## ee101\_voltage\_doubler\_1.sqproj



Figure 1: (a) Voltage pump circuit, (b) Equivalent circuit during T/2 < t < T.

The circuit shown in Fig. 1 (a) acts as a "voltage pump," giving an output  $V_o \equiv V_{C2} = 2V_{DD}$  in the steady state if the diodes are ideal with  $V_{on} = 0$  V. Let us consider the case  $C_1 = C_2$ . We will assume the on resistance of the diodes to be negligibly small (which means that the capacitors charge or discharge instantaneously as the clock changes) and the off resistance to be large (which means that the capacitor voltage does not change unless there is a current path involving a forward-biased diode).

Let us begin with  $V_{C1} = V_{C2} = 0$  V. At t = 0,  $V_{clock} = 0$  V. As a result, both  $C_1$  and  $C_2$  get charged to  $V_{DD} = 5$  V (see Fig. 2). At t = T/2,  $V_{clock}$  changes from 0 V to 5 V. The voltage at the other end of  $C_1$  (node A) would then also tend to increase by 5 V, i.e., it would tend to change from its previous value of 5 V to the new value of 10 V. However, this would turn on  $D_2$  (whose n end is at 5 V), and  $V_A$  would not quite reach 10 V but settle at some intermediate value. Note that all of these changes happen instantaneously thanks to our assumption of ideal diodes.

What intermediate value will  $V_A$  reach? To answer this question, let us note the following points regarding the circuit operation in the interval T/2 < t < T.

- (a)  $V_{C2}$  can only increase since the diode  $D_2$  will not allow  $C_2$  to discharge.
- (b)  $D_1$  does not conduct in this interval since  $V_A > 5$  V.
- (c)  $D_2$  does conduct for the reason mentioned above, viz., the node voltage at A would tend to increase to 10 V.



Figure 2: Waveforms for voltage pump circuit of Fig. 1.

The circuit then simplifies to that shown in Fig. 1 (b) in which  $D_1$  has been replaced with an open circuit and  $D_2$  with a short circuit. Since  $C_1 = C_2$ , the two capacitors will experience the same voltage change (see ee101\_rc8.sqproj). Since  $V_{C1}$  and  $V_{C2}$  have opposite polarity (see Fig. 1 (a)), when  $V_{C2}$  increases by  $\Delta V$ ,  $V_{C1}$  decreases by the same amount. In other words,  $V_{C1}$  changes from 5 to  $5 - \Delta V$ , and  $V_{C2}$  changes from 5 to  $5 + \Delta V$ . This continues until the current stops flowing due to the following condition.

$$V_{\text{clock}} + V_{C1} = V_{C2}$$
, i.e.,  $5 + (5 - \Delta V) = (5 + \Delta V) \rightarrow \Delta V = 2.5 \text{ V}$ . (1)

The new  $V_{C2}$  is therefore 5 + 2.5 = 7.5 V, and the new  $V_{C1}$  is 5 - 2.5 = 2.5 V, as seen in Fig. 2. At t = T,  $V_{clock}$  goes to 0 V again which makes  $C_1$  charge from 2.5 V to 5 V once again.  $D_2$ does not conduct since its n end is already at a voltage greater than  $V_{DD}$ . At t = 3T/2,  $V_{clock}$  changes from 0 V to 5 V. Following the above analysis for the transition at t = T/2, we can say that  $V_{C1}$  will now change from 5 to  $5 - \Delta V$ , and  $V_{C2}$  from 7.5 to  $7.5 + \Delta V$  until  $V_{clock} + V_{C1}$  becomes equal to  $V_{C2}$ , i.e.,

$$5 + (5 - \Delta V) = (7.5 + \Delta V) \rightarrow \Delta V = 1.25 \,\mathrm{V}\,,$$
 (2)

as seen in Fig. 2. Eventually,  $V_{C2} \rightarrow 2V_{DD}$  as desired.

## Exercise Set

- 1. Work out the next few values of  $V_{C2}$ . Verify with simulation.
- 2. How will the waveforms change if
  - (a)  $C_1 = 1 \text{ pF}, C_2 = 0.25 \text{ pF}.$
  - (b)  $C_1 = 0.25 \,\mathrm{pF}, C_2 = 1 \,\mathrm{pF}.$

Verify with simulation.

- 3. For  $C_1 = C_2 = 1 \text{ pF}$ , how will the waveforms change if  $V_{\text{on}}$  for the diodes is 0.7 V instead of 0 V. Verify with simulation.
- 4. If  $V_{\text{on}}$  is 0.5 V and 1 V for  $D_1$  and  $D_2$ , respectively, what would be the steady-state values of  $V_{C1}$  and  $V_{C2}$ ? Verify with simulation.