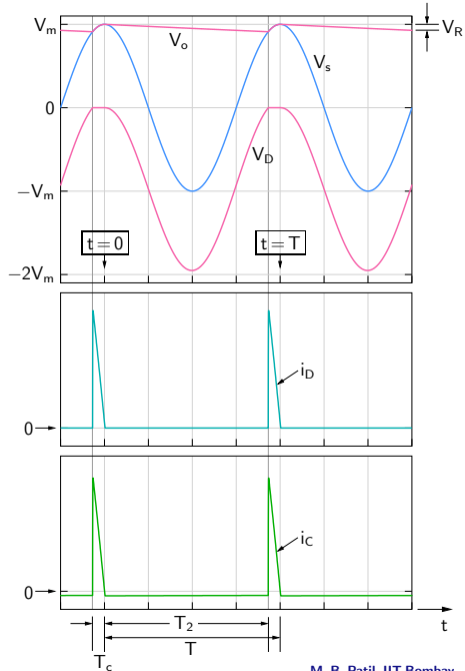
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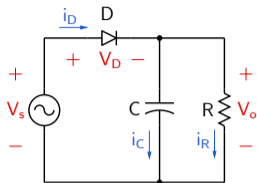
## Half-wave rectifier with capacitor filter



$V_m = 16\text{ V}$ ,  $f = 50\text{ Hz}$ ,  $R = 100\ \Omega$ . For a ripple voltage  $V_R = 2\text{ V}$ , find (a) the filter capacitance  $C$ , (b) average and peak diode currents, (c) maximum reverse voltage across the diode. (Let  $V_{on} = 0\text{ V}$ .)



## Half-wave rectifier with capacitor filter

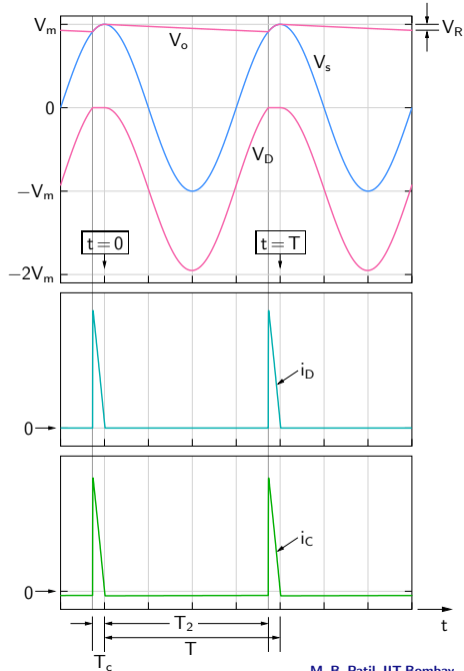


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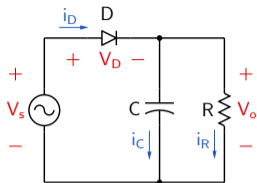
(a) filter capacitance

1. In the discharge phase,

$$V_o(t) = V_m e^{-t/\tau} \approx V_m \left(1 - \frac{t}{\tau}\right).$$



## Half-wave rectifier with capacitor filter



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(a) filter capacitance

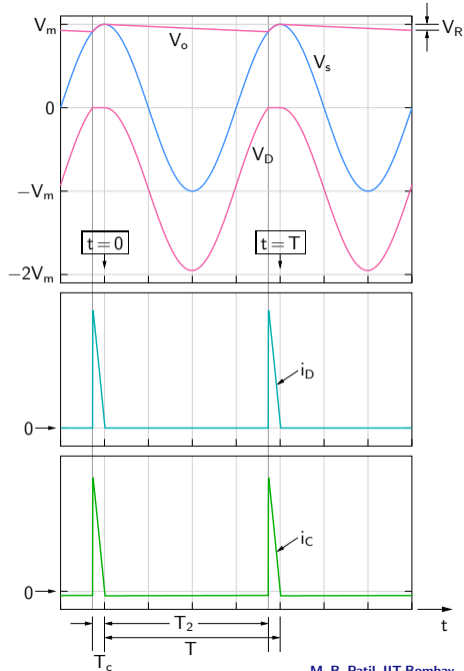
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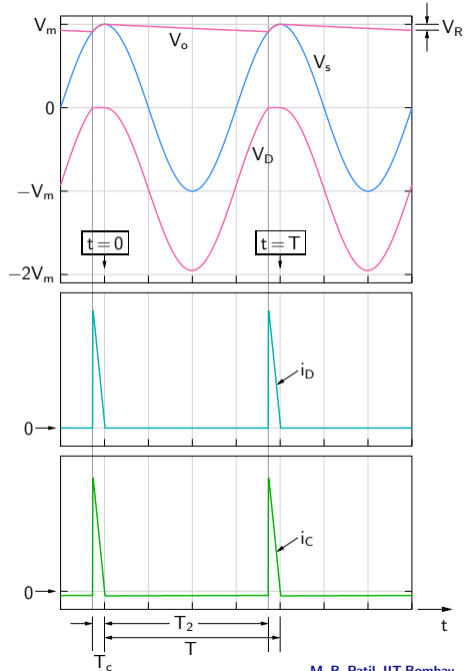
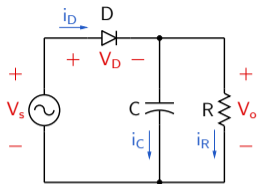
The drop in  $V_o(t)$  is given by the second term.

Using  $T_2 \approx T$ ,

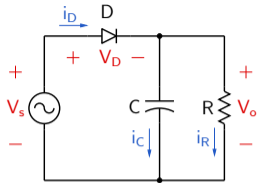
$$V_R = V_m \frac{T}{\tau} = V_m \frac{T}{RC}.$$



## Half-wave rectifier with capacitor filter



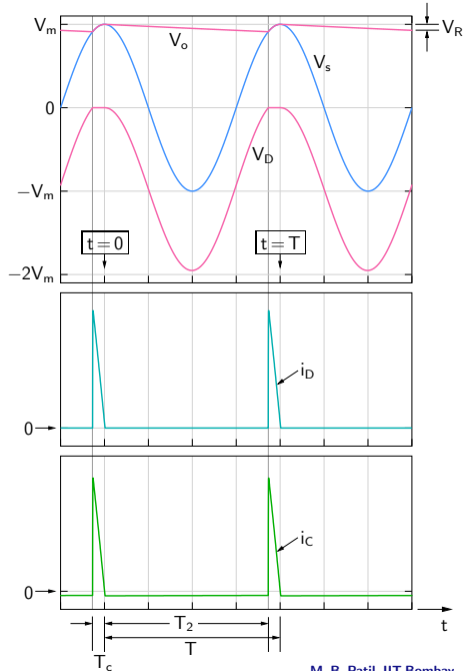
## Half-wave rectifier with capacitor filter



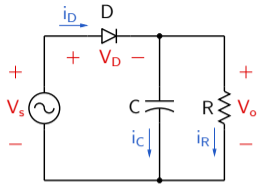
(a) Ripple voltage  $V_R$

2. Assuming  $i_C = i_R = \frac{V_o}{R} \approx \frac{V_m}{R}$  in the discharge phase, we get

$$i_C = \frac{V_m}{R} = C \frac{\Delta V_o}{\Delta t} \approx C \frac{V_R}{T} \rightarrow V_R = V_m \frac{T}{RC}$$



## Half-wave rectifier with capacitor filter

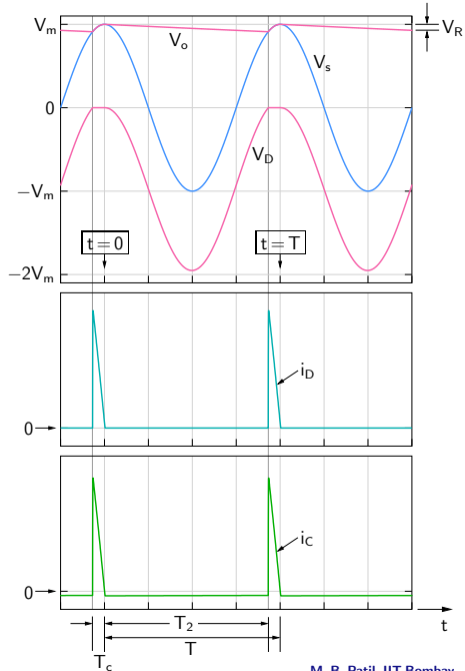


(a) Ripple voltage  $V_R$

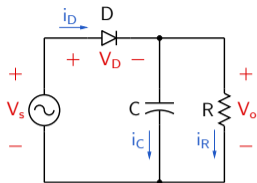
2. Assuming  $i_C = i_R = \frac{V_o}{R} \approx \frac{V_m}{R}$  in the discharge phase, we get

$$i_C = \frac{V_m}{R} = C \frac{\Delta V_o}{\Delta t} \approx C \frac{V_R}{T} \rightarrow V_R = V_m \frac{T}{RC}$$

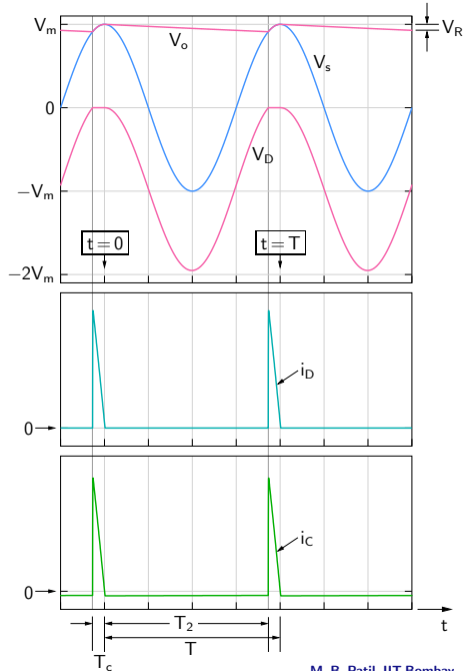
$$\rightarrow C = \frac{V_m}{V_R} \frac{T}{R} = \frac{16\text{ V}}{2\text{ V}} \frac{20\text{ ms}}{100\ \Omega} = 1600\ \mu\text{F}$$



## Half-wave rectifier with capacitor filter

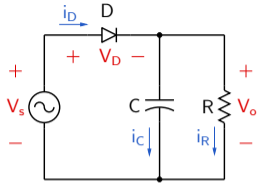


(b) Average diode current





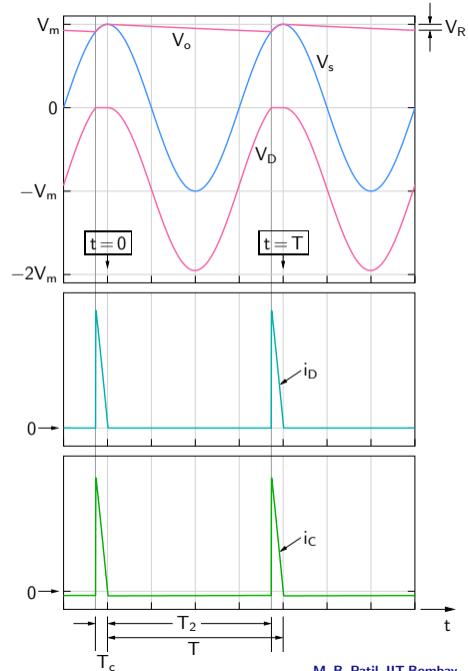
## Half-wave rectifier with capacitor filter



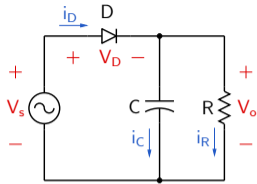
(b) Average diode current

Using charge balance,

$$\int_{T-T_c}^T (i_D - i_R) dt = \int_0^{T-T_c} i_R dt$$



## Half-wave rectifier with capacitor filter

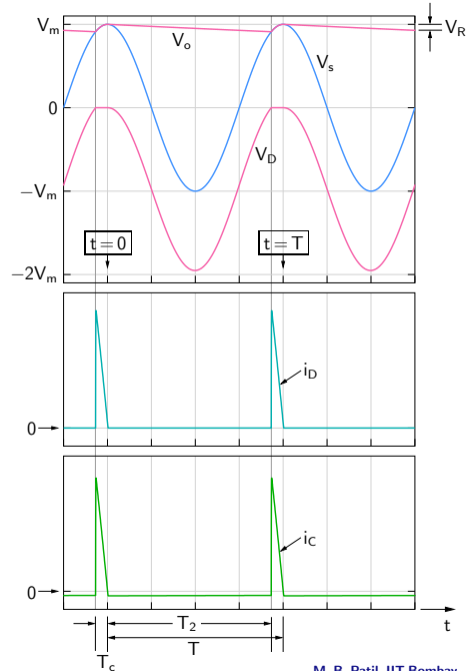


### (b) Average diode current

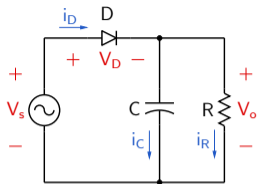
Using charge balance,

$$\int_{T-T_c}^T (i_D - i_R) dt = \int_0^{T-T_c} i_R dt$$

$$\rightarrow \int_{T-T_c}^T i_D dt = \int_0^T i_R dt.$$



## Half-wave rectifier with capacitor filter



### (b) Average diode current

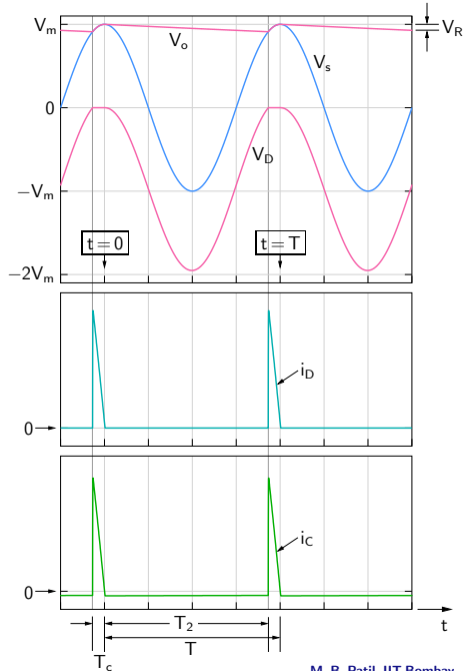
Using charge balance,

$$\int_{T-T_c}^T (i_D - i_R) dt = \int_0^{T-T_c} i_R dt$$

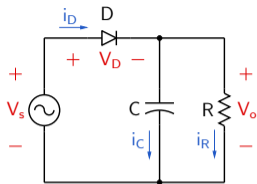
$$\rightarrow \int_{T-T_c}^T i_D dt = \int_0^{T-T_c} i_R dt.$$

$$i_D^{av} = \frac{1}{T} \int_0^T i_D dt = \frac{1}{T} \int_{T-T_c}^T i_D dt$$

$$= \frac{1}{T} \int_0^{T-T_c} i_R dt \approx \frac{V_m}{R}.$$



## Half-wave rectifier with capacitor filter



### (b) Average diode current

Using charge balance,

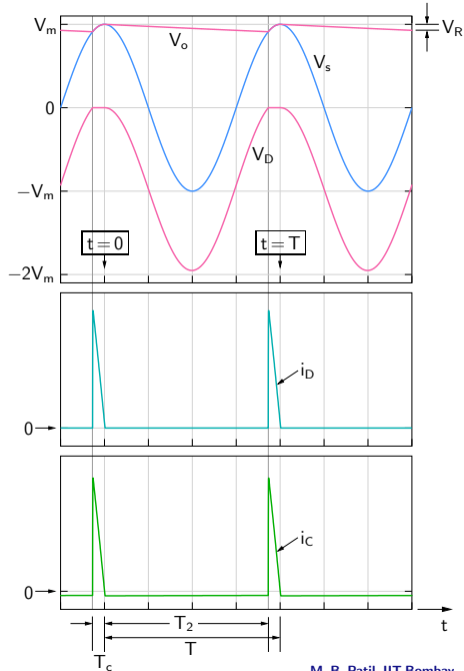
$$\int_{T-T_c}^T (i_D - i_R) dt = \int_0^{T-T_c} i_R dt$$

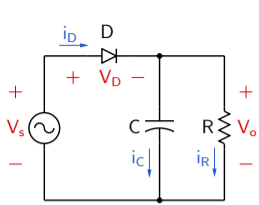
$$\rightarrow \int_{T-T_c}^T i_D dt = \int_0^{T-T_c} i_R dt.$$

$$i_D^{av} = \frac{1}{T} \int_0^T i_D dt = \frac{1}{T} \int_{T-T_c}^T i_D dt$$

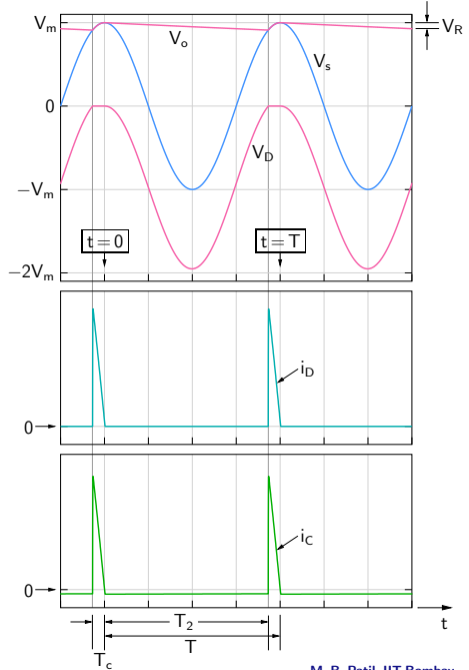
$$= \frac{1}{T} \int_0^{T-T_c} i_R dt \approx \frac{V_m}{R}.$$

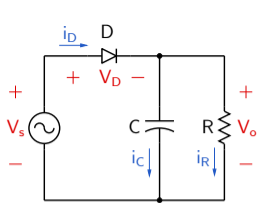
$$i_D^{av} \approx \frac{16 \text{ V}}{100 \Omega} = 160 \text{ mA}.$$





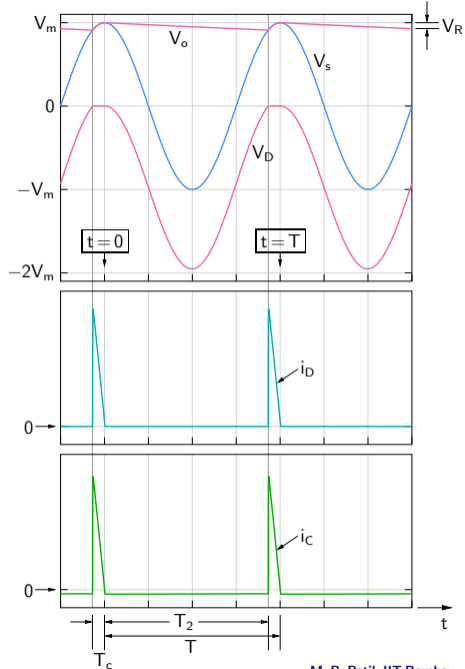
(b) Peak diode current

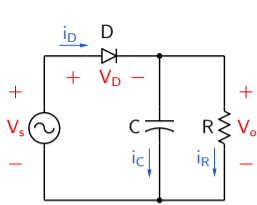




(b) Peak diode current

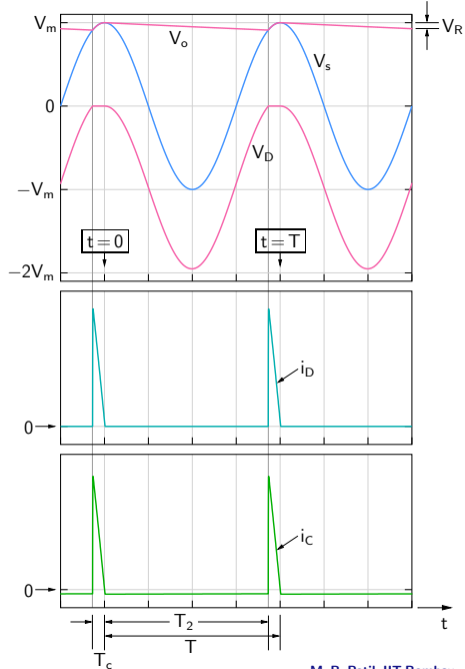
$$i_D^{\text{peak}} = C \frac{d}{dt} (V_m \cos \omega t) \Big|_{t=-T_c} + \frac{V_m}{R}$$

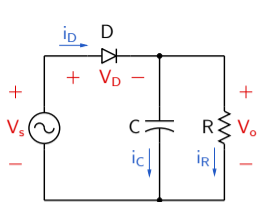




(b) Peak diode current

$$\begin{aligned}
 i_D^{\text{peak}} &= C \frac{d}{dt} (V_m \cos \omega t) \Big|_{t=-T_c} + \frac{V_m}{R} \\
 &= -\omega C V_m \sin(-\omega T_c) + \frac{16 \text{ V}}{100 \Omega} \\
 &= \omega C V_m \sin \omega T_c + 0.16
 \end{aligned}$$



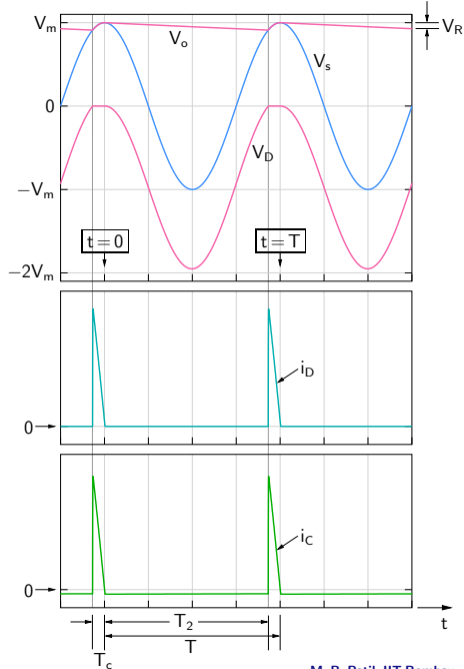


(b) Peak diode current

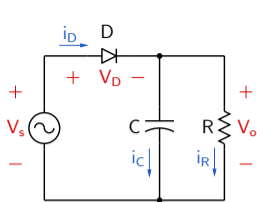
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 \end{aligned}$$

$$V_m \cos(-\omega T_c) = V_m - V_R, \text{ giving}$$

$$\omega T_c = \cos^{-1} \left( 1 - \frac{V_R}{V_m} \right) = \cos^{-1} \left( 1 - \frac{2}{16} \right) = 29^\circ.$$







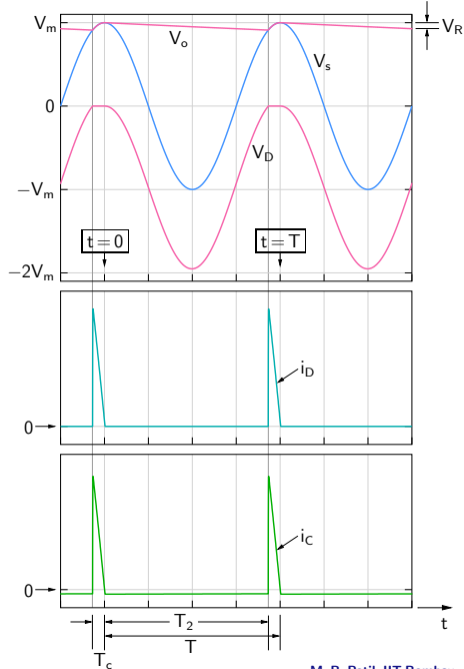
(b) Peak diode current

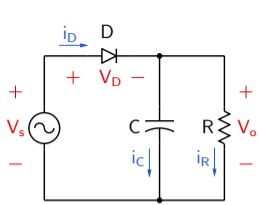
$$\begin{aligned}
 i_D^{\text{peak}} &= C \frac{d}{dt} (V_m \cos \omega t) \Big|_{t=-T_c} + \frac{V_m}{R} \\
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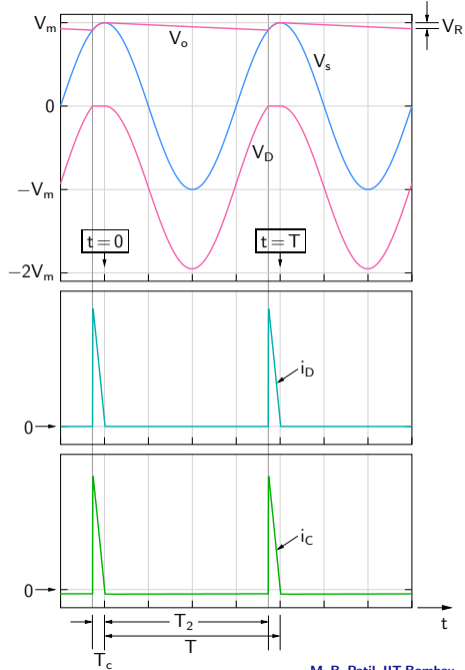
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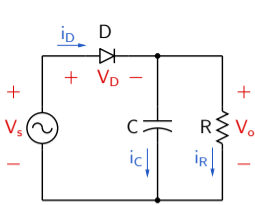
$$\begin{aligned}
 i_D^{\text{peak}} &= 2\pi \times 50 \times 1600 \times 10^{-6} \times 16 \times \sin 29^\circ + 0.16 \\
 &= 3.89 + 0.16 = 4.05 \text{ A.}
 \end{aligned}$$





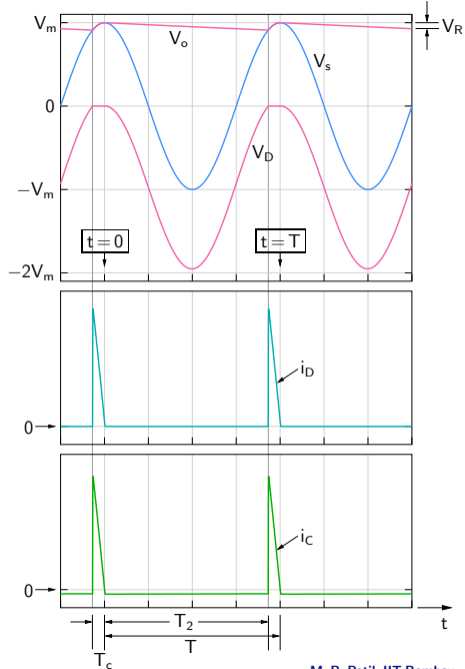
(b) Peak diode current: analytic expression

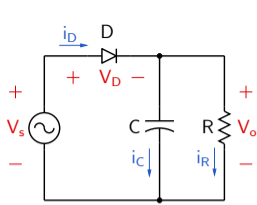




(b) Peak diode current: analytic expression

$$V_m \cos(-\omega T_c) = V_m - V_R \rightarrow \cos \omega T_c = 1 - \frac{V_R}{V_m} \equiv 1 - x$$

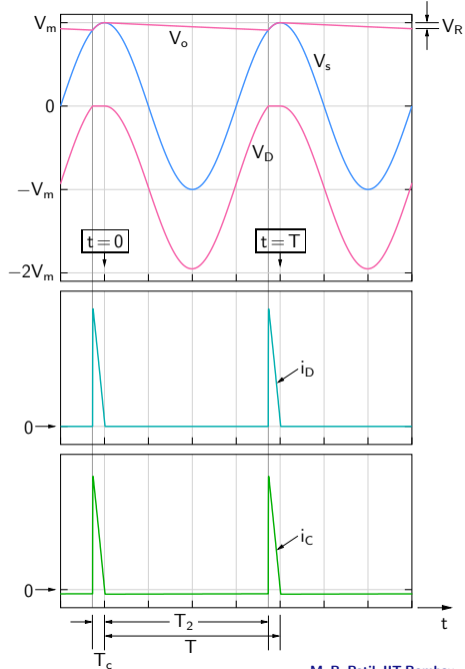


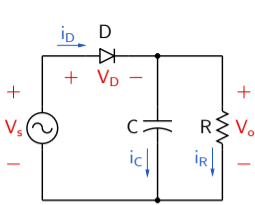


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$$\begin{aligned} \sin \omega T_c &= \sqrt{1 - \cos^2 \omega T_c} = \sqrt{1 - (1 - x)^2} \\ &= \sqrt{1 - (1 - 2x + x^2)} \approx \sqrt{2x} = \sqrt{\frac{2V_R}{V_m}} \end{aligned}$$



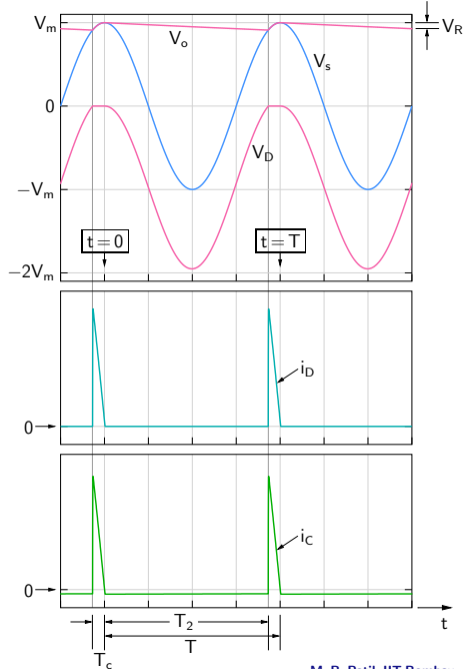


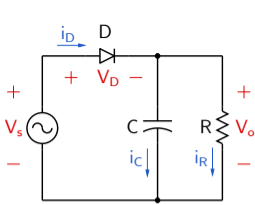
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$$\begin{aligned} i_D^{\text{peak}} &= i_R + C \frac{d}{dt} (V_m \cos \omega t) \Big|_{t=-T_c} \\ &= i_R + \omega C V_m \sin \omega T_c \\ &= i_R + \omega C V_m \sqrt{\frac{2V_R}{V_m}} \end{aligned}$$





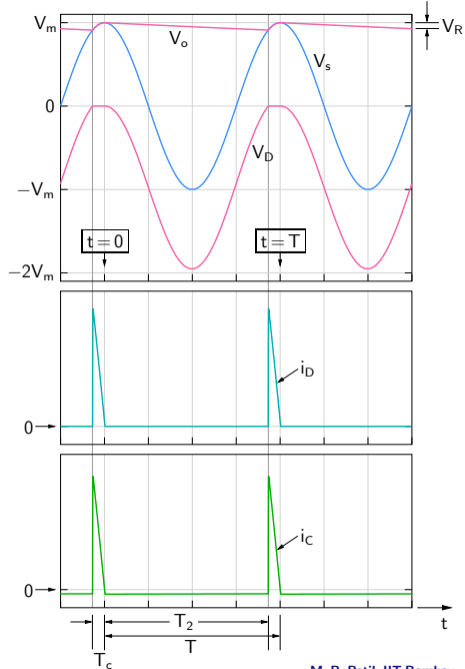
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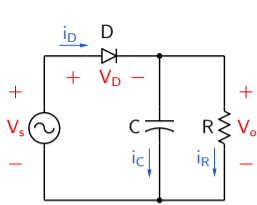
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(c) Maximum reverse bias  $\approx 2 V_m = 32 \text{ V}$ .





(b) Peak diode current: analytic expression

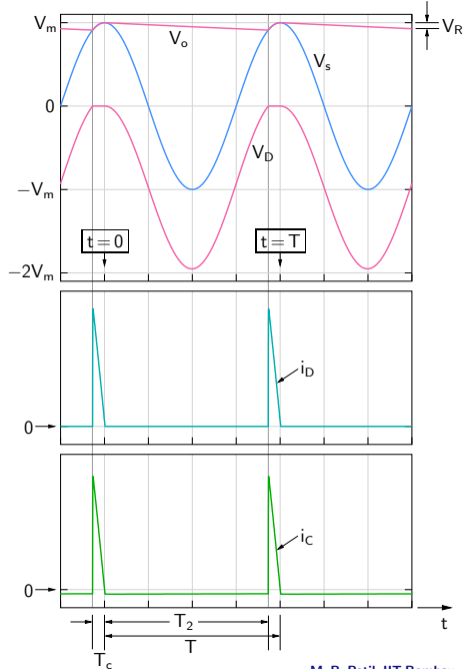
$$V_m \cos(-\omega T_c) = V_m - V_R \rightarrow \cos \omega T_c = 1 - \frac{V_R}{V_m} \equiv 1 - x$$

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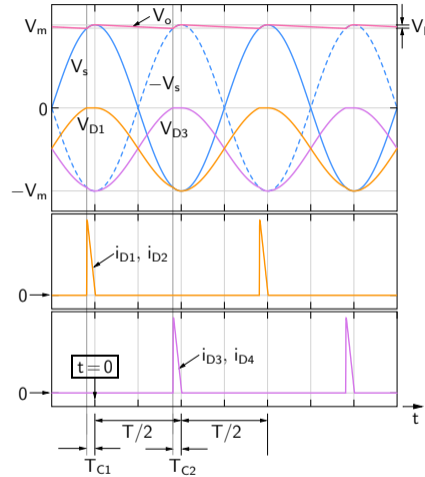
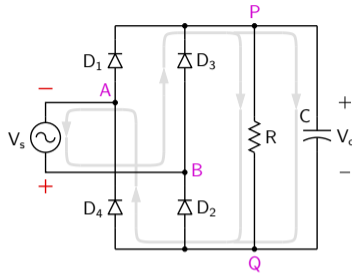
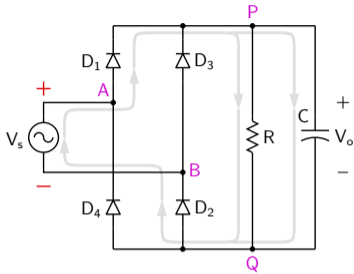
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SEQUEL file: ee101\_half\_rectifier.sqproj

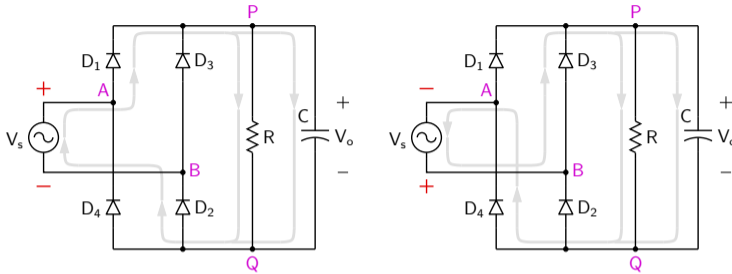


# Full-wave (bridge) rectifier with capacitor filter

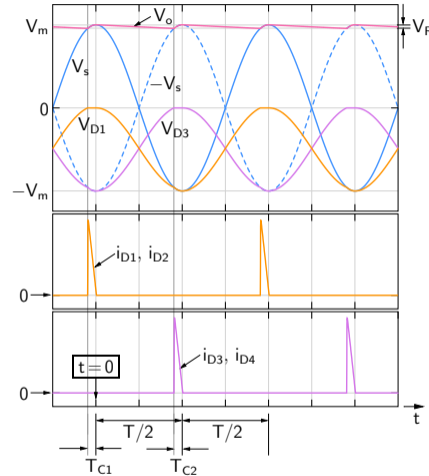




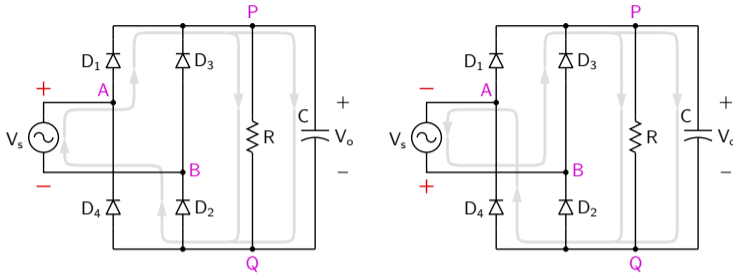
# Full-wave (bridge) rectifier with capacitor filter



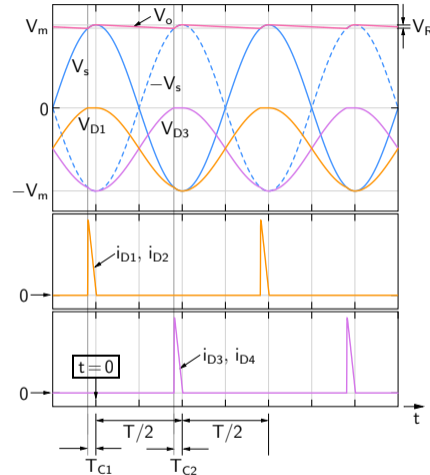
- \* As in the half-wave rectifier case, we have charging and discharging intervals, and  $V_o \approx V_m$  is maintained.



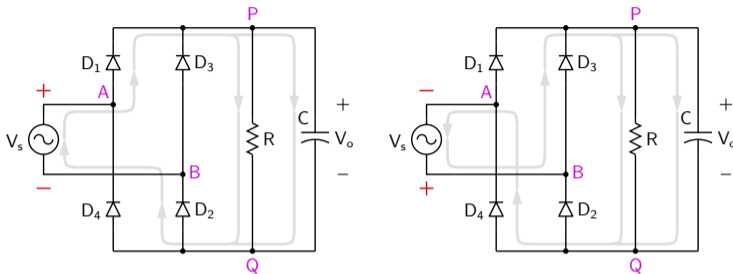
# Full-wave (bridge) rectifier with capacitor filter



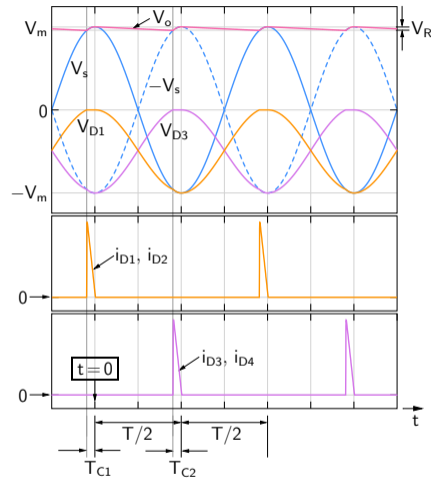
- \* As in the half-wave rectifier case, we have charging and discharging intervals, and  $V_o \approx V_m$  is maintained.
- \* Charging through  $D_1, D_2$  takes place when  $V_o(t)$  falls below  $V_s(t)$ .



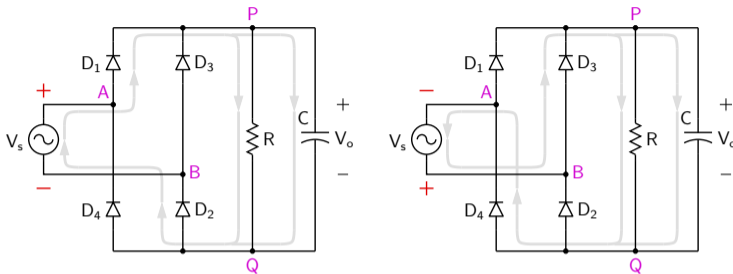
# Full-wave (bridge) rectifier with capacitor filter



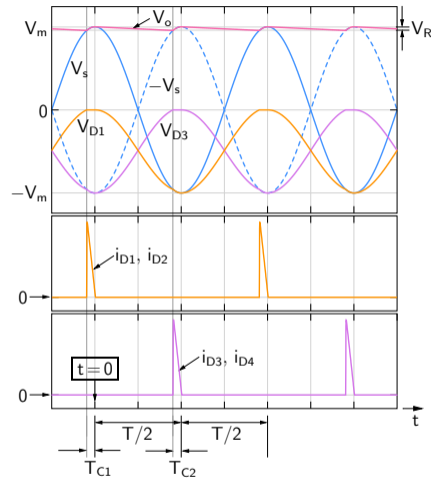
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- \* Charging through  $D_3, D_4$  takes place when  $V_o(t)$  falls below  $-V_s(t)$ .



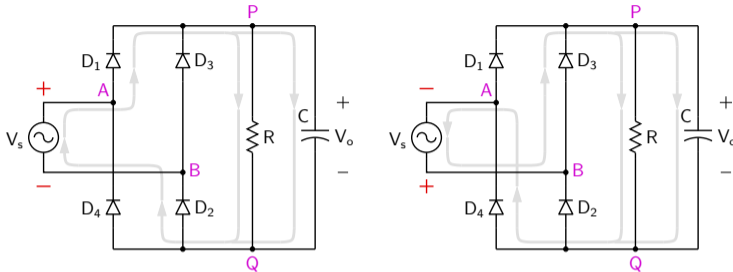
# Full-wave (bridge) rectifier with capacitor filter



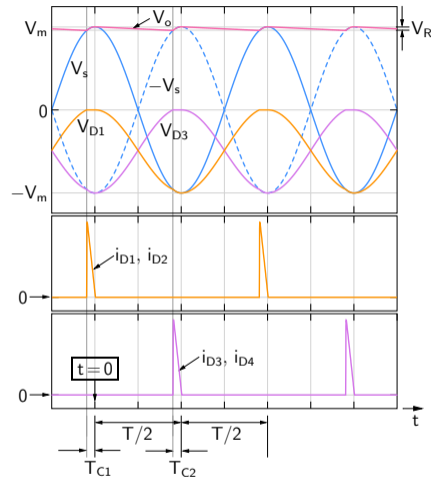
- \* As in the half-wave rectifier case, we have charging and discharging intervals, and  $V_o \approx V_m$  is maintained.
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- \* Charging through  $D_3, D_4$  takes place when  $V_o(t)$  falls below  $-V_s(t)$ .
- \* The discharging interval is typically much longer than the charging intervals ( $T_{C1}$  and  $T_{C2}$ ).



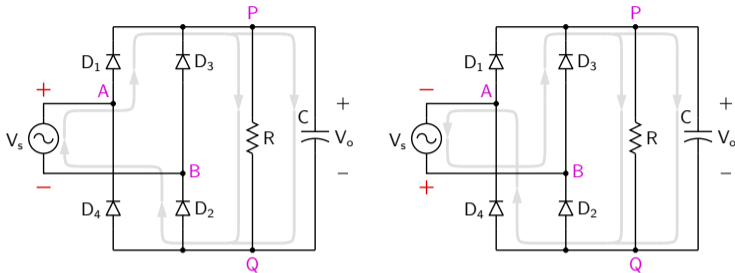
# Full-wave (bridge) rectifier with capacitor filter



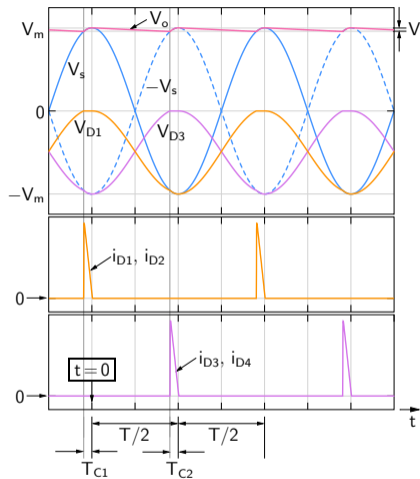
- \* As in the half-wave rectifier case, we have charging and discharging intervals, and  $V_o \approx V_m$  is maintained.
- \* Charging through  $D_1, D_2$  takes place when  $V_o(t)$  falls below  $V_s(t)$ .
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- \* The discharging interval is typically much longer than the charging intervals ( $T_{C1}$  and  $T_{C2}$ ).
- \* The maximum reverse bias across any of the diodes is  $V_m$ .



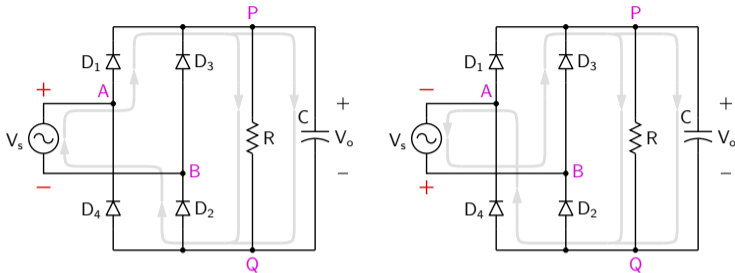
# Full-wave rectifier with capacitor filter



$V_m = 16\text{ V}$ ,  $f = 50\text{ Hz}$ ,  $R = 100\ \Omega$ . For a ripple voltage  $V_R = 2\text{ V}$ , find (a) the filter capacitance  $C$ , (b) average and peak diode currents, (c) maximum reverse voltage across the diode. (Let  $V_{on} = 0\text{ V}$ .)

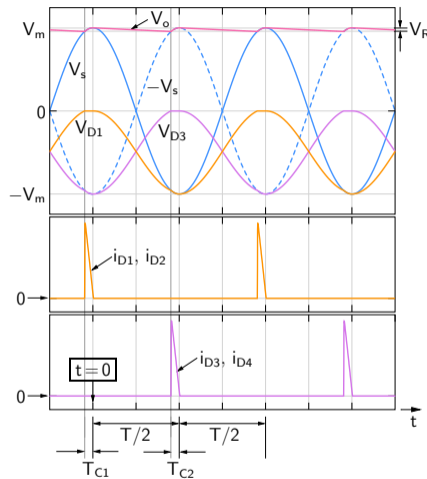


# Full-wave rectifier with capacitor filter

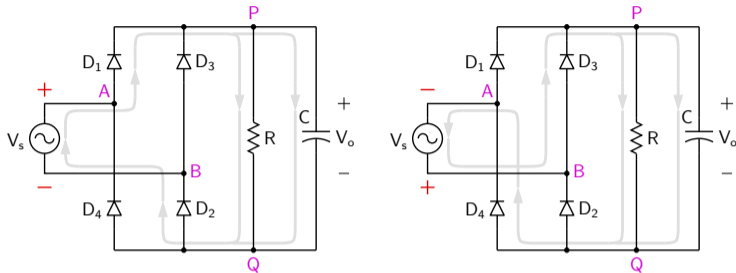


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(a) filter capacitance:



# Full-wave rectifier with capacitor filter

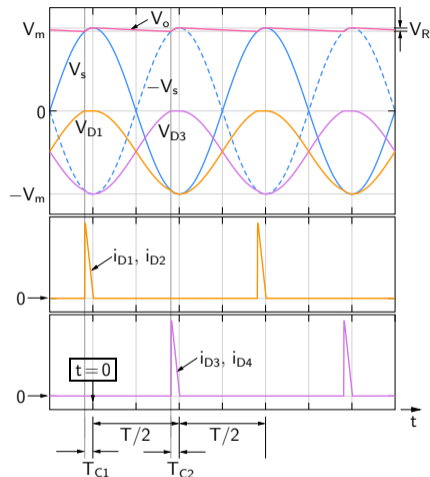


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(a) filter capacitance:

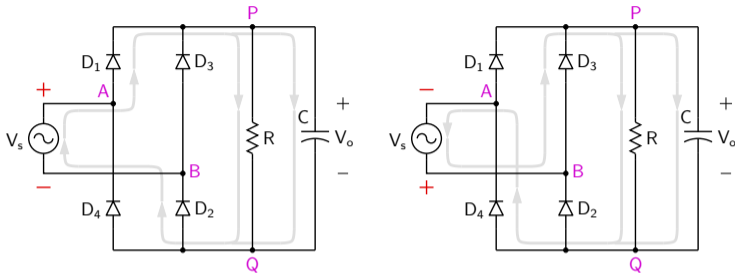
Assuming  $i_C = i_R = \frac{V_o}{R} \approx \frac{V_m}{R}$  in the discharge phase, we get

$$i_C = \frac{V_m}{R} = C \frac{\Delta V_o}{\Delta t} \approx C \frac{V_R}{T/2} \rightarrow V_R = V_m \frac{T}{2RC}.$$





# Full-wave rectifier with capacitor filter



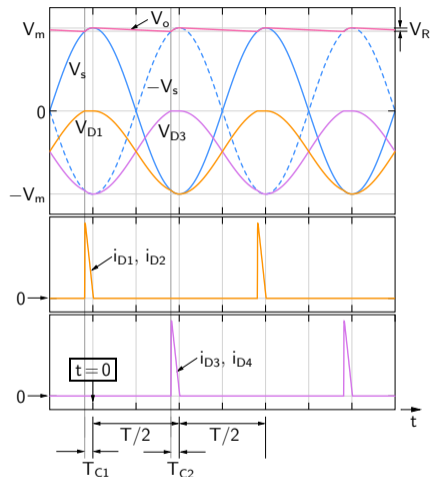
$V_m = 16\text{ V}$ ,  $f = 50\text{ Hz}$ ,  $R = 100\ \Omega$ . For a ripple voltage  $V_R = 2\text{ V}$ , find (a) the filter capacitance  $C$ , (b) average and peak diode currents, (c) maximum reverse voltage across the diode. (Let  $V_{on} = 0\text{ V}$ .)

(a) filter capacitance:

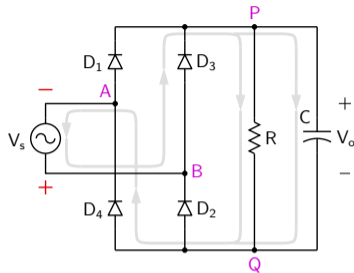
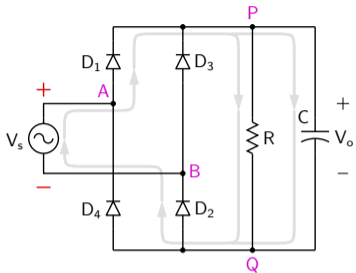
Assuming  $i_C = i_R = \frac{V_o}{R} \approx \frac{V_m}{R}$  in the discharge phase, we get

$$i_C = \frac{V_m}{R} = C \frac{\Delta V_o}{\Delta t} \approx C \frac{V_R}{T/2} \rightarrow V_R = V_m \frac{T}{2RC}$$

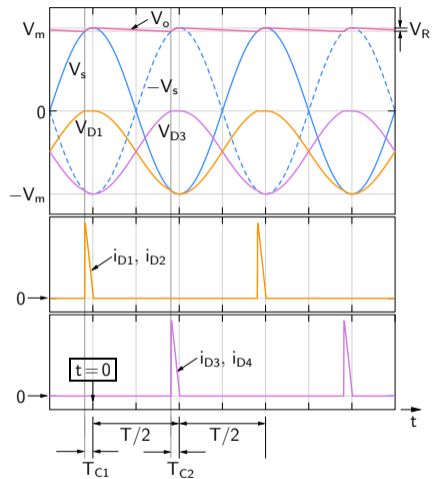
$$\rightarrow C = \frac{1}{2} \frac{V_m}{V_R} \frac{T}{R} = \frac{1}{2} \frac{16\text{ V}}{2\text{ V}} \frac{20\text{ ms}}{100\ \Omega} = 800\ \mu\text{F}$$



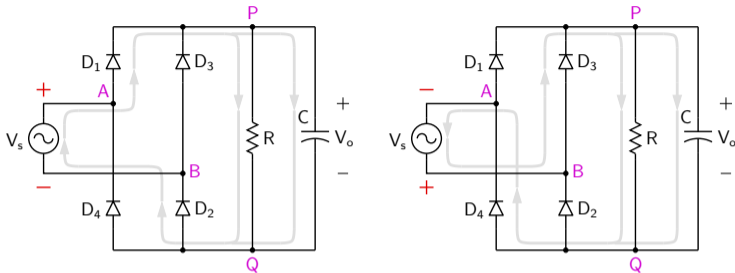
# Full-wave rectifier with capacitor filter



(b) Average diode current

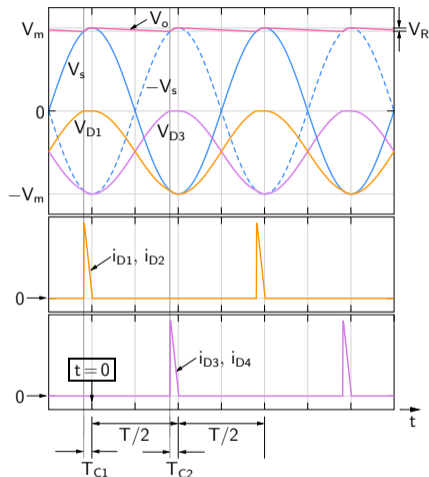


# Full-wave rectifier with capacitor filter

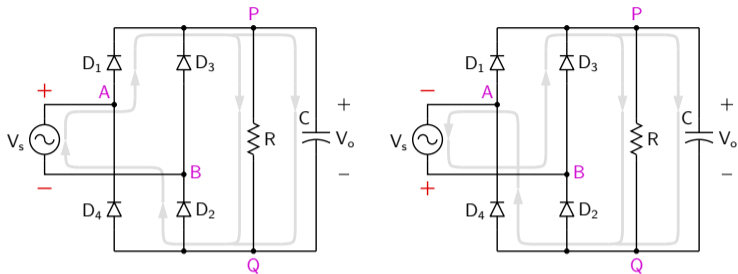


## (b) Average diode current

Half of the charge lost by the capacitor is supplied by  $i_{D1}$  ( $= i_{D2}$ ), and the other half by  $i_{D3}$  ( $= i_{D4}$ ).



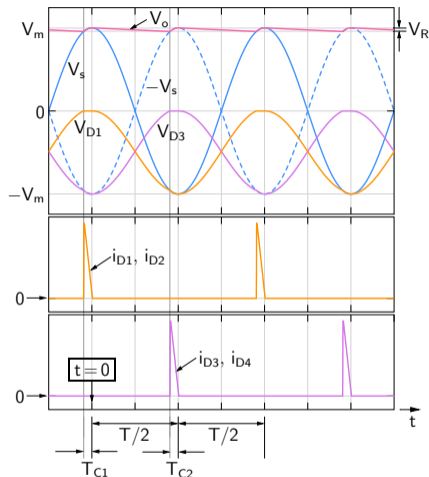
# Full-wave rectifier with capacitor filter



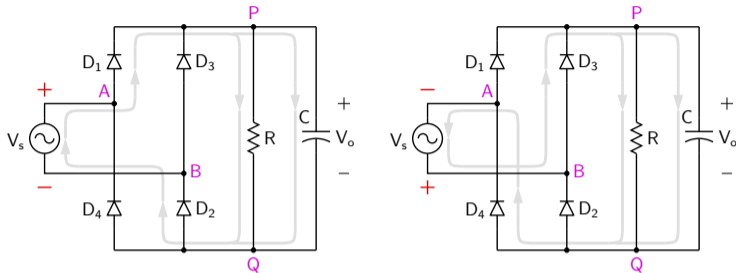
## (b) Average diode current

Half of the charge lost by the capacitor is supplied by  $i_{D1}$  ( $= i_{D2}$ ), and the other half by  $i_{D3}$  ( $= i_{D4}$ ).

$$i_D^{av} = \frac{1}{T} \times \frac{1}{2} \times (\text{Charge lost in one cycle})$$



# Full-wave rectifier with capacitor filter

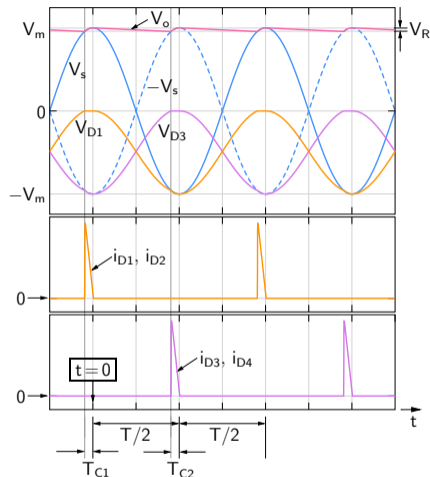


## (b) Average diode current

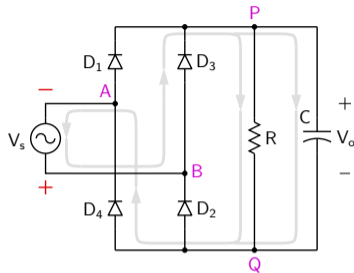
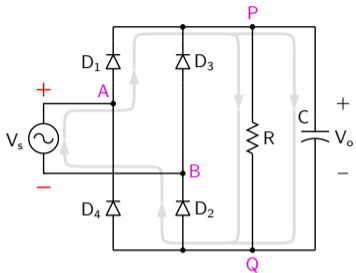
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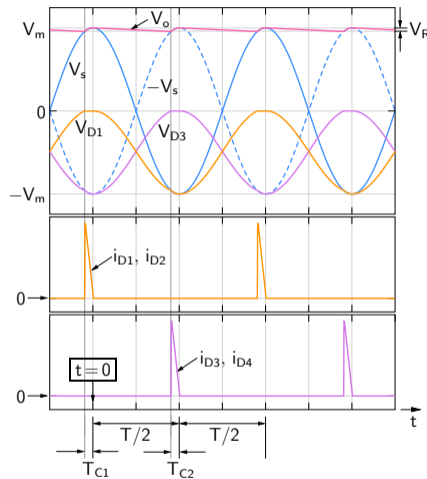
$$\approx \frac{1}{T} \times \frac{1}{2} \times \left( \frac{V_m}{R} \times T \right) = \frac{V_m}{2R} = \frac{16 \text{ V}}{2 \times 100 \Omega} = 80 \text{ mA.}$$



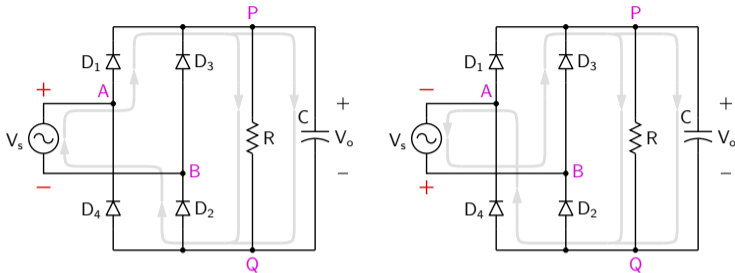
# Full-wave rectifier with capacitor filter



(b) Peak diode current

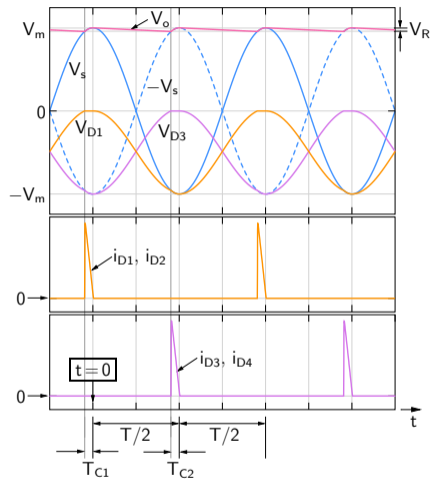


# Full-wave rectifier with capacitor filter

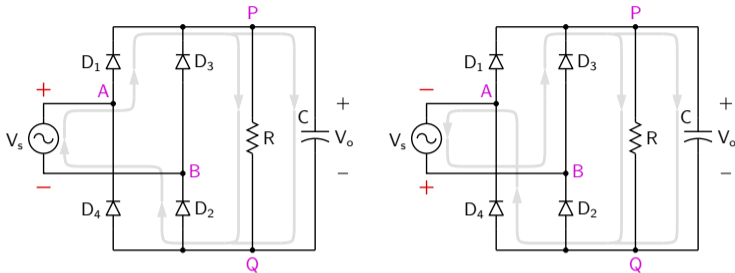


(b) Peak diode current

$$\begin{aligned}
 i_{D1}^{\text{peak}} &= C \frac{d}{dt} (V_m \cos \omega t) \Big|_{t=-T_{C1}} + \frac{V_m}{R} \\
 &= -\omega C V_m \sin(-\omega T_{C1}) + \frac{16 \text{ V}}{100 \Omega} \\
 &= \omega C V_m \sin \omega T_{C1} + 0.16
 \end{aligned}$$



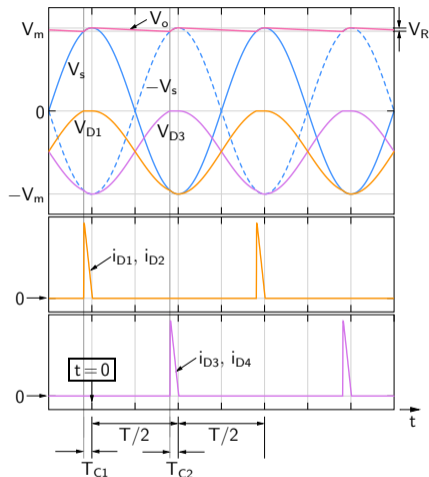
# Full-wave rectifier with capacitor filter



(b) Peak diode current

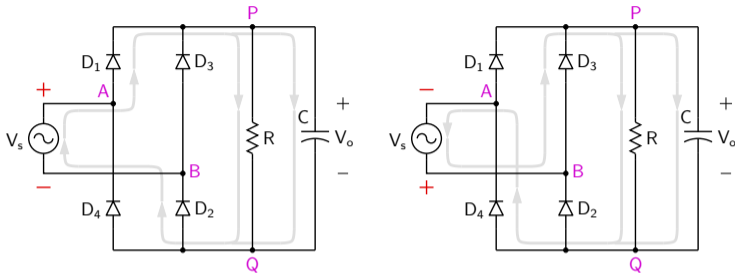
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$$\omega T_{C1} = \cos^{-1} \left( 1 - \frac{V_R}{V_m} \right) = \cos^{-1} \left( 1 - \frac{2}{16} \right) = 29^\circ.$$





# Full-wave rectifier with capacitor filter

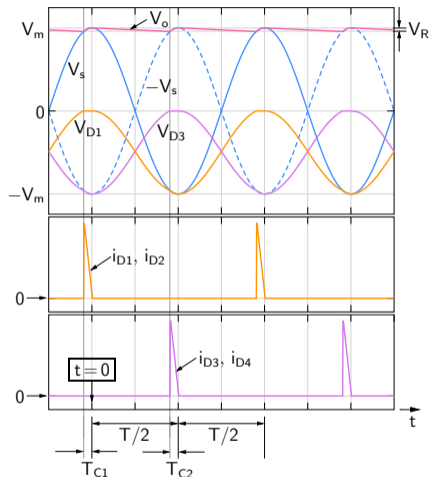


(b) Peak diode current

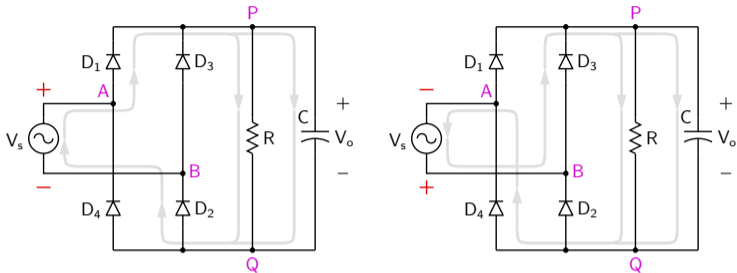
$$\begin{aligned}
 i_{D1}^{\text{peak}} &= C \frac{d}{dt} (V_m \cos \omega t) \Big|_{t=-T_{C1}} + \frac{V_m}{R} \\
 &= -\omega C V_m \sin(-\omega T_{C1}) + \frac{16 \text{ V}}{100 \Omega} \\
 &= \omega C V_m \sin \omega T_{C1} + 0.16
 \end{aligned}$$

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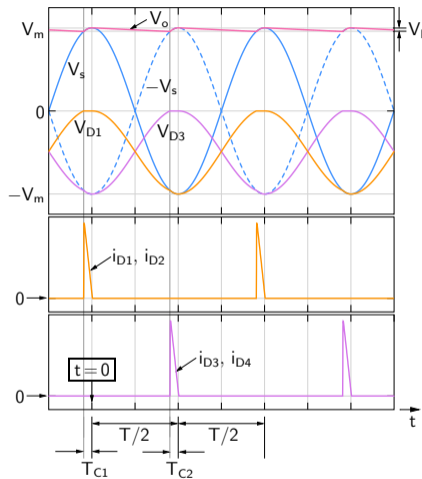
$$\begin{aligned}
 i_{D1}^{\text{peak}} &= 2\pi \times 50 \times 800 \times 10^{-6} \times 16 \times \sin 29^\circ + 0.16 \\
 &= 1.95 + 0.16 = 2.1 \text{ A}.
 \end{aligned}$$



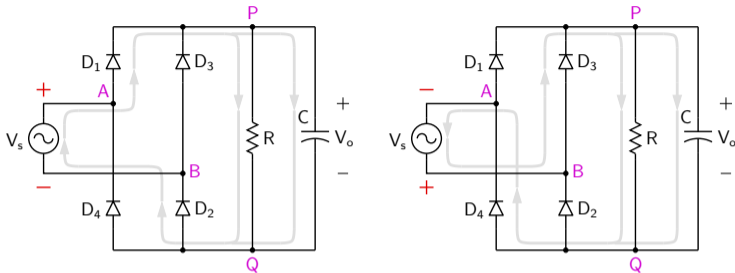
# Full-wave rectifier with capacitor filter



(c) Maximum reverse bias =  $V_m = 16\text{ V}$ .

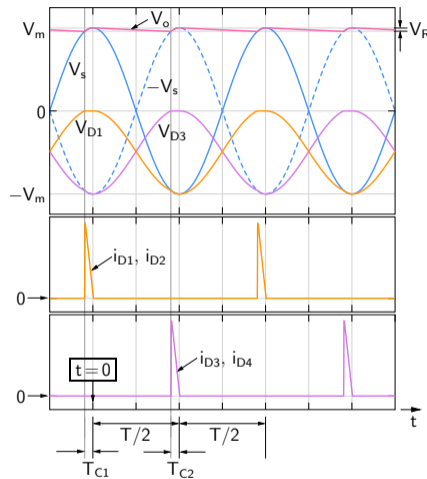


# Full-wave rectifier with capacitor filter



(c) Maximum reverse bias =  $V_m = 16\text{ V}$ .

SEQUEL file: [diode\\_rectifier\\_4.sqproj](#)



## Comparison of half-wave and full-wave (bridge) rectifiers with capacitive filter

For the same source voltage ( $V_m \sin \omega t$ ), load ( $R$ ), and ripple voltage ( $V_R$ ), compare the half-wave and full-wave rectifiers.

## Comparison of half-wave and full-wave (bridge) rectifiers with capacitive filter

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Parameter	Half-wave	Full-wave
Number of diodes	1	4
Filter capacitance	$C$	$C/2$
Average diode current	$i_D^{\text{av}}$	$i_D^{\text{av}}/2$
Peak diode current	$i_D^{\text{peak}}$	$i_D^{\text{peak}}/2$
Maximum reverse voltage	$2 V_m$	$V_m$